CHAPTER 3

AQUEOUS SOLUTIONS AND CHEMICAL EQUILIBRIA

In this chapter,

- chemical equilibrium including calculations of chemical composition and of equilibrium concentrations for monoprotic acid/base systems will be considered.
- buffer solutions, which are extremely important in many areas of science, and describe the properties of these solutions will be discussed.

THE CHEMICAL COMPOSITION OF AQUEOUS SOLUTIONS

Electrolytes form ions when dissolved in water (or certain other solvents) and thus produce solutions that conduct electricity.

Strong electrolytes ionize essentially completely in a solvent, Weak electrolytes ionize only partially.

Conducting electricity by weak electrolytes <<< strong electrolyte

TABLE 9-1

Classification of Electrolytes

Strong	Weak
1. Inorganic acids such as HNO ₃ , HClO ₄ ,	 Many inorganic acids, including H₂CO₃,
H ₂ SO ₄ *, HCl, HI, HBr, HClO ₃ , HBrO ₃	H ₃ BO ₃ , H ₃ PO ₄ , H ₂ S, H ₂ SO ₃
2. Alkali and alkaline-earth hydroxides	2. Most organic acids
3. Most salts	3. Ammonia and most organic bases
	4. Halides, cyanides, and thiocyanates of
	Hg, Zn, and Cd

*H₂SO₄ is completely dissociated into HSO₄²⁻ and H₃O⁺ ions and for this reason is classified as a **strong electrolyte**.

 HSO_4^{2-} ion is a weak electrolyte and is only partially dissociated into SO_4^{2-} and H_3O^+ .

Brønsted-Lowry Theory

An acid donates protons.

A base is a proton acceptor.

only in the presence of a proton acceptor (base).

only in the presence of a proton donor (acid).

A salt is produced in the reaction of an acid with a base.

NaCl, Na₂SO₄, NaOOCCH₃

Arrhenius acid-base definition

(acid produces H₃O⁺ and base forms OH⁻ in water.)

Lewis acid-base definition

(acid accepts and shares electron and bases share their electrons)

A conjugate base is formed when an acid loses a proton.

$$H_2O + HNO_2 \rightleftharpoons H_3O^+ + NO_2^ base_1$$
 $acid_2$ $conjugate$ $conjugate$ $base_2$

 $base_2 + proton = acid_2$

conjugate acid/base pair

acid₁/base₁

 $acid_1 \rightleftharpoons base_1 + proton$

A conjugate acid is formed when an base gains a proton.

$$NH_3 + H_2O \rightleftharpoons NH_4^+ + OH_5^ base_1$$
 $acid_2$ $conjugate$ $conjugate$ $acid_1$ $base_2$

conjugate acid/base pair base₂/acid₂

A substance acts as an acid only in the presence of a base and vice versa.

Neutralization:
$$acid_1 + base_2 \rightleftharpoons base_1 + acid_2$$

$$HNO_2 + NH_3 \Leftrightarrow NH_4^+ + NO_2^-$$

$$NO_2^- + H_2O \Leftrightarrow HNO_2^- + OH^-$$

base₁ acid₂ conjugate conjugate
acid₁ base₂

$$NH_4^+ + H_2O \Leftrightarrow NH_3 + H_3O^+$$

 $acid_1$ base₂ conjugate conjugate
 $base_1$ acid₂

Amphiprotic Species

Species that have both acidic and basic properties are amphiprotic.

behaves as a base in the presence of a proton donor.

$$H_2PO_4^- + H_3O^+ \rightleftharpoons H_3PO_4 + H_2O_{\text{base}_1}$$

behaves as an acid in the presence of a proton acceptor.

$$H_2PO_4^- + OH^- \rightleftharpoons HPO_4^{2-} + H_2O_{acid_1}$$

Water acts as a proton acceptor (base) and as a proton donor (acid):

Amphiprotic solvent

The simple amino acids are an important class of amphiprotic compounds that contain both a weak acid and a weak base functional group.

an amino acid, undergoes a kind of internal acid/base reaction to produce a zwitterion—a species that has both a positive and a negative charge.

$$NH_2CH_2COOH \rightleftharpoons NH_3^+CH_2COO^-$$
glycine zwitterion

acid/base reaction between a carboxylic acid and an amine

$$R'COOH + R''NH_2 \rightleftharpoons R'COO^- + R''NH_3^+$$
 $acid_1$ $base_2$ $base_1$ $acid_2$

Water acts as a proton acceptor (base) and as a proton donor (acid): Amphiprotic solvent

Other common amphiprotic solvents are methanol, ethanol, and anhydrous acetic acid.

$$NH_{3} + CH_{3}OH \rightleftharpoons NH_{4}^{+} + CH_{3}O^{-}$$

$$CH_{3}OH + HNO_{2} \rightleftharpoons CH_{3}OH_{2}^{+} + NO_{2}^{-}$$

$$CH_{3}OH \Rightarrow acid_{2} \Rightarrow conjugate \Rightarrow acid_{1}$$

Autoprotolysis (autoionization)

Amphiprotic solvents undergo **self-ionization**, or **autoprotolysis**, to form a pair of ionic species.

Water slightly undergoes autoprotolysis at room temperature. Thus, the hydronium (H₃O⁺) and hydroxide ion(OH⁻) concentrations in pure water are only about 10⁻⁷ M.

Strengths of Acids and Bases

strong acids: reaction with the solvent is sufficiently complete that no undissociated solute molecules are left in aqueous solution.

weak acids: react incompletely with water to give solutions containing significant quantities of both the parent acid and its conjugate base.

Note that acids can be cationic, anionic, or electrically neutral.

The same holds for bases.

The **common strong acids** include HCl, HBr, HI, HClO₄, HNO₃, the first proton in H₂SO₄, and the organic sulfonic acid RSO₃H.

The **common strong bases** include NaOH, KOH, Ba(OH)₂, and the quaternary ammonium hydroxide R₄NOH, where R is an alkyl group such as CH₃ or C₂H₅.

Conjugate acids/bases of strong acids/bases do not undergo a hydrolysis reaction. They are not strong enough to produce hydronium (H₃O+) and hydroxide ion(OH-).

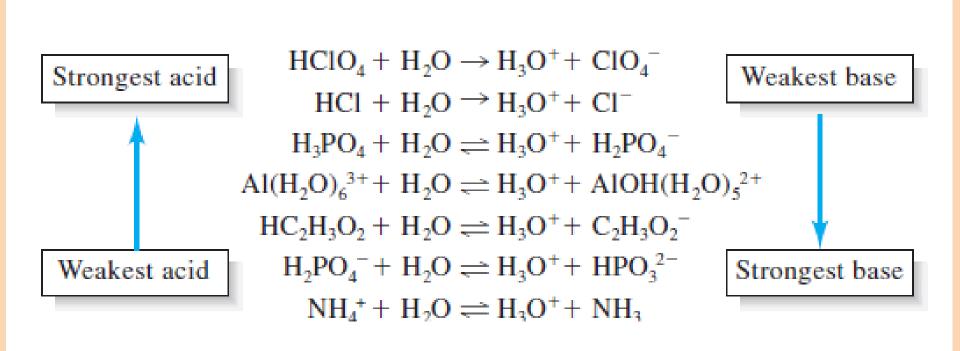
Conjugate acids/bases of weak acids are strong enough to undergo a hydrolysis reaction. They are produce hydronium (H₃O⁺) or hydroxide ion(OH⁻) and change the pH of the solution.

Note that acids can be cationic, anionic, or electrically neutral.

The same holds for bases.

The tendency of a solvent to accept or donate protons determines the strength of a solute acid or base dissolved in it.

Water, is a leveling solvent for perchloric, hydrochloric, and nitric acids because all three are completely ionized in this solvent and show no differences in strength.



In a **leveling solvent**, several acids are **completely dissociated** and show the same strength.

14

Anhydrous acetic acid acts as a differentiating solvent toward the two acids by revealing the inherent differences in their acidities.

$$CH_3COOH + HClO_4 \rightleftharpoons CH_3COOH_2^+ + ClO_4^ base_1$$
 $acid_2$
 $acid_1$
 $base_2$

Perchloric acid is, however, about 5000 times stronger than hydrochloric acid in this solvent.

We conclude that:

- anhydrous acetic acid, is a weaker proton acceptor than water,
- ❖neither of HCl and HClO₄ undergoes complete dissociation.
- Instead, equilibria such as the above mentioned are established.

In a differentiating solvent, various acids dissociate to different degrees and have different strengths.

"Only perchloric acid is a strong acid in methanol and ethanol. Therefore, these two alcohols are also differentiating solvents."

CHEMICAL EQUILIBRIUM

Many reactions used in analytical chemistry never result in complete conversion of reactants to products.

They proceed to a state of **chemical equilibrium** in which the ratio of concentrations of reactants and products is **constant**.

Equilibrium- constant expressions:

- describe the concentration relationships among reactants and products at equilibrium.
- permit calculation of the error in an analysis resulting from the quantity of unreacted analyte that remains when equilibrium has been reached.

The Equilibrium State

$$H_3AsO_4 + 3I^- + 2H^+ \rightleftharpoons H_3AsO_3 + I_3^- + H_2O$$

$$H_3AsO_3 + I_3^- + H_2O \rightleftharpoons H_3AsO_4 + 3I^- + 2H^+$$

We can follow the rate of this reaction and the extent to which it proceeds to the right by monitoring the appearance of the **orange-red** color of the triiodide ion I_3 .

A solution of identical color intensity can be produced by using appropriate amount of reactants for both reactions.

The final position of a chemical equilibrium is **independent** of the route to the equilibrium state.

the **concentration relationship** at chemical equilibrium (that is, the position of equilibrium) is independent of the route to the equilibrium state.

This relationship is altered by applying stress to the system.

Such stresses include changes in temperature, in pressure (if one of the reactants or products is a gas), or in total concentration of a reactant or a product.

These effects can be predicted qualitatively from the Le Châtelier's principle.

The mass-action effect is a shift in the position of an equilibrium caused by adding one of the reactants or products to a system.

This principle states that the position of chemical equilibrium always shifts in a direction that tends to relieve the effect of an applied stress.

Equilibrium is a dynamic process.

Although chemical reactions appear to stop at equilibrium, in fact, the amounts of reactants and products are constant because the rates of the forward and reverse processes are exactly the same.

Chemical thermodynamics is a branch of chemistry that concerns the flow of heat and energy in chemical reactions. The position of a chemical equilibrium is related to these energy changes.

Equilibrium-Constant Expressions

$$wW + xX \rightleftharpoons yY + zZ$$

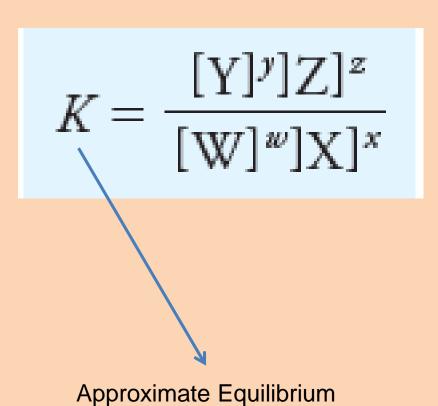
$$K = \frac{[\mathbf{Y}]^y]\mathbf{Z}]^z}{[\mathbf{W}]^w]\mathbf{X}]^x}$$

where the square-bracketed terms are:

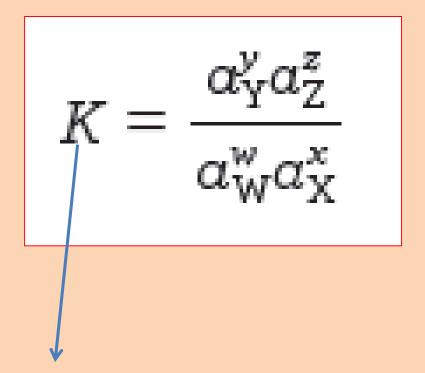
- 1. molar concentrations if they represent dissolved solutes.
- **2. partial pressures in atmospheres** if they are gas-phase reactants or products.

In such an instance, we will often replace the square bracketed terms with the symbol **p**, which stands for the partial pressure of the gases in atmospheres.

If a reactant or product is a **pure liquid**, a **pure solid**, or the **solvent** present in excess, **no term** for this species appears in the equilibrium-constant expression.



constants



Exact Equilibrium constants (thermodynamic)

Types of Equilibrium Constants in Analytical Chemistry

TABLE 9-2

Equilibria and Equilibrium Constants Important in Analytical Chemistry

Equilibria and Equilibrium Constants important in Analytical Chemistry			
Type of Equilibrium	Name and Symbol of Equilibrium-Constant	Typical Example	Equilibrium-Constant Expression
Dissociation of water Heterogeneous equilibrium between a slightly soluble substance and its ions in a saturated solution	Ion-product constant, K_{w} Solubility product, K_{sp}	$2H_2O \rightleftharpoons H_3O^+ + OH^-$ $BaSO_4(s) \rightleftharpoons Ba^{2+} + SO_4^{2-}$	$K_{\rm w} = [{\rm H_3O^+}][{\rm OH^-}]$ $K_{\rm sp} = [{\rm Ba^2}^+][{\rm SO_4}^{2-}]$
Dissociation of a weak acid or base	Dissociation constant, $K_{\rm a}$ or $K_{\rm b}$	$CH_3COOH + H_2O \rightleftharpoons$ $H_3O^+ + CH_3COO^ CH_3COO^- + H_2O \rightleftharpoons$ $OH^- + CH_3COOH$	$K_{\rm a} = {{\rm [H_3O^+][CH_3COO^-]} \over {\rm [CH_3COOH]}}$ $K_{\rm b} = {{\rm [OH^-][CH_3COOH]} \over {\rm [CH_3COO^-]}}$
Formation of a complex ion	Formation constant, β_n	$Ni^{2+} + 4CN^{-} \rightleftharpoons Ni(CN)_4^{2-}$	$ \beta_4 = \frac{[\text{Ni}(\text{CN})_4^{2-}]}{[\text{Ni}^{2+}][\text{CN}^-]^4} $
Oxidation/reduction equilibrium	$K_{ m redox}$	$MnO_4^- + 5Fe^{2+} + 8H^+ \rightleftharpoons Mn^{2+} + 5Fe^{3+} + 4H_2O$	$K_{\text{redox}} = \frac{[\text{Mn}^{2+}][\text{Fe}^{3+}]^5}{[\text{MnO}_4^{-}][\text{Fe}^{2+}]^5[\text{H}^{+}]^8}$
Distribution equilibrium for a solute between immiscible solvents	$K_{ m d}$	$I_2(aq) \rightleftharpoons I_2(org)$	$K_{\mathrm{d}} = \frac{\left[\mathrm{I}_{2}\right]_{\mathrm{org}}}{\left[\mathrm{I}_{2}\right]_{\mathrm{aq}}}$

The formation of Ni(CN)₄²⁻ is typical in that it occurs in steps as shown. **stepwise formation constants are:** K_1 , K_2 , ...

$$Ni^{2+} + CN^{-} \rightleftharpoons Ni(CN)^{+} \qquad K_{1} = \frac{[Ni(CN)^{+}]}{[Ni^{2+}][CN^{-}]}$$

$$Ni(CN)^{+} + CN^{-} \rightleftharpoons Ni(CN)_{2} \qquad K_{2} = \frac{[Ni(CN)_{2}]}{[Ni(CN)^{+}][CN^{-}]}$$

$$Ni(CN)_{2} + CN^{-} \rightleftharpoons Ni(CN)_{3}^{-} \qquad K_{3} = \frac{[Ni(CN)_{3}^{-}]}{[Ni(CN)_{2}][CN^{-}]}$$

$$Ni(CN)_{3}^{-} + CN^{-} \rightleftharpoons Ni(CN)_{4}^{2-} \qquad K_{4} = \frac{[Ni(CN)_{4}^{2-}]}{[Ni(CN)_{3}^{-}][CN^{-}]}$$

Overall constants are designated by the symbol β_n .

$$Ni^{2+} + 2CN^{-} \rightleftharpoons Ni(CN)_{2} \qquad \beta_{2} = K_{1}K_{2} = \frac{[Ni(CN)_{2}]}{[Ni^{2+}][CN^{-}]^{2}}$$

$$Ni^{2+} + 3CN \rightleftharpoons Ni(CN)_{3}^{-} \qquad \beta_{3} = K_{1}K_{2}K_{3} = \frac{[Ni(CN)_{3}^{-}]}{[Ni^{2+}][CN^{-}]^{3}}$$

$$Ni^{2+} + 4CN^{-} \rightleftharpoons Ni(CN)_{4}^{2-} \qquad \beta_{4} = K_{1}K_{2}K_{3}K_{4} = \frac{[Ni(CN)_{4}^{2-}]}{[Ni^{2+}][CN^{-}]^{4}}$$

Applying the Ion-Product Constant for Water

Aqueous solutions contain small concentrations of **hydronium** and **hydroxide ions** as a result of the dissociation reaction.

$$2H_2O \rightleftharpoons H_3O^+ + OH^-$$

$$K[H_2O]^2 = K_w = [H_3O^+][OH^-]$$

ion-product constant for water

$$-\log K_{w} = -\log[H_{3}O^{+}] - \log [OH^{-}]$$

$$p K_w = pH + pOH$$
 At 25°C, $pK_w = 14.00$.

$$K = \frac{[H_3O^+][OH^-]}{[H_2O]^2}$$

TABLE 9-3

Variation of K_w with Temperature

Temperature, °C	$K_{ m w}$
0	0.114×10^{-14}
25	1.01×10^{-14}
50	5.47×10^{-14}
75	19.9×10^{-14}
100	49 $\times 10^{-14}$

Why [H₂O] Does Not Appear in Equilibrium-Constant Expressions for Aqueous Solutions

In a dilute aqueous solution, the molar concentration of water is

$$[H_2O] = \frac{1000 \text{ g-H}_2O}{\text{L H}_2O} \times \frac{1 \text{ mol H}_2O}{18.0 \text{ g-H}_2O} = 55.6 \text{ M}$$

If we have 0.1 mol of HCl in 1 L of water. The presence of this acid will shift the equilibrium to the left.

$$2H_2O \rightleftharpoons H_3O^+ + OH^-$$

Originally, however, there was only 10⁻⁷ mol/L OH⁻ to consume the added protons.

Therefore, even if all the OH⁻ ions are converted to H₂O, the water concentration will increase to only

$$[H_2O] = 55.6 \frac{\text{mol H}_2O}{\text{L H}_2O} + 1 \times 10^{-7} \frac{\text{mol OH}^-}{\text{L H}_2O} \times \frac{1 \text{ mol H}_2O}{\text{mol OH}^-} \approx 55.6 \text{ M}$$

$$\frac{10^{-7} \,\mathrm{M}}{55.6 \,\mathrm{M}} \times 100\% = 2 \times 10^{-7}\%$$

$$K(55.6)^2 = K_w = 1.00 \times 10^{-14} \text{ at } 25^{\circ}\text{C}$$

The ion-product constant for water permits us to easily find the hydronium and hydroxide ion concentrations of aqueous solutions.

Applying the ION-PRODUCT constant for water

Calculate the hydronium and hydroxide ion concentrations of pure water at 25°C and 100°C.

Answers:

At 25°C
$$[H_3O^+] = [OH^-] = 1.00 \times 10^{-7} \text{ M}$$

At 100°C $[H_3O^+] = [OH^-] = 7.00 \times 10^{-7} \text{ M}$

EXAMPLE: Calculate the hydronium and hydroxide ion concentrations and the pH and pOH of 0.013 M aqueous KOH at 25 °C.

EXAMPLE: Calculate the hydronium and hydroxide ion concentrations and the pH and pOH of 1.30×10⁻⁷ M aqueous KOH at 25 °C.

EXAMPLE: Calculate the hydronium and hydroxide ion concentrations and the pH and pOH of 0.023 M aqueous HNO₃ at 25 °C.

EXAMPLE: Calculate the hydronium and hydroxide ion concentrations and the pH and pOH of 2.30×10⁻⁷ M aqueous HNO₃ at 25 °C.

USING ACID/BASE DISSOCIATION CONSTANTS

1. Dissociation Constants for Conjugate Acid/Base Pairs

2. Hydronium Ion Concentration of Solutions of Weak Acids

3. Hydronium Ion Concentration of Solutions of Weak Bases

Using Solubility-Product Constants

1. The Solubility of a Precipitate in Pure Water

2.The Effect of a Common Ion on the Solubility of a Precipitate