## CHAPTER 4

## EFFECT OF ELECTROLYTES ON CHEMICAL EQUILIBRIUM :

EFFECT OF ELECTROLYTES ON IONIC EQUILIBRIUM, THERMODYNAMIC AND CONCENTRATION EQUILIBRIUM CONSTANTS, ACTIVITY AND ACTIVITY COEFFICIENTS

## In this chapter,

*chemical equilibrium including calculations of chemical composition and of equilibrium concentrations for monoprotic acid/base systems will be considered.

* buffer solutions, which are extremely important in many areas of science, and describe the properties of these solutions will be discussed.


## THE CHEMICAL COMPOSITION OF AQUEOUS SOLUTIONS

Electrolytes form ions when dissolved in water (or certain other solvents) and thus produce solutions that conduct electricity.

Strong electrolytes ionize essentially completely in a solvent, Weak electrolytes ionize only partially.

Conducting electricity by weak electrolytes <<< strong electrolyte

## TABLE 9-1

Classification of Electrolytes

| Strong | Weak |
| :--- | :--- |
| 1. Inorganic acids such as $\mathrm{HNO}_{3}, \mathrm{HClO}_{4}$, | 1. Many inorganic acids, including $\mathrm{H}_{2} \mathrm{CO}_{3}$, |
| $\mathrm{H}_{2} \mathrm{SO}_{4}{ }^{*}, \mathrm{HCl}, \mathrm{HI}, \mathrm{HBr}, \mathrm{HClO}_{3}, \mathrm{HBrO}_{3}$ | $\mathrm{H}_{3} \mathrm{BO}_{3}, \mathrm{H}_{3} \mathrm{PO}_{4}, \mathrm{H}_{2} \mathrm{~S}, \mathrm{H}_{2} \mathrm{SO}_{3}$ |
| 2. Alkali and alkaline-earth hydroxides | 2. Most organic acids |
| 3. Most salts | 3. Ammonia and most organic bases |
|  | 4. Halides, cyanides, and thiocyanates of |
|  | $\mathrm{Hg}, \mathrm{Zn}$, and Cd |

* $\mathrm{H}_{2} \mathrm{SO}_{4}$ is completely dissociated into $\mathrm{HSO}_{4}{ }^{2-}$ and $\mathrm{H}_{3} \mathrm{O}^{+}$ions and for this reason is classified as a strong electrolyte.
$\mathrm{HSO}_{4}{ }^{2-}$ ion is a weak electrolyte and is only partially dissociated into $\mathrm{SO}_{4}{ }^{2-}$ and $\mathrm{H}_{3} \mathrm{O}^{+}$.


## Brønsted-Lowry Theory

An acid donates protons.
only in the presence of a proton acceptor (base).

A base is a proton acceptor.
only in the presence of a proton donor (acid).

A salt is produced in the reaction of an acid with a base. $\mathrm{NaCl}, \mathrm{Na}_{2} \mathrm{SO}_{4}, \mathrm{NaOOCCH}_{3}$

## Arrhenius acid-base definition

 (acid produces $\mathrm{H}_{3} \mathrm{O}^{+}$and base forms $\mathrm{OH}^{-}$in water.)Lewis acid-base definition
(acid accepts and shares electron and bases share their electrons)

A conjugate base is formed when an acid loses a proton.

$\mathrm{H}_{2} \mathrm{O}+\mathrm{HNO}_{2} \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{NO}_{2}^{-}$conjugate acid/base pair

A conjugate acid is formed when an base gains a proton.


conjugate acid/base pair base $_{2} /$ acid $_{2}$

A substance acts as an acid only in the presence of a base and vice versa.

Neutralization: acid $_{1}+$ base $_{2} \rightleftharpoons$ base $_{1}+$ acid $_{2}$
$\mathrm{HNO}_{2}+\mathrm{NH}_{3} \Leftrightarrow \mathrm{NH}_{4}{ }^{+}+\mathrm{NO}_{2}{ }^{-}$
$\mathrm{NO}_{2}^{-}+\mathrm{H}_{2} \mathrm{O} \Leftrightarrow \mathrm{HNO}_{2}+\mathrm{OH}^{-}$
base $_{1} \quad$ acid $_{2}$ conjugate conjugate acid $_{1} \quad$ base $_{2}$
$\mathrm{NH}_{4}^{+}+\mathrm{H}_{2} \mathrm{O} \Leftrightarrow \mathrm{NH}_{3}+\mathrm{H}_{3} \mathrm{O}^{+}$
acid $_{1} \quad$ base $_{2} \quad$ conjugate conjugate base $_{1} \quad$ acid $_{2}$

## Amphiprotic Species

Species that have both acidic and basic properties are amphiprotic.

* behaves as a base in the presence of a proton donor.

$$
\underset{\text { base }_{1}}{\mathrm{H}_{2} \mathrm{PO}_{4}^{-}}+\underset{\text { acid }}{2}+\underset{\text { acid }_{1}}{\mathrm{H}_{3} \mathrm{O}^{+}} \rightleftharpoons \underset{\text { base }_{2}}{\mathrm{H}_{3} \mathrm{PO}_{4}}+\underset{\mathrm{b}_{2} \mathrm{O}}{\mathrm{H}_{2}}
$$

* behaves as an acid in the presence of a proton acceptor.

$$
\underset{\text { acid }_{1}}{\mathrm{H}_{2} \mathrm{PO}_{4}^{-}}+\underset{\text { base }}{2}-\mathrm{OH}^{-} \rightleftharpoons \underset{\text { base }}{1} \text { } \mathrm{HPO}_{4}^{2-}+\underset{\text { acid }}{2}
$$

Water acts as a proton acceptor (base) and as a proton donor (acid): Amphiprotic solvent

The simple amino acids are an important class of amphiprotic compounds that contain both a weak acid and a weak base functional group.
an amino acid, undergoes a kind of internal acid/base reaction to produce a zwitterion-a species that has both a positive and a negative charge.

## $\mathrm{NH}_{2} \mathrm{CH}_{2} \mathrm{COOH} \rightleftharpoons \mathrm{NH}_{3}{ }^{+} \mathrm{CH}_{2} \mathrm{COO}^{-}$ glycine <br> zwitterion

acid/base reaction between a carboxylic acid and an amine


Water acts as a proton acceptor (base) and as a proton donor (acid): Amphiprotic solvent

Other common amphiprotic solvents are methanol, ethanol, and anhydrous acetic acid.


## Autoprotolysis (autoionization)

Amphiprotic solvents undergo self-ionization, or autoprotolysis, to form a pair of ionic species.


Water slightly undergoes autoprotolysis at room temperature. Thus, the hydronium $\left(\mathrm{H}_{3} \mathrm{O}^{+}\right)$and hydroxide ion $\left(\mathrm{OH}^{-}\right)$concentrations in pure water are only about $10^{-7} \mathrm{M}$.

## Strengths of Acids and Bases

strong acids: reaction with the solvent is sufficiently complete that no undissociated solute molecules are left in aqueous solution.
weak acids: react incompletely with water to give solutions containing significant quantities of both the parent acid and its conjugate base.

Note that acids can be cationic, anionic, or electrically neutral.
The same holds for bases.

The common strong acids include $\mathrm{HCl}, \mathrm{HBr}, \mathrm{HI}, \mathrm{HClO}_{4}$, $\mathrm{HNO}_{3}$, the first proton in $\mathrm{H}_{2} \mathrm{SO}_{4}$, and the organic sulfonic acid $\mathrm{RSO}_{3} \mathrm{H}$.

The common strong bases include $\mathrm{NaOH}, \mathrm{KOH}, \mathrm{Ba}(\mathrm{OH})_{2}$, and the quaternary ammonium hydroxide $\mathrm{R}_{4} \mathrm{NOH}$, where R is an alkyl group such as $\mathrm{CH}_{3}$ or $\mathrm{C}_{2} \mathrm{H}_{5}$.

Conjugate acids/bases of strong acids/bases do not undergo a hydrolysis reaction. They are not strong enough to produce hydronium $\left(\mathrm{H}_{3} \mathrm{O}^{+}\right)$and hydroxide ion $\left(\mathrm{OH}^{-}\right)$.

Conjugate acids/bases of weak acids are strong enough to undergo a hydrolysis reaction. They are produce hydronium $\left(\mathrm{H}_{3} \mathrm{O}^{+}\right)$or hydroxide ion $\left(\mathrm{OH}^{-}\right)$and change the pH of the solution.

Note that acids can be cationic, anionic, or electrically neutral.
The same holds for bases.

The tendency of a solvent to accept or donate protons determines the strength of a solute acid or base dissolved in it.

Water, is a leveling solvent for perchloric, hydrochloric, and nitric acids because all three are completely ionized in this solvent and show no differences in strength.

Strongest acid


$$
\begin{aligned}
\mathrm{HClO}_{4}+\mathrm{H}_{2} \mathrm{O} & \rightarrow \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{ClO}_{4}^{-} \\
\mathrm{HCl}+\mathrm{H}_{2} \mathrm{O} & \rightarrow \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{Cl}^{-} \\
\mathrm{H}_{3} \mathrm{PO}_{4}+\mathrm{H}_{2} \mathrm{O} & \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{H}_{2} \mathrm{PO}_{4}^{-} \\
\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}^{3+}+\mathrm{H}_{2} \mathrm{O} & \left.\rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{AlOH}_{2} \mathrm{H}_{2} \mathrm{O}\right)_{5}^{2+} \\
\mathrm{CC}_{2} \mathrm{H}_{3} \mathrm{O}_{2}+\mathrm{H}_{2} \mathrm{O} & \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}^{-} \\
\mathrm{H}_{2} \mathrm{PO}_{4}^{-}+\mathrm{H}_{2} \mathrm{O} & \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{HPO}_{3}^{2-} \\
\mathrm{NH}_{4}{ }^{+}+\mathrm{H}_{3} \mathrm{O} & \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{NH}_{3}
\end{aligned}
$$

In a leveling solvent, several acids are completely dissociated and show the same strength.

Anhydrous acetic acid acts as a differentiating solvent toward the two acids by revealing the inherent differences in their acidities.

$$
\underset{3}{\mathrm{CH}_{3} \mathrm{COOOH}}+\underset{\text { acid }_{2}}{\mathrm{HClO}_{4}} \rightleftharpoons \underset{3}{\mathrm{CH}_{3} \mathrm{COOH}_{2}^{+}}+\underset{\text { acid }_{1}}{\mathrm{ClO}_{2}}{ }_{4}^{-}
$$

Perchloric acid is, however, about 5000 times stronger than hydrochloric acid in this solvent.

We conclude that :

* anhydrous acetic acid, is a weaker proton acceptor than water, neither of HCl and $\mathrm{HClO}_{4}$ undergoes complete dissociation.
* Instead, equilibria such as the above mentioned are established.

In a differentiating solvent, various acids dissociate to different degrees and have different strengths.
"Only perchloric acid is a strong acid in methanol and ethanol. Therefore, these two alcohols are also differentiating solvents."

## CHEMICAL EQUILIBRIUM

Many reactions used in analytical chemistry never result in complete conversion of reactants to products.

They proceed to a state of chemical equilibrium in which the ratio of concentrations of reactants and products is constant.

## Equilibrium- constant expressions:

* describe the concentration relationships among reactants and products at equilibrium.
* permit calculation of the error in an analysis resulting from the quantity of unreacted analyte that remains when equilibrium has been reached.


## The Equilibrium State

$$
\mathrm{H}_{3} \mathrm{AsO}_{4}+3 \mathrm{I}^{-}+2 \mathrm{H}^{+} \rightleftharpoons \mathrm{H}_{3} \mathrm{AsO}_{3}+\mathrm{I}_{3}^{-}+\mathrm{H}_{2} \mathrm{O}
$$

$$
\mathrm{H}_{3} \mathrm{AsO}_{3}+\mathrm{I}_{3}^{-}+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{H}_{3} \mathrm{AsO}_{4}+3 \mathrm{I}^{-}+2 \mathrm{H}^{+}
$$

We can follow the rate of this reaction and the extent to which it proceeds to the right by monitoring the appearance of the orange-red color of the triiodide ion $\mathrm{I}_{3}{ }^{-}$.

A solution of identical color intensity can be produced by using appropriate amount of reactants for both reactions.

The final position of a chemical equilibrium is independent of the route to the equilibrium state.
the concentration relationship at chemical equilibrium (that is, the position of equilibrium) is independent of the route to the equilibrium state.

This relationship is altered by applying stress to the system.
Such stresses include changes in temperature, in pressure (if one of the reactants or products is a gas), or in total concentration of a reactant or a product.

These effects can be predicted qualitatively from the Le Châtelier's principle.

The mass-action effect is a shift in the position of an equilibrium caused by adding one of the reactants or products to a system.

This principle states that the position of chemical equilibrium always shifts in a direction that tends to relieve the effect of an applied stress.

## Equilibrium is a dynamic process.

Although chemical reactions appear to stop at equilibrium, in fact, the amounts of reactants and products are constant because the rates of the forward and reverse processes are exactly the same.

Chemical thermodynamics is a branch of chemistry that concerns the flow of heat and energy in chemical reactions. The position of a chemical equilibrium is related to these energy changes.

## Equilibrium-Constant Expressions

$$
w \mathrm{~W}+x \mathrm{X} \rightleftharpoons y \mathrm{Y}+z \mathrm{Z} \quad K=\frac{\left.\left.[\mathrm{Y}]^{y}\right] \mathrm{Z}\right]^{z}}{\left.\left.[\mathrm{~W}]^{w}\right] \mathrm{X}\right]^{x}}
$$

where the square-bracketed terms are:

1. molar concentrations if they represent dissolved solutes.
2. partial pressures in atmospheres if they are gas-phase reactants or products.

In such an instance, we will often replace the square bracketed terms with the symbol $p$, which stands for the partial pressure of the gases in atmospheres.

If a reactant or product is a pure liquid, a pure solid, or the solvent present in excess, no term for this species appears in the equilibriumconstant expression.


Approximate Equilibrium constants


Exact Equilibrium
constants
(thermodynamic)

## Types of Equilibrium Constants in Analytical Chemistry

## TABLE 9-2

## Equilibria and Equilibrium Constants Important in Analytical Chemistry

| Type of Equilibrium | Name and Symbol of <br> Equilibrium-Constant | Typical Example |
| :--- | :--- | :--- |

The formation of $\mathrm{Ni}(\mathrm{CN})_{4}{ }^{2-}$ is typical in that it occurs in steps as shown. stepwise formation constants are: $K_{1}, K_{2}, \ldots$

$$
\begin{aligned}
\mathrm{Ni}^{2+}+\mathrm{CN}^{-} \rightleftharpoons \mathrm{Ni}(\mathrm{CN})^{+} & K_{1}=\frac{\left[\mathrm{Ni}(\mathrm{CN})^{+}\right]}{\left[\mathrm{Ni}^{2+}\right]\left[\mathrm{CN}^{-}\right]} \\
\mathrm{Ni}(\mathrm{CN})^{+}+\mathrm{CN}^{-} \rightleftharpoons \mathrm{Ni}(\mathrm{CN})_{2} & K_{2}=\frac{\left[\mathrm{Ni}(\mathrm{CN})_{2}\right]}{\left[\mathrm{Ni}(\mathrm{CN})^{+}\right]\left[\mathrm{CN}^{-}\right]} \\
\mathrm{Ni}(\mathrm{CN})_{2}+\mathrm{CN}^{-} \rightleftharpoons \mathrm{Ni}(\mathrm{CN})_{3}^{-} & K_{3}=\frac{\left[\mathrm{Ni}(\mathrm{CN})_{3}{ }^{-}\right]}{\left[\mathrm{Ni}(\mathrm{CN})_{2}\right]\left[\mathrm{CN}^{-}\right]} \\
\mathrm{Ni}(\mathrm{CN})_{3}^{-}+\mathrm{CN}^{-} \rightleftharpoons \mathrm{Ni}(\mathrm{CN})_{4}^{2-} & K_{4}=\frac{\left[\mathrm{Ni}(\mathrm{CN})_{4}^{2-}\right]}{\left[\mathrm{Ni}(\mathrm{CN})_{3}{ }^{2-}\right]\left[\mathrm{CN}^{-}\right]}
\end{aligned}
$$

Overall constants are designated by the symbol $\beta_{n}$.

$$
\begin{array}{ll}
\mathrm{Ni}^{2+}+2 \mathrm{CN}^{-} \rightleftharpoons \mathrm{Ni}(\mathrm{CN})_{2} & \beta_{2}=K_{1} K_{2}=\frac{\left[\mathrm{Ni}(\mathrm{CN})_{2}\right]}{\left[\mathrm{Ni}^{2+}\right]\left[\mathrm{CN}^{-}\right]^{2}} \\
\mathrm{Ni}^{2+}+3 \mathrm{CN} \rightleftharpoons \mathrm{Ni}(\mathrm{CN})_{3}{ }^{-} & \beta_{3}=K_{1} K_{2} K_{3}=\frac{\left[\mathrm{Ni}(\mathrm{CN})_{3}{ }^{-}\right]}{\left[\mathrm{Ni}^{2+}\right]\left[\mathrm{CN}^{-}\right]^{3}} \\
\mathrm{Ni}^{2+}+4 \mathrm{CN}^{-} \rightleftharpoons \mathrm{Ni}(\mathrm{CN})_{4}{ }^{2-} & \beta_{4}=K_{1} K_{2} K_{3} K_{4}=\frac{\left[\mathrm{Ni}(\mathrm{CN})_{4}{ }^{2-}\right]}{\left[\mathrm{Ni}^{2+}\right]\left[\mathrm{CN}^{-}\right]^{4}}
\end{array}
$$

## Applying the Ion-Product Constant for Water

Aqueous solutions contain small concentrations of hydronium and hydroxide ions as a result of the dissociation reaction.

$$
\begin{aligned}
& 2 \mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{OH}^{-} \quad K=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{OH}^{-}\right]}{\left[\mathrm{H}_{2} \mathrm{O}\right]^{2}} \\
& K\left[\mathrm{H}_{2} \mathrm{O}\right]^{2}=K_{\mathrm{w}}=\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{OH}^{-}\right]
\end{aligned}
$$

ion-product constant for water

## TABLE 9-3

## Variation of $K_{w}$ with Temperature

$$
\begin{aligned}
& -\log K_{w}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right]-\log \left[\mathrm{OH}^{-}\right] \\
& p K_{w}=p H+p O H \quad \text { At } 25^{\circ} \mathrm{C}, \mathrm{p} K_{\mathrm{w}}=14.00
\end{aligned}
$$

| Temperature, ${ }^{\circ} \mathrm{C}$ | $K_{\mathrm{w}}$ |
| :---: | :--- |
| 0 | $0.114 \times 10^{-14}$ |
| 25 | $1.01 \times 10^{-14}$ |
| 50 | $5.47 \times 10^{-14}$ |
| 75 | $19.9 \times 10^{-14}$ |
| 100 | 49 |$\times 10^{-14}$.

## Why [ $\mathrm{H}_{2} \mathrm{O}$ ] Does Not Appear in Equilibrium-Constant Expressions for Aqueous Solutions

In a dilute aqueous solution, the molar concentration of water is

$$
\left[\mathrm{H}_{2} \mathrm{O}\right]=\frac{1000 \mathrm{~g} \mathrm{H}_{2} \mathrm{O}}{\mathrm{~L} \mathrm{H}_{2} \mathrm{O}} \times \frac{1 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}}{18.0 \mathrm{gH}_{2} \mathrm{O}}=55.6 \mathrm{M}
$$

If we have 0.1 mol of HCl in 1 L of water. The presence of this acid will shift the equilibrium to the left.

$$
2 \mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{OH}^{-}
$$

Originally, however, there was only $10^{-7} \mathrm{~mol} / \mathrm{L} \mathrm{OH}^{-}$to consume the added protons.
Therefore, even if all the $\mathrm{OH}^{-}$ions are converted to $\mathrm{H}_{2} \mathrm{O}$, the water concentration will increase to only

$$
\left[\mathrm{H}_{2} \mathrm{O}\right]=55.6 \frac{\mathrm{~mol} \mathrm{H}_{2} \mathrm{O}}{\mathrm{~L} \mathrm{H}_{2} \mathrm{O}}+1 \times 10^{-7} \frac{\mathrm{~mol} \mathrm{OH}^{-}}{\mathrm{L} \mathrm{H}_{2} \mathrm{O}} \times \frac{1 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}}{\mathrm{~mol} \mathrm{OH}^{-}} \approx 55.6 \mathrm{M}
$$

$$
\begin{aligned}
& \frac{10^{-7} \mathrm{M}}{55.6 \mathrm{M}} \times 100 \%=2 \times 10^{-7} \% \\
& K(55.6)^{2}=K_{\mathrm{w}}=1.00 \times 10^{-14} \text { at } 25^{\circ} \mathrm{C}
\end{aligned}
$$

The percent change in water concentration is insignificant.

The ion-product constant for water permits us to easily find the hydronium and hydroxide ion concentrations of aqueous solutions.

## Applying the ION-PRODUCT constant for water

Calculate the hydronium and hydroxide ion concentrations of pure water at $25^{\circ} \mathrm{C}$ and $100^{\circ} \mathrm{C}$.

Answers:
At $25^{\circ} \mathrm{C}$
$\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\left[\mathrm{OH}^{-}\right]=1.00 \times 10^{-7} \mathrm{M}$
At $100^{\circ} \mathrm{C}$
$\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\left[\mathrm{OH}^{-}\right]=7.00 \times 10^{-7} \mathrm{M}$

EXAMPLE: Calculate the hydronium and hydroxide ion concentrations and the pH and pOH o 0.013 M aqueous $\mathrm{KOH} 2 \mathrm{t} 25^{\circ} \mathrm{C}$.

EXAMPLE: Calculate the hydronium and hydroxide ion concentrations and the pH and pOH of $\subset .30 \times 10^{-7} \mathrm{M}$ aqueous KOH an $25^{\circ} \mathrm{C}$.

EXAMPLE: Calculate the hydronium and hydroxide ion concentrations and the pH and pOH o 0.023 M aqueous $\mathrm{HNO}_{3}$ at $25^{\circ} \mathrm{C}$.

EXAMPLE: Calculate the hydronium and hydroxide ion concentrations and the pH and pOH o $2.30 \times 10^{-7} \mathrm{M}$ aqueous $\mathrm{HNO}_{3}$ at $25^{\circ} \mathrm{C}$.

## USING ACID/BASE DISSOCIATION CONSTANTS

1. Dissociation Constants for Conjugate Acid/Base Pairs

## 2. Hydronium Ion Concentration of Solutions of Weak Acids

3. Hydronium Ion Concentration of Solutions of Weak Bases

## Using Solubility-Product Constants

1. The Solubility of a Precipitate in Pure Water
2.The Effect of a Common Ion on the Solubility of a Precipitate
