EEE328 Digital Signal Processing

Ankara University

Faculty of Engineering

Electrical and Electronics Engineering Department

Sampling and Reconstruction of Continuous-Time Signals

EEE328 Digital Signal Processing Lecture 10

Agenda

- Sampling
- Recovery of Continuous-Time Signal from Its Samples

Recovery of Continuous-Time Signal from Its Samples Using an Ideal Low-Pass Filter



Recovery of Continuous-Time Signal from Its Samples Using an Ideal Low-Pass Filter $X_c(j\Omega)$ $-\Omega_N$ Ω_N Ω $X_s(j\Omega)$ 1 \boldsymbol{T} • • • $2\Omega_s$ Ω $-2\Omega_s$ $-\Omega_s$ Ω_N $-\Omega_N$ 0 Ω_s $\Omega_s - \Omega_N$ $X_r(j\Omega)$ $H_r(j\Omega)$ $\Omega_N < \Omega_c < \Omega_s - \Omega_N$ Ω $-\Omega_N$ Ω $-\Omega_c$ Ω_c Ω_N

Ankara University Electrical and Electronics Eng. Dept. EEE328

$$x_{s}(t) = \sum_{n=-\infty}^{\infty} x[n]\delta(t - nT)$$
$$x_{r}(t) = \sum_{n=-\infty}^{\infty} x[n]h_{r}(t - nT)$$
$$h_{r}(t) = \frac{\sin(\frac{\pi t}{T})}{\pi t/T}$$
$$x_{r}(t) = \sum_{n=-\infty}^{\infty} x[n]\frac{\sin(\frac{\pi (t - nT)}{T})}{\pi (t - nT)/T}$$

 $n = -\infty$









Ideal Bandlimited Interpolation



$$X_r(j\Omega) = \frac{1}{T} \sum_{n=-\infty}^{\infty} x[n] H_r(j\Omega) e^{-j\Omega T n}$$

 $X_r(j\Omega) = H_r(j\Omega)X(e^{j\Omega T})$

References

- Signals & Systems, Second Edition, A. V. Oppenheim, A. S. Willsky with S. H. Nawab, Prentice Hall, 1997
- Discrete-Time Signal Processing, Second Edition, A. V. Oppenheim, R. W. Schafer with J. R. Buck, Prentice Hall, 1999