EEE104 Circuit Analysis I

Ankara University

Faculty of Engineering

Electrical and Electronics Engineering Department

Ankara University Electrical and Electronics Eng. Dept. EEE104

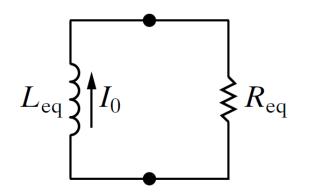
Response of First Order RL Circuits

EEE104 Circuit Analysis I

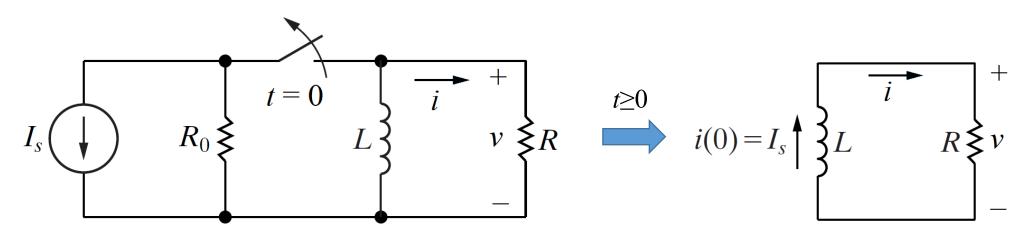
Lecture 10

Agenda

- Natural Response of an RL Circuit
- Natural Response of an RC Circuit



Natural Response Form of RL Circuit



A circuit for RL circuit natural response

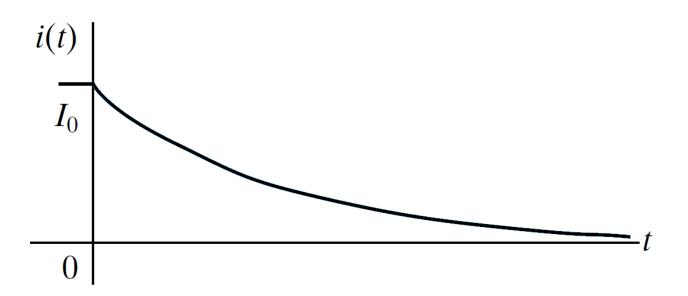
$$i(0^{-}) = i(0^{+}) = I_{0}$$

$$i(t) = I_{0}e^{-\left(\frac{R}{L}\right)t}, t \ge 0 \qquad \tau = \frac{L}{R} \rightarrow i(t) = I_{0}e^{-\frac{t}{\tau}}, t \ge 0$$

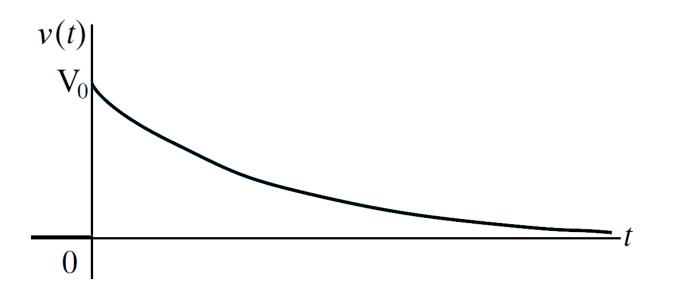
$$v(t) = i(t)R = I_{0}Re^{-\left(\frac{R}{L}\right)t}, t \ge 0^{+} \qquad v(t) = V_{0}e^{-\frac{t}{\tau}}, t \ge 0^{+}$$

$$v(0^{-}) = 0$$

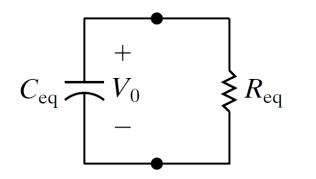
$$v(0^{+}) = I_{0}R = V_{0}$$



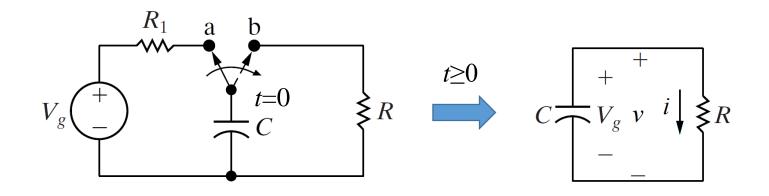
Natural current response of RL circuit



Natural voltage response of RL circuit



Natural Response Form of RC Circuit



A circuit for RL circuit natural response

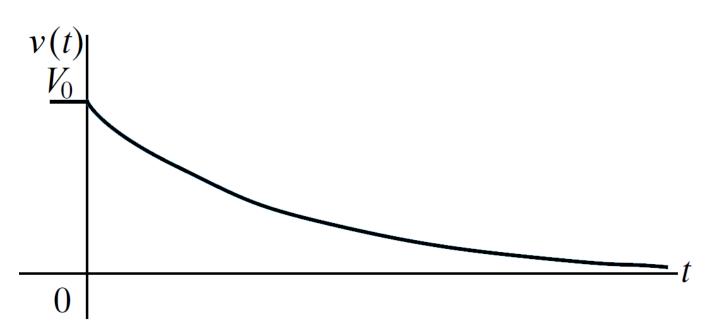
$$v(0^{-}) = v(0^{+}) = V_{0}$$

$$v(t) = V_{0}e^{-\frac{t}{RC}}, t \ge 0 \qquad \tau = RC \quad \rightarrow v(t) = V_{0}e^{-\frac{t}{\tau}}, t \ge 0$$

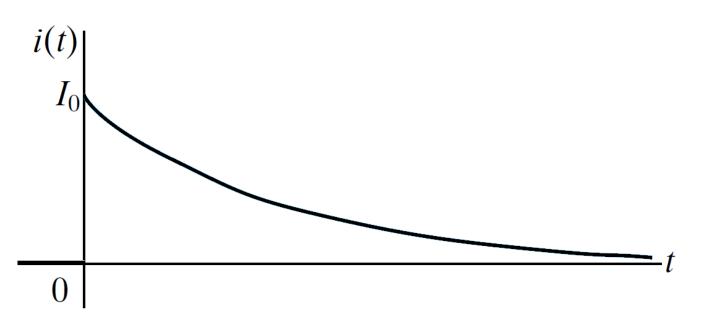
$$i(t) = \frac{v(t)}{R} = \frac{V_{0}}{R}e^{-\frac{t}{RC}}, t \ge 0^{+} \qquad i(t) = I_{0}e^{-\frac{t}{\tau}}, t \ge 0^{+}$$

$$i(0^{-}) = 0$$

$$i(0^{+}) = \frac{V_{0}}{R} = I_{0}$$



Natural voltage response of RC circuit



Natural current response of RC circuit

Reference

 Electric Circuits, Tenth Edition, James W. Nilsson, Susan A. Riedel Pearson, 2015