

EEE201

Circuit Analysis II

Ankara University

Faculty of Engineering

Electrical and Electronics Engineering Department

Introduction to the Laplace Transform

EEE201 Circuit Analysis II

Lecture 10

Agenda

- Inverse Transforms
- Poles and Zeros of $F(s)$
- Initial and Final Value Theorems

Inverse Transforms

$$F(s) = \frac{N(s)}{D(s)} = \frac{a_n s^n + a_{n-1} s^{n-1} + \dots + a_1 s + a_0}{b_m s^m + b_{m-1} s^{m-1} + \dots + b_1 s + b_0}$$

$m > n \Rightarrow$ *proper rational function*

$m \leq n \Rightarrow$ *improper rational function*

Poles and Zeros of $F(s)$

$$F(s) = \frac{K(s + z_1)(s + z_2) \dots (s + z_n)}{(s + p_1)(s + p_2) \dots (s + p_m)}$$

K is the constant a_n/b_m .

$-z_1, -z_2, -z_3, \dots$ are the zeros of $F(s)$.

$-p_1, -p_2, -p_3, \dots$ are the poles of $F(s)$.

Initial and Final Value Theorems

Initial value theorem:

$$\lim_{t \rightarrow 0} f(t) = \lim_{s \rightarrow \infty} sF(s)$$

Final value theorem:

$$\lim_{t \rightarrow \infty} f(t) = \lim_{s \rightarrow 0} sF(s)$$

Reference

- Electric Circuits, Tenth Edition, James W. Nilsson, Susan A. Riedel
Pearson, 2015