## Lecture 14 : Dirac Equation -3

**Examples for the scattering processes :** See the D.Griffiths textbook "Int.Elementary Particles J.Wiley) for all the calculational details.

1. Electron-muon scattering  $e^- + \mu^- \rightarrow e^- + \mu^-$ 





Feynman diagram for the process  $e^- + \mu^- \rightarrow e^- + \mu^-$ 

Twisted Feynman diagram

**2.** Compton scattering  $e^- + \gamma \rightarrow e^- + \gamma$ 

Tree level diagrams



**3.** Casimir trick : To do the sum over the spins using completeness relations and trace techniques.

## 4. Trace techniques :

$$Tr(A + B) = Tr(A) + Tr(B)$$

$$Tr(\alpha A) = \alpha Tr(A)$$

$$Tr(AB) = Tr(BA)$$

$$g_{\mu\nu}g^{\mu\nu} = 4$$

$$\gamma^{\mu}\gamma^{\nu} + \gamma^{\nu}\gamma^{\mu} = 2g^{\mu\nu}$$

$$\gamma^{\mu}\gamma^{\nu} + \gamma^{\nu}\gamma^{\mu} = 4g^{\nu\lambda}$$

$$\gamma_{\mu}\gamma^{\nu}\gamma^{\lambda}\gamma^{\sigma}\gamma^{\mu} = -2\gamma^{\sigma}\gamma^{\lambda}\gamma^{\nu}$$

$$Tr(\gamma^{\mu}\gamma^{\nu}\gamma^{\lambda}\gamma^{\sigma}) = 4(g^{\mu\nu}g^{\lambda\sigma} - g^{\mu\lambda}g^{\nu\sigma} + g^{\mu\sigma}g^{\nu\lambda})$$

$$Tr(\gamma^{5}\gamma^{\mu}\gamma^{\nu}\gamma^{\lambda}\gamma^{\sigma}) = 4i\epsilon^{\mu\nu\lambda\sigma}$$

Trace of a product of odd number of the gamma matrices is zero.

## 5. Cross sections and lifetimes

- Rutherford scattering
- Pair annihilation

## 6. Renormalization concept

Example : Vacuum polarization diagram ( a fourth order correction)



For all the details of the calculations and interpretaion of the results see the textbook by D.Griffiths' "Intr. to Elementary Particles, J.Wiley"

**Study Exercise 1** : Work out in detail the Examples 7.7 and 7.8 from the textbook "Introduction to Elementary Particles by D.Griffiths J.Wiley Pub."

**Homework Problems :** Solve the following problems from the textbook by D.Griffiths' "Intr. to Elementary Particles, J.Wiley"

- a) Problem 7.12
- **b)** Problem 7.13
- c) Problem 7.14
- **d)** Problem 7.15
- **e)** Problem 7.16
- **f)** Problem 7.16
- **g)** Problem 7.17