



BME 202 Electronics

Lecture 7: BJT – AC Analysis

Outline



- Different models for the BJT transistors
- Equivalent models to find the ac parameters for an amplifier
- Effects of source resistance and load resistor on the overall gain and characteristics of an amplifier
- General ac characteristics of important BJT configurations

BJT Transistor Modelling

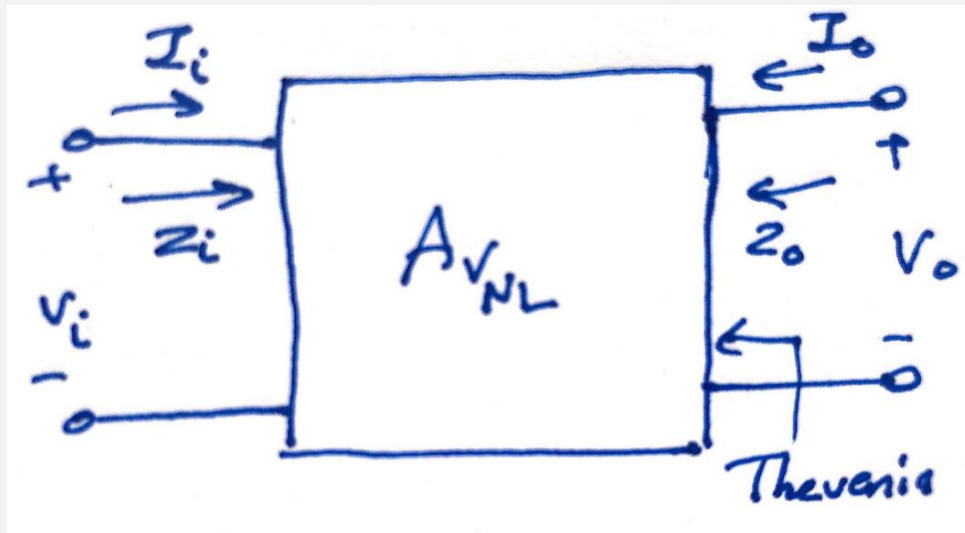
A model is an **equivalent circuit** that represents the AC characteristics of the transistor.

A model uses circuit elements that **approximate** the behavior of the transistor.

There are two models commonly used in **small signal AC analysis** of a transistor:

- r_e model
- Hybrid equivalent model

Two-Port Systems Approach



With V_i set to 0 V:

$$Z_{Th} = Z_o = R_o$$

The voltage across the open terminals is:

$$E_{Th} = A_{V_{NL}} V_i$$

where $A_{V_{NL}}$ is the no-load voltage gain

The r_e Transistor Model

BJTs are basically **current-controlled devices**; therefore the r_e model uses **a diode and a current source** to duplicate the behavior of the transistor.

One **disadvantage** to this model is its **sensitivity to the DC level**. This model is designed for specific circuit conditions.

Common-Base Configuration

Input impedance:

$$r_e = \frac{26 \text{ mV}}{I_e} \quad Z_i = r_e$$

Output impedance:

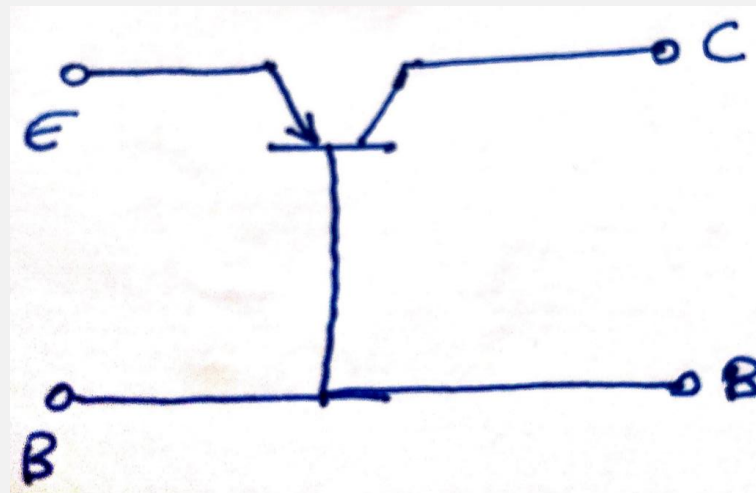
$$Z_o \cong \infty \Omega$$

Voltage gain:

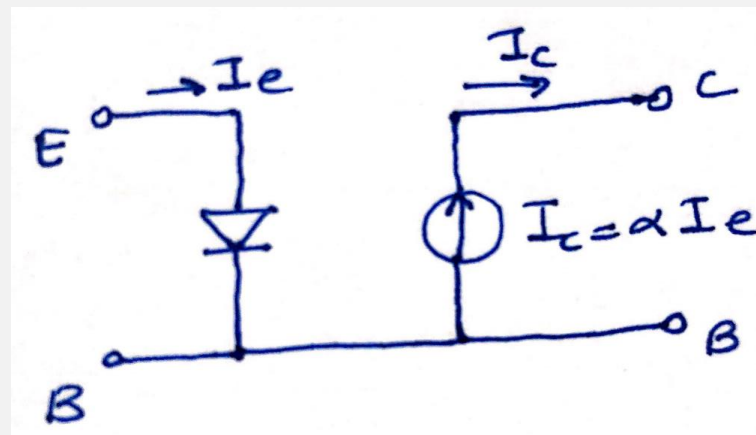
$$A_V = \frac{\alpha R_L}{r_e} \cong \frac{R_L}{r_e}$$

Current gain:

$$A_i = -\alpha \cong -1$$



PNP



Common-Base Configuration

Input impedance:

$$r_e = \frac{26 \text{ mV}}{I_e} \quad Z_i = r_e$$

Output impedance:

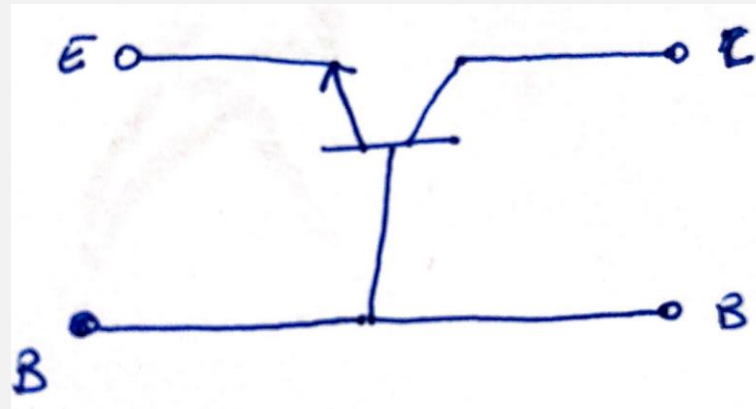
$$Z_o \cong \infty \Omega$$

Voltage gain:

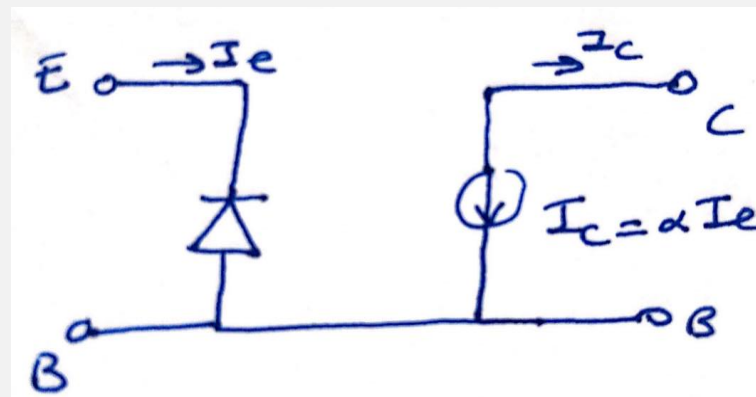
$$A_v = \frac{\alpha R_L}{r_e} \cong \frac{R_L}{r_e}$$

Current gain:

$$A_i = -\alpha \cong -1$$



NPN

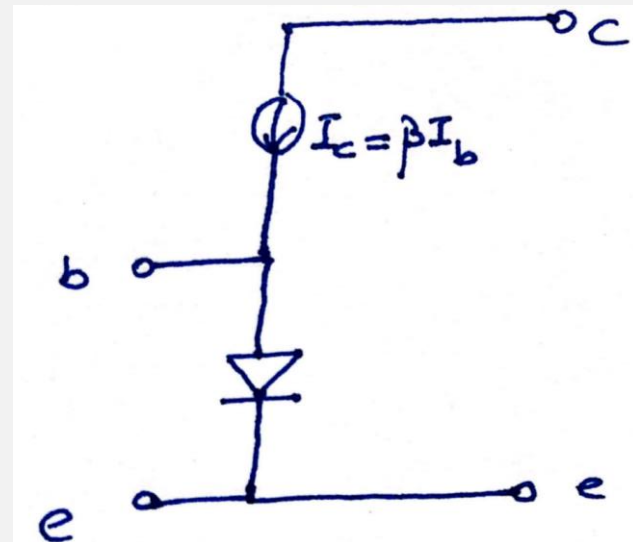
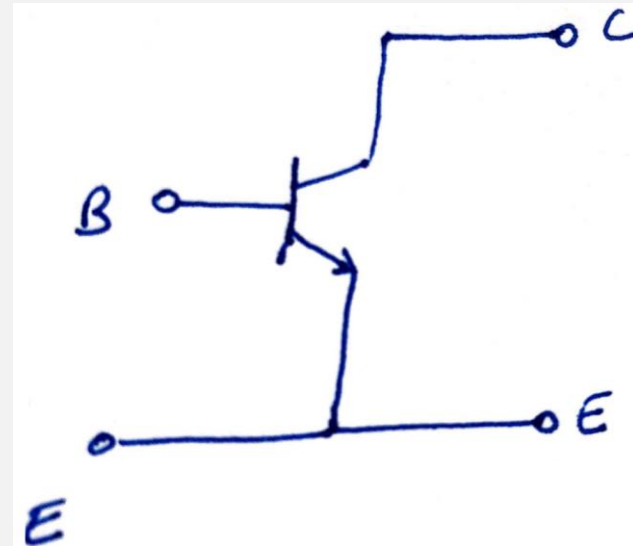


Common-Emitter Configuration

The diode r_e model can be replaced by the resistor r_e .

$$I_e = (\beta + 1)I_b \cong \beta I_b$$

$$r_e = \frac{26 \text{ mV}}{I_e}$$



Common-Emitter Configuration

Input impedance:

$$Z_i = \beta r_e$$

Output impedance:

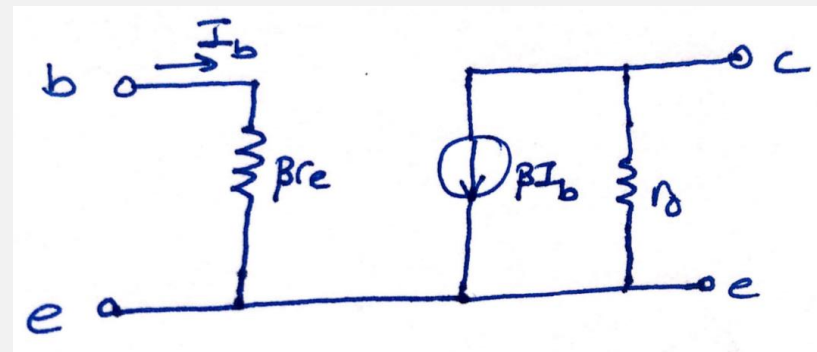
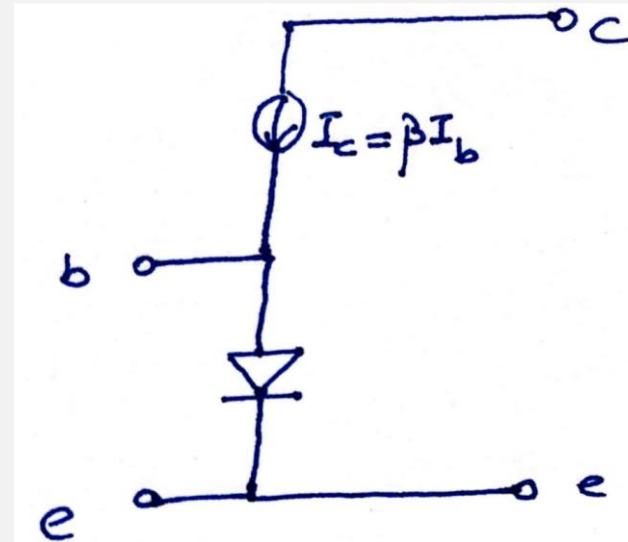
$$Z_o = r_o \cong \infty \Omega$$

Voltage gain:

$$A_v = -\frac{R_L}{r_e}$$

Current gain:

$$A_i = \beta \Big|_{r_o = \infty}$$



r_e model

Common-Collector Configuration

Input impedance:

$$Z_i = (\beta + 1)r_e$$

Output impedance:

$$Z_o = r_e \parallel R_E$$

Common emitter model is also applied similarly to common-collector configuration.

Voltage gain:

$$A_V = \frac{R_E}{R_E + r_e}$$

Current gain:

$$A_i = \beta + 1$$

The Hybrid Equivalent Model

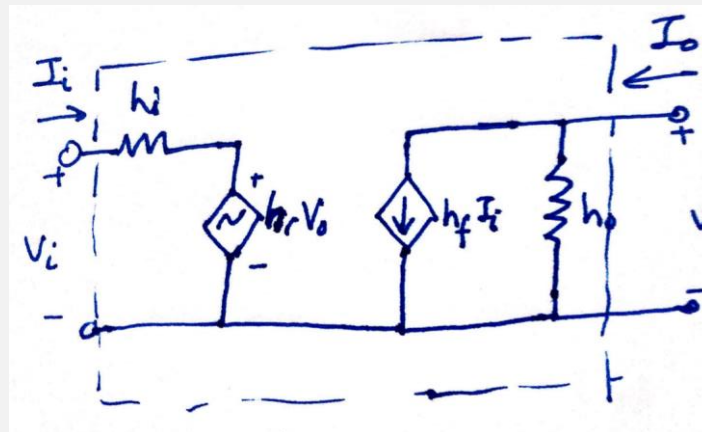
Hybrid parameters are developed and used for modeling the transistor. These parameters can be found on a transistor's specification sheet:

h_i = input resistance

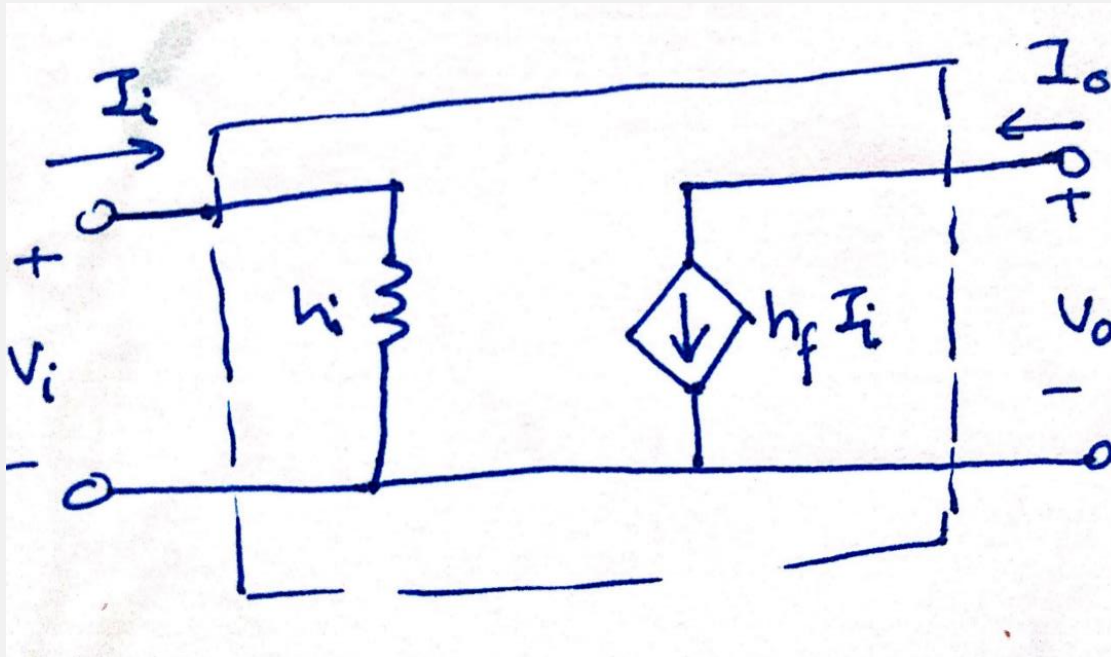
h_r = reverse transfer voltage ratio (V_i/V_o) $\cong 0$

h_f = forward transfer current ratio (I_o/I_i)

h_o = output conductance



Simplified General h-Parameter Model



h_i = input resistance

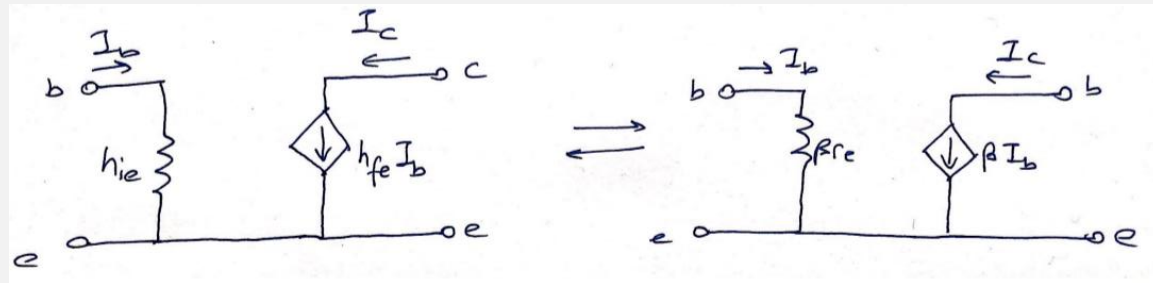
h_f = forward transfer current ratio (I_o/I_i)

r_e vs. h-Parameter Model

Common-Emitter

$$h_{ie} = \beta r_e$$

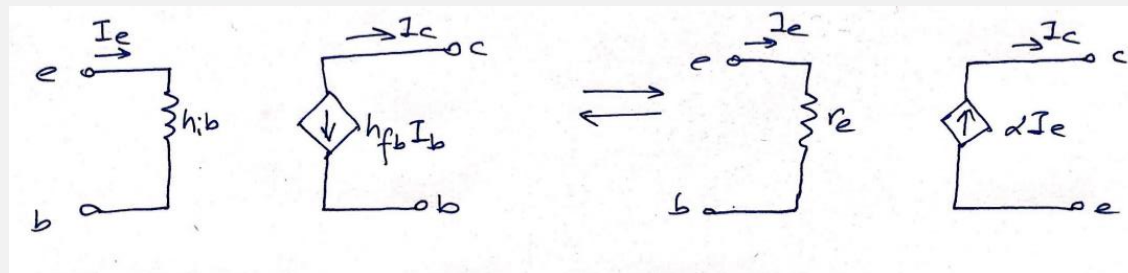
$$h_{fe} = \beta_{ac}$$



Common-Base

$$h_{ib} = r_e$$

$$h_{fb} = -\alpha \cong -1$$



The Hybrid π Model



The hybrid pi model is most useful for analysis of **high-frequency transistor** applications.

At lower frequencies the hybrid pi model closely approximate the r_e parameters, and can be replaced by them.