

CEN 212 FLUID MECHANICS

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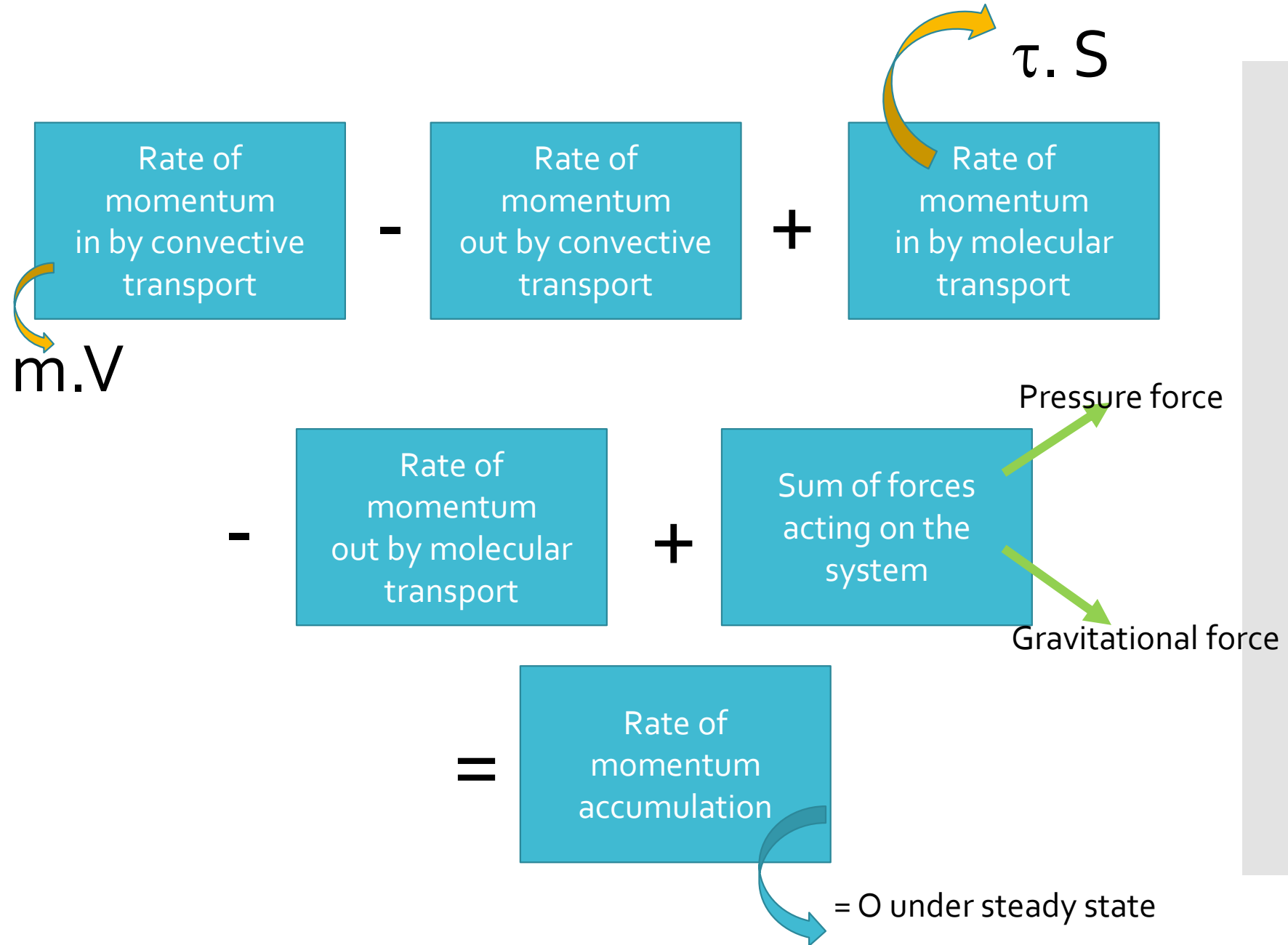
MOMENTUM BALANCE

- SHELL MOMENTUM BALANCES and VELOCITY DISTRIBUTIONS IN LAMINAR FLOW

In order to obtain a velocity profile in flow systems, a momentum balance shall be made on a volume element, in which momentum enters and leaves the system by;

- a. Convection: from flow of the bulk fluid
- b. Molecular transport: as a result of velocity gradients (viscous action)

MOMENTUM BALANCE



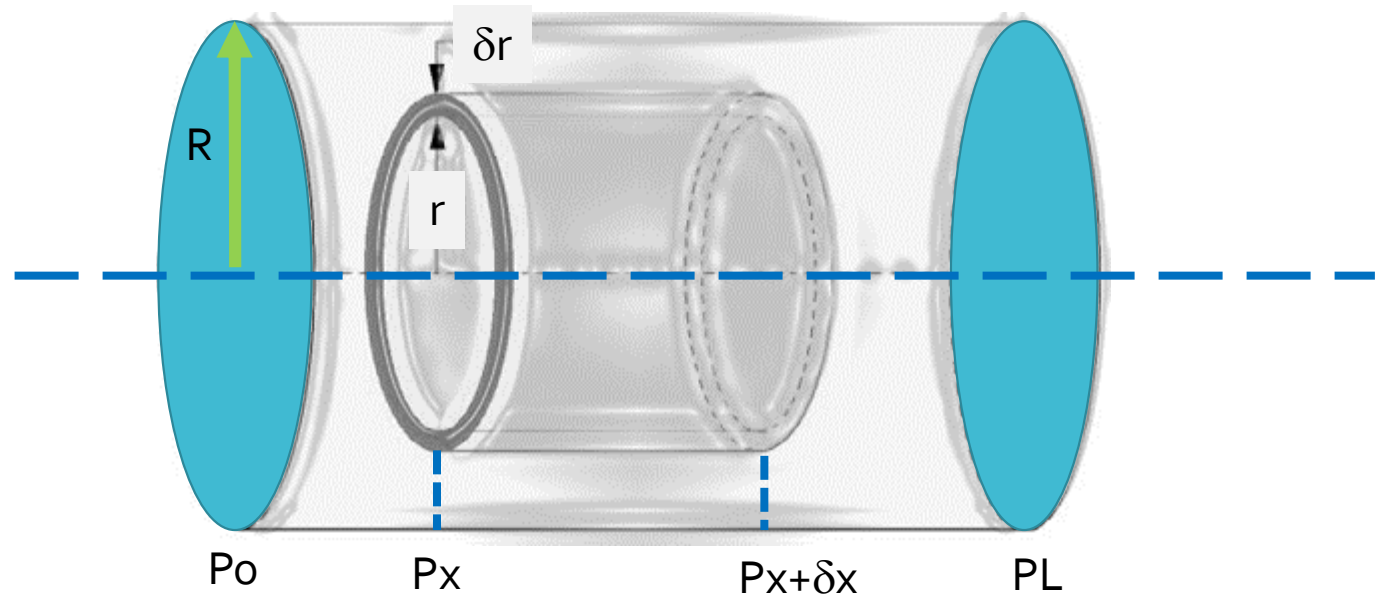
MOMENTUM BALANCE

- In order to set up and solve viscous problems
 - a. A momentum balance over a thin shell should be written.
 - b. The differential equation for the momentum flux should be written.
 - c. Newton's Law of Viscosity should be inserted to obtain a differential equation for the velocity
 - d. This equation should be solved by using boundary conditions.

MOMENTUM BALANCE

- Boundary conditions are statements about the velocity or stress at the boundaries of the system. The most commonly used boundary conditions are:
 - a. At solid-liquid interface, the velocity of the fluid equals the velocity of the solid surface tangential to the fluid.
 - b. At liquid-liquid interface, momentum transport and velocity perpendicular to the interface is constant.
 - c. At gas-liquid interface momentum transport is taken to be zero.

MOMENTUM BALANCE



Assumptions:

- One-dimensional laminar flow
- Newtonian fluid
- End-effects are ignored
- Steady-state

MOMENTUM BALANCE

- Total momentum balance equation:

- $\tau r x \cdot 2\pi r \Delta x \Big|_r - \tau r x \cdot 2\pi r \Delta x \Big|_{r+\Delta r} + \rho V x \cdot 2\pi r \Delta r \Big|_x - \rho V x \cdot 2\pi r \Delta r \Big|_{x+\Delta x} +$

$$P 2\pi r \Delta r \Big|_x - P 2\pi r \Delta r \Big|_{x+\Delta x} = 0$$

MOMENTUM BALANCE

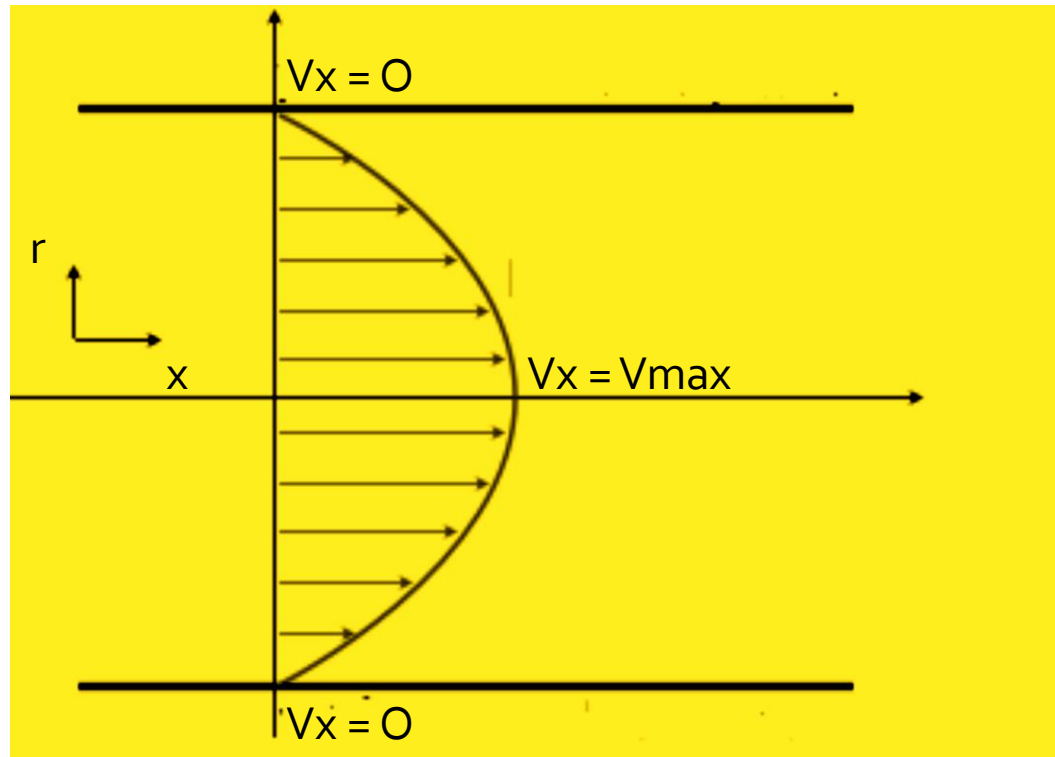
$$V_x = \frac{\Delta P}{\mu L} \frac{r^2}{4} + c_1 \ln r + C_2$$

Boundary conditions are:

1. $r=R$ $V_x=0$
2. $R=0$ $V_x=V_{\max}$

MOMENTUM BALANCE

- $$V_x = \frac{(P_0 - P_L)}{4\mu L} \cdot R^2 \left(1 - \left(\frac{r}{R}\right)^2\right)$$



MOMENTUM BALANCE

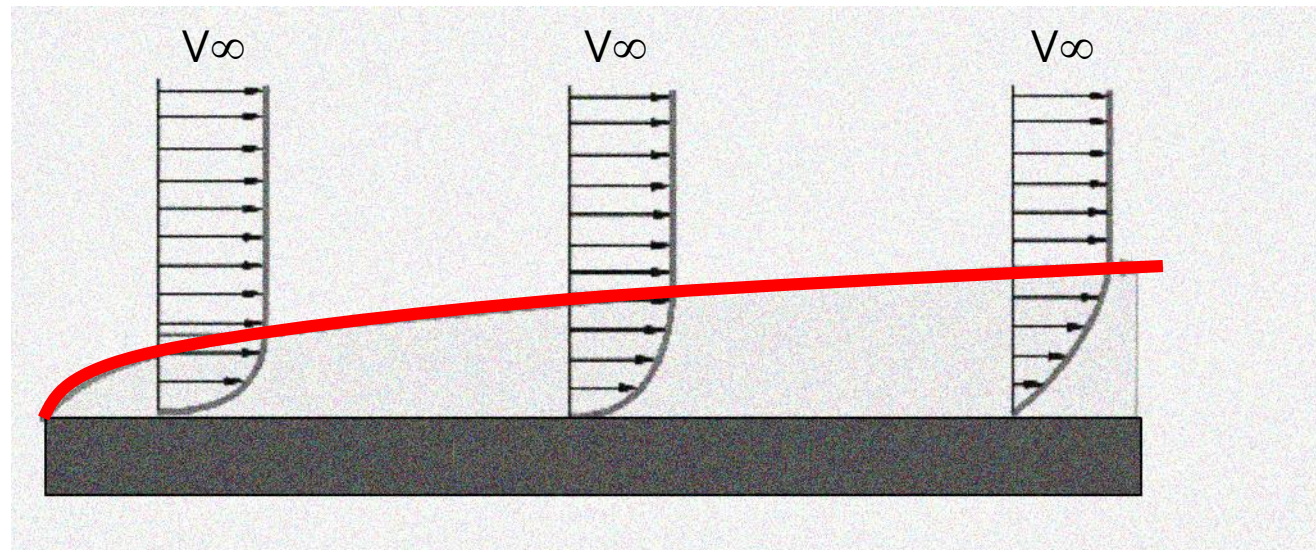
HAGEN-POISEUILLE EQUATION;

$$V_x = \frac{(P_o - P_L)D^2}{32 \mu L}$$

gives the pressure drop because of friction in laminar flow through a horizontal pipe. One of its uses is in the experimental measurement of viscosity

BOUNDARY LAYERS

- A Boundary Layer is defined as that part of a moving fluid in which the fluid motion is influenced by the presence of a solid boundary.



BOUNDARY LAYERS

