

CEN 207 Physical Chemistry

Text book:

Atkins' Physical Chemistry, Peter Atkins, Julio de Paula, James Keeler, 11th Edition, Oxford University Press.

Reference books

- . Physical Chemistry, [Robert J. Silbey](#), Robert A. Alberty, [Moungi G. Bawendi](#)
- . Physical Chemistry, Ira N. Levine

B. The kinetic model

In the kinetic theory of gases (which is sometimes called the kinetic-molecular theory, KMT) it is assumed that the only contribution to the energy of the gas is from the kinetic energies of the molecules.

The model assumptions:

- i. The gas consists of molecules of mass m ceaseless random motion obeying the laws of classical mechanics.
- ii. The size of the molecules is negligible, in the sense that their diameters are much smaller than the average distance travelled between collisions; they are “point-like”.
- iii. The molecules interact only through brief elastical collisions. (An elastical collision is a collision in which the total translational kinetic energy of the molecules is conserved).

B. The kinetic model

Pressure and molecular speeds: using the kinetic model to derive an expression for the pressure of a gas.

The calculation of the change in momentum:

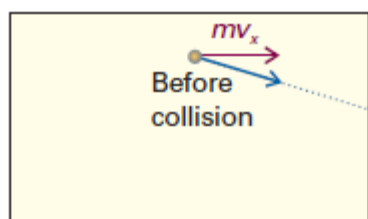
m : particle mass;

v_x : a component of velocity is parallel to the x-axis

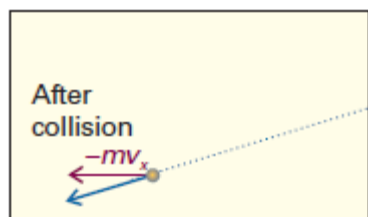
Linear momentum: mv_x (before collision)

Linear momentum: $-mv_x$ (after collision)

The x-component of momentum therefore changes by $2mv_x$ (y and z components are unchanged. Many molecules collide with the wall in an interval Δt (for total change of momentum x the number of molecules)



(a)



(b)

B. The kinetic model

distance ($v_x \Delta t$) along with the x-axis to strike the wall.

A: the area of the wall

V: the volume ($A \cdot v_x \Delta t$) all the particles reach the wall (if they are travelling towards it)

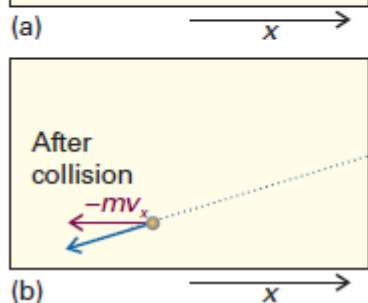
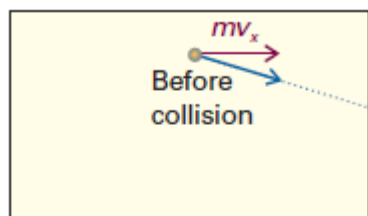
The number density of particles: nN_A/V

n: the total amount of molecules,

N_A : Avogadro's constant

V: the container of volume

It follows that the number of molecules in the volume ($A \cdot v_x \Delta t$) is $(nN_A/V) \times (A \cdot v_x \Delta t)$



B. The kinetic model

The total momentum change:

$$\text{Momentum change} = \frac{nN_A Av_x \Delta t}{2V} * 2mv_x = \frac{n \overbrace{mN_A}^M Av_x^2 \Delta t}{V} = \frac{nMAv_x^2 \Delta t}{V}$$

Calculate the force

Momentum change is divided by the interval Δt during which it occurs, is

$$\text{Rate of change of momentum} = \frac{nMAv_x^2}{V}$$

Rate of change of momentum = Force (according to Newton's second law of motion).

Calculate the pressure

$$\text{Pressure} = \frac{nM\langle v_x^2 \rangle}{V} ; \langle v_x^2 \rangle = \frac{1}{3} \langle v^2 \rangle$$

B. The kinetic model

$$v_{rms} = \langle v^2 \rangle^{1/2} \quad \text{Root-mean-square speed (definition)}$$

So it can be written for the pressure as

$$\langle v_x^2 \rangle = \frac{1}{3} \langle v^2 \rangle = \frac{1}{3} v_{rms}^2$$

to give

$$pV = \frac{1}{3} nM v_{rms}^2$$

Relation between pressure and volume [KMT]

pV= constant (at constant temperature) which is the content of Boyle's law. The right-hand side of the equation is equal to **nRT** (pV=nRT).