Advanced Quantum Mechanics

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The continuity condition requires that:

$$\Psi_I(0)=\Psi_{II}(0),$$
 boundary between regions and II $\Psi_{II}(L)=\Psi_{III}(L),$ boundary between regions and III Also, the first derivatives of the solution must e continuous at

Also, the first derivatives of the solution must e continuous at region boundaries:

$$[x = 0] \rightarrow \frac{d\Psi_{I}(x)}{dx} = \frac{d\Psi_{II}(x)}{dx}$$
$$[x = L] \rightarrow \frac{d\Psi_{II}(x)}{dx} = \frac{d\Psi_{III}(x)}{dx}$$

then we can write:

$$A+B=C+D \quad and \quad Ce^{ik_{II}L}+De^{-ik_{II}L}=Fe^{ik_{III}L}$$

$$-ik_{I}(A-B)=ik_{II}(D-C) \quad and \quad ik_{II}(De^{ik_{II}L}-Ce^{-ik_{II}L})=-ik_{III}Fe^{k_{III}L}$$
 from all those relations we find :

$$F = 4k_{I}k_{II}Ae^{-ik_{I}L}\left[4k_{I}k_{II}\cos(k_{II}L)Big - 2i(k_{I}^{2} + k_{II}^{2})\sin(k_{2}a)\right]$$

$$\frac{F}{A} = \frac{4k_{I}k_{II}}{\sqrt{16k_{I}^{2}k_{II}^{2}\cos^{2}(k_{II}L) + 4k_{I}^{2}k_{II}^{2}\sin^{2}(k_{II}L)}}$$

$$T = \left[1 + rac{1}{4} rac{(k_I - \left(k_{II})^2}{k_I k_{II}}
ight)^2 sin^2 (k_{II}a) Big]^{-1}$$