## Circuits Containing Resistors & Capacitors (RC Circuits)



# **RC Circuits**

When the switch is closed, the capacitor will begin to charge. As it does, the voltage across it increases, and the current through the resistor decreases.



- To find the voltage as a function of time, use the **Loop Rule** to write the equation for the *voltage changes* around the loop:  $\mathscr{E} = IR + \frac{Q}{C}$ .
- $\mathbf{I} = \mathbf{dQ}/\mathbf{dt}$ , so integrate to find the charge as a function of time:  $Q = C \mathscr{C}(1 - e^{-t/RC}).$
- The voltage across the capacitor is  $V_C = Q/C$ . The current I at time t is found by differentiating the charge:  $\frac{dQ}{dQ} = \frac{e^{-t/RC}}{e^{-t/RC}}$

$$I = \frac{dQ}{dt} = \frac{\mathscr{C}}{R} e^{-t/RC}.$$

• The quantity **RC** that appears in the exponent is called *the time constant* of the circuit:  $\tau$ 

$$\tau = RC.$$

## **Example**

## **RC Circuit, with EMF.**

•The capacitance in the circuit shown is  $C = 0.30 \ \mu F$ , the total resistance is  $R = 20 \ k\Omega$ , the battery emf is

### $E = 12 V. \qquad \underline{Calculate}:$

(a) the time constant,



- (b) the maximum charge the capacitor could acquire,
- (c) the time it takes for the charge to reach 99% of this value,
- (d) the current I when the charge Q is half its maximum value,
- (e) the maximum current,
- (f) the charge Q when the current I is 0.20 of its maximum value.

• If an isolated charged capacitor is connected across a resistor, *it discharges:* 

$$Q = Q_0 e^{-t/RC}.$$

• The voltage & current as functions of time can be found from the charge:

$$V_{\rm C} = V_0 e^{-t/RC}$$



and 
$$I = -\frac{dQ}{dt} = \frac{Q_0}{RC}e^{-t/RC} = I_0 e^{-t/RC}$$
.

#### **Example:** Discharging *RC* circuit.

In the RC circuit shown, the battery has fully charged the capacitor, so Q<sub>0</sub> = C E. Then at t = 0 the switch is thrown from position a to b. The battery emf is 20.0 V, and the capacitance C = 1.02 μF. The current I is observed to decrease to 0.50 of its initial value in 40 μs.
(a) What is the value of Q, the charge on the capacitor, at t = 0?
(b) What is the value of R? (c) What is Q at t = 60 μs?



### **Conceptual Example: Bulb in RC circuit.**

- In the circuit shown, the capacitor is originally uncharged.
- Describe the behavior of the lightbulb from the instant switch S is closed until a long time later.



### **Example Resistor in a turn signal.** Estimate the order of magnitude of the resistor in a turn-signal circuit.



## **Electric Hazards**

- Most people can "feel" a current of 1 mA; a few mA of current begins to be painful. Currents above 10 mA may cause uncontrollable muscle contractions, making rescue difficult.
- Currents around **100 mA** passing through the torso can cause death by ventricular fibrillation.
- Higher currents may not cause fibrillation, but can cause severe burns.
- Household voltage can be lethal if you are wet and in good contact with the ground. Be careful!

### A person receiving a shock has become part of a complete circuit.



Faulty wiring and improper grounding can be hazardous. Make sure electrical work is done by a professional.



- The safest plugs are those with three prongs; they have a separate ground line.
- Here is an example of household wiring colors can vary, though! Be sure you know which is the hot wire before you do anything.

