

CEN-CHE 422
ENZYME ENGINEERING

Determination of K_m and r_{\max}

$$r = \frac{r_{\max} C_S}{K_m + C_S}$$

The graph of MM equation (r vs C_S) is not entirely satisfactory for the determination of r_{\max} and K_m .

Michaelis-Menten equation is linearized by being inverted to $y=n+mx$ form

- ✓ Lineweaver-Burk Equation*
- ✓ Eadie-Hoffstee Equation
- ✓ Hanes-Woolf Equation
(Langmuir Equation)

$$\frac{1}{r} = \frac{K_m}{r_{\max}} \frac{1}{C_S} + \frac{1}{r_{\max}}$$

$$\frac{r}{C_S} = \frac{r_{\max}}{K_m} - \frac{1}{K_m} r$$

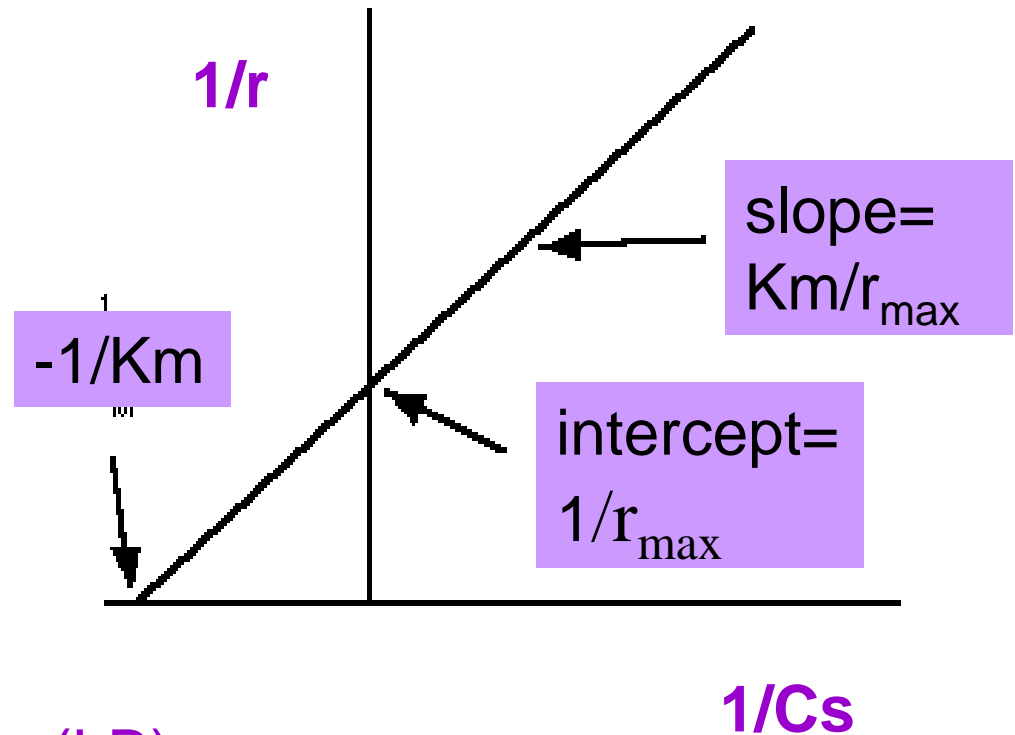
$$\left(\frac{C_S}{r} = \frac{K_m}{r_{\max}} + \frac{C_S}{r_{\max}} \right)$$

Lineweaver-Burk Graph

$$r = \frac{r_{\max} C_S}{K_m + C_S}$$

If MM equation is inverted: :

$$\frac{1}{r} = \frac{K_m}{r_{\max}} \frac{1}{C_S} + \frac{1}{r_{\max}}$$



Lineweaver-Burk Equation (LB)

$$\text{slope} = \frac{K_m}{r_{\max}} \quad \text{intercept} = \frac{1}{r_{\max}}$$

Eadie-Hoffstee Graph

$$r = \frac{r_{\max} C_S}{K_m + C_S}$$

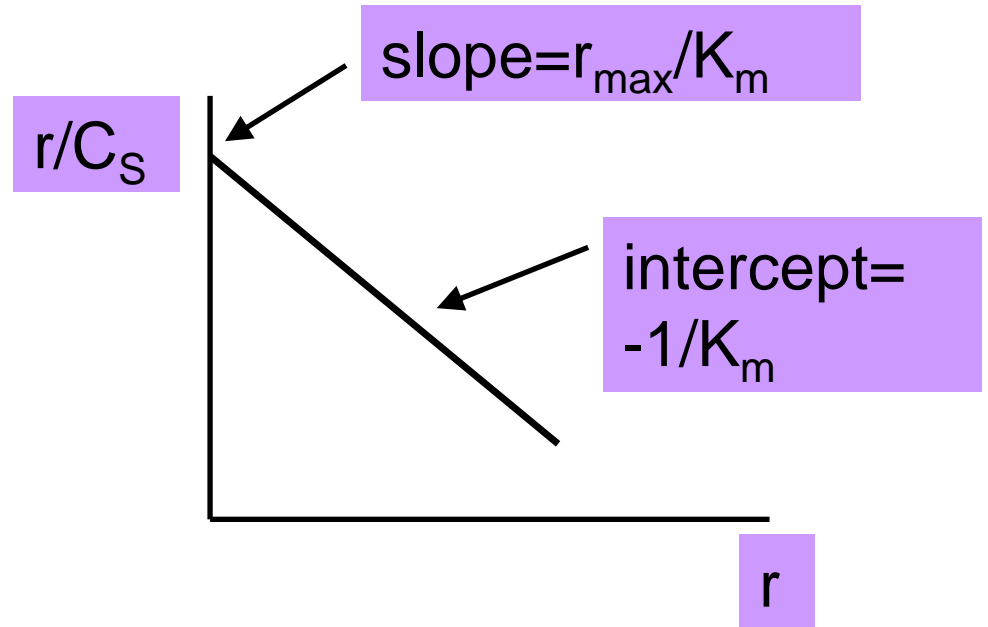
$$r(K_m + C_S) = r_{\max} C_S$$

$$rK_m = (r_{\max} - r)C_S$$

$$\frac{r}{C_S} = \frac{r_{\max}}{K_m} - \frac{1}{K_m} r$$

$$\text{intercept} = \frac{r_{\max}}{K_m}$$

$$\text{slope} = -\frac{1}{K_m}$$



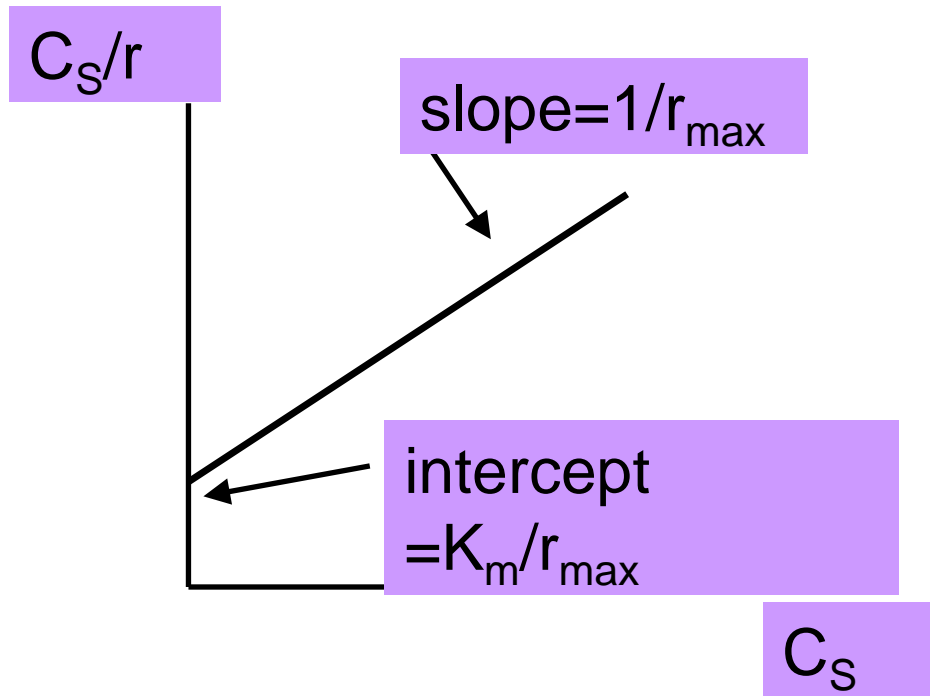
Eadie-Hoffstee Equation

Hanes-Woolf Graph

$$C_S \times \left(\frac{1}{r} = \frac{K_m}{r_{\max}} \frac{1}{C_S} + \frac{1}{r_{\max}} \right) \times C_S$$

$$\left(\frac{C_S}{r} = \frac{K_m}{r_{\max}} + \frac{C_S}{r_{\max}} \right)$$

Hanes-Woolf Equation



$$\text{slope} = \frac{1}{r_{\max}}$$

$$\text{intercept} = \frac{K_m}{r_{\max}}$$

ENZYMЕ INHIBITION

Inhibitor(I): Inhibitors are substances which tend to decrease the rate of enzyme-catalysed reaction (by forming a complex, EI, ES, ESI, etc..)

1. Irreversible Inhibition

2. Reversible Inhibition

Competitive Inhibition

Uncompetitive Inhibition

Noncompetitive Inhibition

Mixed Inhibition

Substrate Inhibition

Partial Inhibition

Allosteric Inhibition

Irreversible Inhibition

- There is no structural similarity between the substrate and the enzyme
- The active group of the enzyme undergoes chemical change. Therefore, the enzyme-inhibitor complex cannot re-dissociate to form an active enzyme.
- These inhibitors are known as enzyme poisons.
- Iodoacetate and some heavy metal ions metal cations
- *This type of inhibition is permanent*

Competitive Inhibition

Competitive inhibitors closely resemble in some respects the substrate whose reactions they inhibit.

Because of the similarity they may compete for the same binding-site on the enzyme.



quasi-steady-state assumption

Inhibitor binds to active site on enzyme $\frac{dC_{ES}}{dt} = 0$

$$\frac{dC_{EI}}{dt} = 0$$

reaction rate: $r = k_2 \underline{C_{ES}}?$

$$\frac{dC_{ES}}{dt} = k_1 C_E C_S - k_{-1} C_{ES} - k_2 C_{ES} = 0$$

$$C_{ES} = \frac{k_1}{k_{-1} + k_2} C_E C_S \quad \longrightarrow \quad C_{ES} = \frac{C_E C_S}{Km} \quad \checkmark$$

$$\frac{dC_{EI}}{dt} = k_i C_E C_I - k_{-i} C_{EI} = 0$$

$$C_{EI} = \frac{k_i}{k_{-i}} C_E C_I \quad \longrightarrow \quad C_{EI} = \frac{C_E C_I}{Ki} \quad \checkmark$$

Enzyme balance: $C_{Eo} = C_E + C_{ES} + C_{EI}$

$$C_{Eo} = C_E + \frac{C_E C_I}{K_i} + \frac{C_E C_S}{K_m}$$

$$C_E = \frac{C_{Eo}}{1 + \frac{C_S}{K_m} + \frac{C_I}{K_i}} \quad \checkmark$$

$$C_{ES} = \frac{C_E C_S}{K_m}$$

If we substitute C_E into C_{ES}

$$C_{ES} = \frac{C_S}{K_m} \times \frac{C_{Eo}}{1 + \frac{C_S}{K_m} + \frac{C_I}{K_i}} \quad \longrightarrow \quad C_{ES} = \frac{C_S C_{Eo}}{K_m + C_S + \frac{K_m}{K_i} C_I}$$

reaction rate:

$$r = k_2 C_{ES} = \frac{k_2 C_{Eo} C_S}{C_S + K_m \left(1 + \frac{C_I}{K_i}\right)} \quad \longrightarrow \quad r = \frac{r_{\max} C_S}{C_S + \underbrace{K_m \left(1 + \frac{C_I}{K_i}\right)}_{K_m^*}} \quad \checkmark$$

If MM equation is linearized (LB):

$$\frac{1}{r} = \frac{K_m}{r_{\max}} \left(1 + \frac{C_I}{K_i}\right) \frac{1}{C_S} + \frac{1}{r_{\max}}$$

$$\text{slope} = \frac{K_m}{r_{\max}} \left(1 + \frac{C_I}{K_i}\right)$$

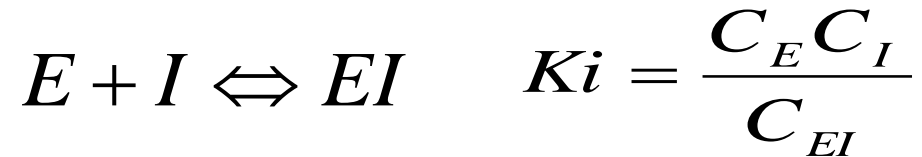
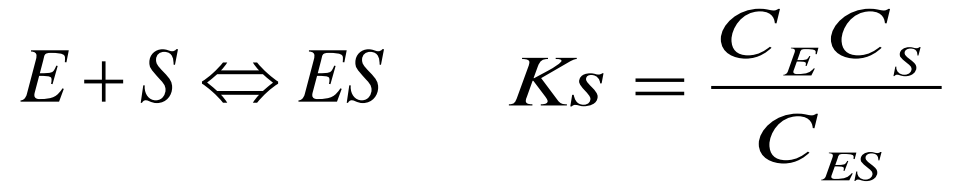
$$\text{intercept} = \frac{1}{r_{\max}}$$

*The lines intersect
at the same point
on 1/r axis (1/r_{max})*

*1/r_{max} is unchanged by the
addition of inhibitor*

If the lines drawn at different inhibitor concentrations intersect at the same point on the ordinate, the type of inhibition is **competitive inhibition**

Noncompetitive Inhibition



reaction rate: $r = k_2 C_{ES}$
?

Michaelis-Menten assumption:

Enzyme balance:

$$C_{E_0} = C_E + C_{ES} + C_{EI} + C_{ESI}$$

Using dissociation constants:

$$C_{ES} = \frac{C_E C_S}{K_S} \quad C_{EI} = \frac{C_E C_I}{K_i} \quad C_{ESI} = \frac{C_{ES} C_I}{K_i} = \frac{C_E C_S C_I}{K_i K_S}$$

Inserting in C_{E_0}

$$C_{E_0} = C_E + \frac{C_E C_S}{K_S} + \frac{C_E C_I}{K_i} + \frac{C_E C_S C_I}{K_i K_S}$$
$$C_{E_0} = C_E \left(1 + \frac{C_S}{K_S} + \frac{C_I}{K_i} + \frac{C_S C_I}{K_i K_S} \right)$$

$$C_E = \frac{C_{Eo}}{\left(1 + \frac{C_S}{K_S} + \frac{C_I}{K_i} + \frac{C_I C_S}{K_i K_S}\right)}$$

Inserting in C_{ES}

$$C_{ES} = \frac{C_E C_S}{K_S}$$

$$C_{ES} = \frac{C_S}{K_S} \times \frac{C_{Eo}}{\left(1 + \frac{C_S}{K_S} + \frac{C_I}{K_i} + \frac{C_I C_S}{K_i K_S}\right)}$$

$$C_{ES} = \frac{C_{Eo} C_S}{\left(K_S + C_S + \frac{C_I K_S}{K_i} + \frac{C_I C_S}{K_i}\right)}$$



reaction rate: $r = k_2 C_{ES} = \frac{k_2 C_{Eo} C_S}{K_S \left(1 + \frac{C_I}{K_i}\right) + C_S \left(1 + \frac{C_I}{K_i}\right)}$

$$r = \frac{C_S r_{\max}}{(K_S + C_S) \left(1 + \frac{C_I}{K_i}\right)} r_{\max}^*$$

If MM equation is linearized:

$$\frac{1}{r} = \frac{K_m}{r_{\max}} \left(1 + \frac{C_I}{K_i}\right) \frac{1}{C_S} + \frac{1}{r_{\max}} \left(1 + \frac{C_I}{K_i}\right)$$

$$\text{slope} = \frac{K_m}{r_{\max}} \left(1 + \frac{C_I}{K_i}\right)$$

$$\text{intercept} = \frac{1}{r_{\max}} \left(1 + \frac{C_i}{K_i}\right)$$

$$K_S = \frac{k_{-1}}{k_1}$$

$$K_m = \frac{k_{-1} + k_2}{k_1}$$

$$k_2 \ll k_{-1}$$

$$\downarrow$$

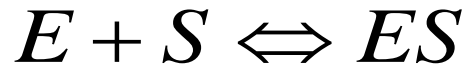
$$K_m = K_S$$

*The lines intersect
at the same point
on $1/C_S$ axis ($1/K_m$)*

If the lines drawn at different inhibitor concentrations intersect at the same point on the x axis, the type of inhibition is **noncompetitive inhibition**

In noncompetitive inhibition :
✓ K_m does not change

Uncompetitive Inhibition



quasi-steady-state assumption

$$\frac{dC_{ES}}{dt} = 0$$

$$\frac{dC_{ESI}}{dt} = 0$$

reaction rate: $r = k_2 C_{ES}$

?

$$\frac{dC_{ES}}{dt} = k_1 C_E C_S - k_{-1} C_{ES} - k_i C_{ES} C_I + k_{-i} C_{ESI} - k_2 C_{ES} = 0$$

$$C_{ES} = \frac{k_1 C_E C_S + k_{-i} C_{ESI}}{(k_{-1} + k_i C_I + k_2)} \quad \checkmark$$

$$\frac{dC_{ESI}}{dt} = k_i C_{ES} C_I - k_{-i} C_{ESI} = 0$$

$$C_{ESI} = \frac{C_{ES} C_I}{(k_{-i} / k_i)} \quad \checkmark$$

Inserting in C_{ES}

$$C_{ES} = \frac{k_1 C_E C_S + k_{-i} \frac{C_{ES} C_I}{(k_{-i} / k_i)}}{(k_{-1} + k_i C_I + k_2)}$$

$$\left[(k_{-1} + k_2 + k_i C_I) - k_i C_I \right] C_{ES} = k_1 C_E C_S \Rightarrow C_{ES} = \frac{k_1 C_E C_S}{(k_{-1} + k_2)}$$

Inserting in C_{ESI}

$$C_{ESI} = \frac{C_I}{K_i} \times \frac{k_1 C_E C_S}{(k_{-1} + k_2)} \quad \checkmark$$

Enzyme mass balance: $C_{E0} = C_E + C_{ES} + C_{ESI}$

$$C_{E0} = C_E + \frac{k_1 C_S}{(k_{-1} + k_2)} C_E + \frac{k_1 C_I C_S}{K_i (k_{-1} + k_2)} C_E$$

$$C_E = \frac{C_{E0}}{1 + \frac{k_1 C_S}{(k_{-1} + k_2)} + \frac{k_1 C_I C_S}{K_i (k_{-1} + k_2)}}$$

Inserting in C_{ES}

$$C_{ES} = \frac{k_1}{(k_{-1} + k_2)} \times \frac{C_{E0}}{1 + \frac{k_1 C_S}{(k_{-1} + k_2)} + \frac{k_1 C_I C_S}{K_i (k_{-1} + k_2)}}$$

$$C_{ES} = \frac{C_{Eo} C_S}{\frac{k_{-1} + k_2}{k_1} + C_S + \frac{C_I C_S}{K_i}}$$

$$C_{ES} = \frac{C_{Eo} C_S}{K_m + C_S + \frac{C_I C_S}{K_i}} \quad \checkmark$$

reaction rate: $r = k_2 C_{ES}$

$$r = \frac{k_2 C_{Eo} C_S}{K_m + C_S + \frac{C_I C_S}{K_i}}$$

$$r = \frac{r_{\max} C_S}{K_m + C_S \left(1 + \frac{C_I}{K_i} \right)}$$

r_{\max}^*

$$r = \frac{r_{\max} / \left[C_S \left(1 + \frac{C_I}{K_i} \right) \right]}{K_m^* / \left[C_S \left(1 + \frac{C_I}{K_i} \right) \right] + C_S}$$

If MM equation is linearized:

$$\frac{1}{r} = \frac{K_m}{r_{\max}} \frac{1}{C_S} + \frac{1}{r_{\max}} \left(1 + \frac{C_I}{K_i} \right)$$

$$\text{slope} = \frac{K_m}{r_{\max}}$$

$$\text{Intercept} = \frac{1}{r_{\max}}$$

The lines are parallel to each other

If the lines drawn at different inhibitor concentrations are parallel to each other, the type of inhibition is **uncompetitive inhibition**