

# Privacy II

Murat Osmanoglu

# Privacy Enhancing Techniques

# - Ring Signatures

## Digital Signatures

PK, SK



# Privacy Enhancing Techniques

# - Ring Signatures

## Digital Signatures

PK, SK



SK



Signature

SIGNING  
ALGORITHM

## Digital Signatures

PK, SK



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PK, SK



1 or 0

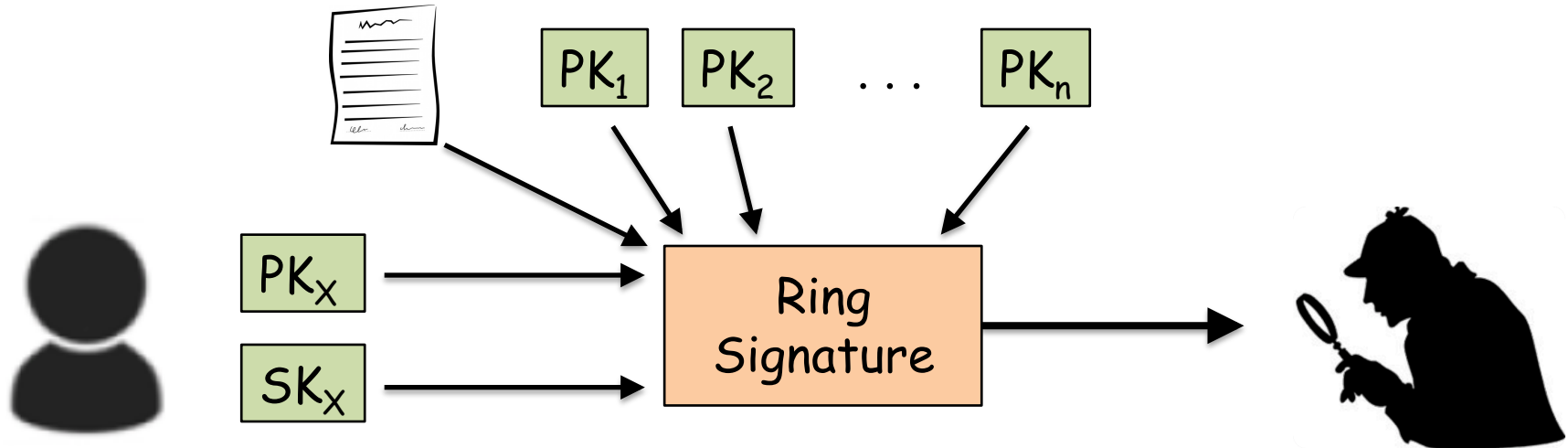


PK

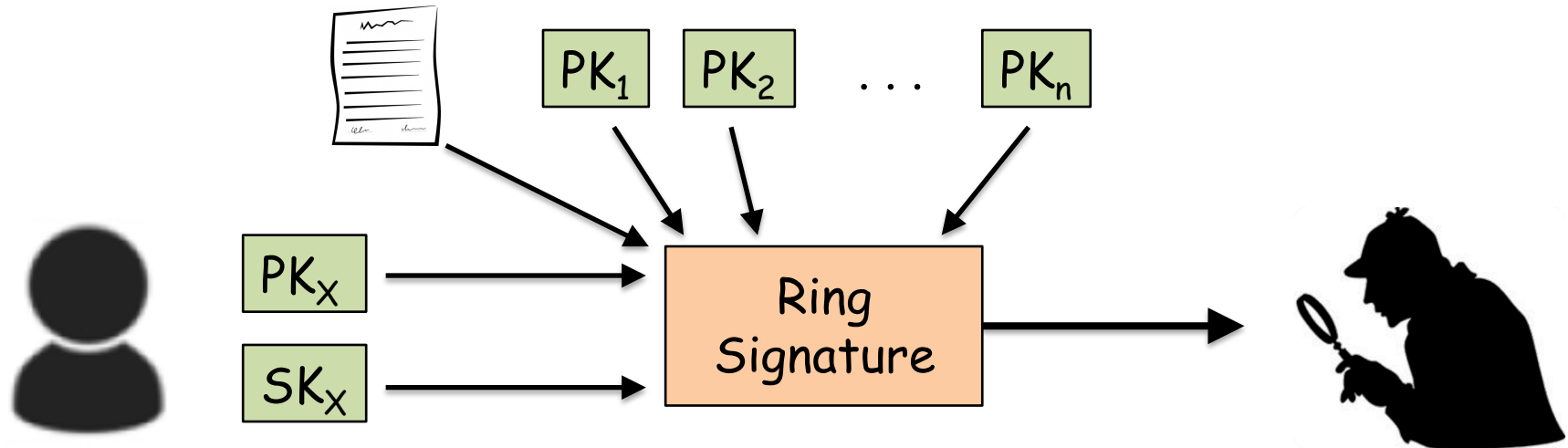


VERIFICATION  
ALGORITHM

- introduced by Rivest et al. [5] in 2001

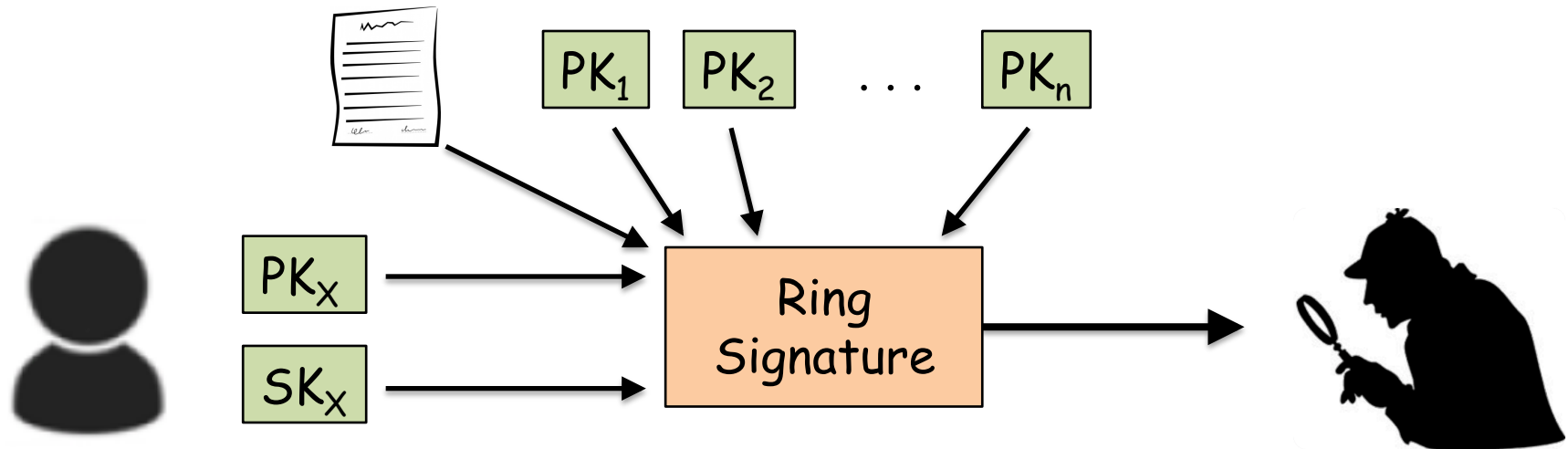


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- verifier can tell that one member from the set  $\{PK_1, PK_2, \dots, PK_n, PK_x\}$  signed the message, but cannot tell which one the actual signer

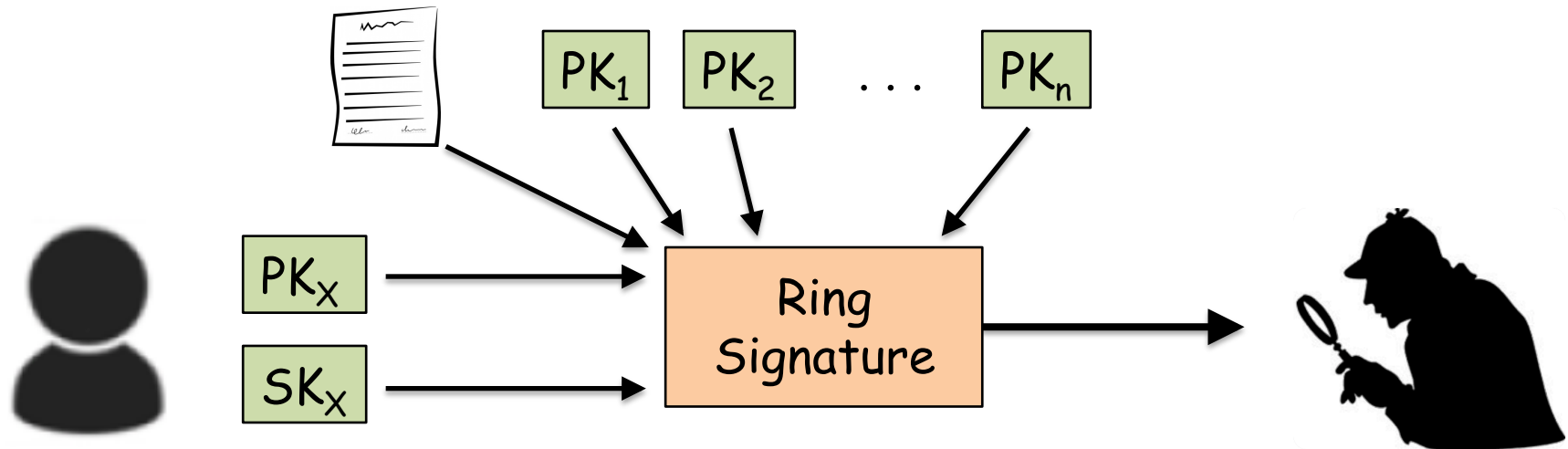
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  - one can vote for two different candidate without being detected



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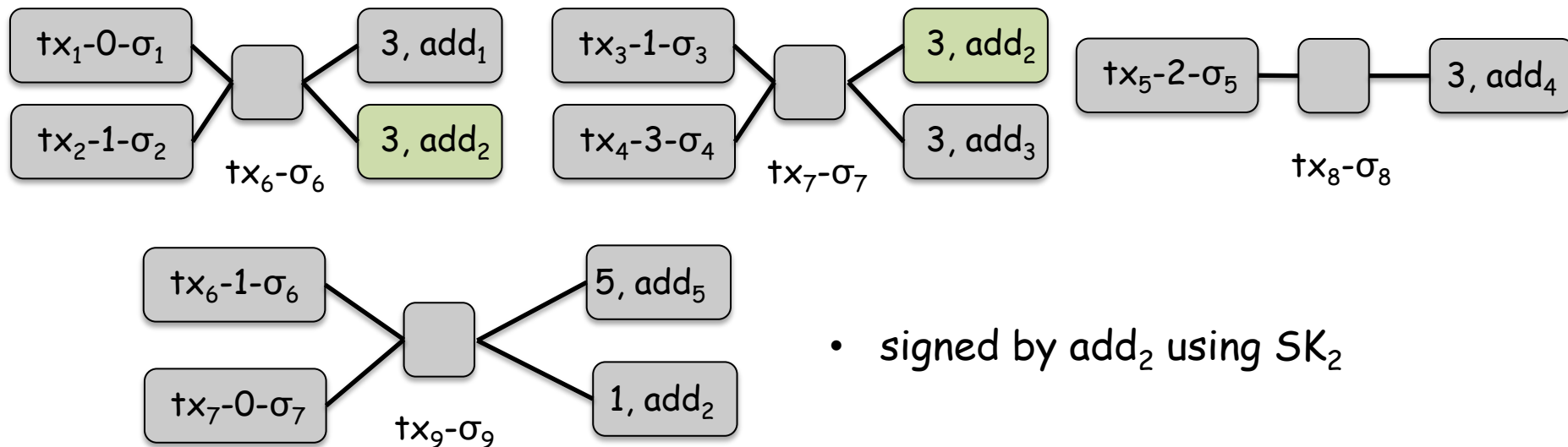


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- assume you designing a voting scheme using ring signatures
  - one can vote for two different candidate without being detected
  - traceable ring signatures, introduced by Fujisaka and Suzuki [6] in 2007, enabling us to detect if two signatures produced by same user

# Privacy Enhancing Techniques

# Ring Signatures

- the transfer of an amount bitcoin ownership rights from one address to another one
- each tx consists of two main fields :
  - input : unspent transaction outputs claimed by the sender from previous transactions (previous transaction id, index, scrip<sub>t</sub>sign)
  - output : instructions for claiming the sent bitcoins (value, scrip<sub>t</sub>publickey)
- if the transaction output not spent before, and the signature is valid, the transaction considered as valid

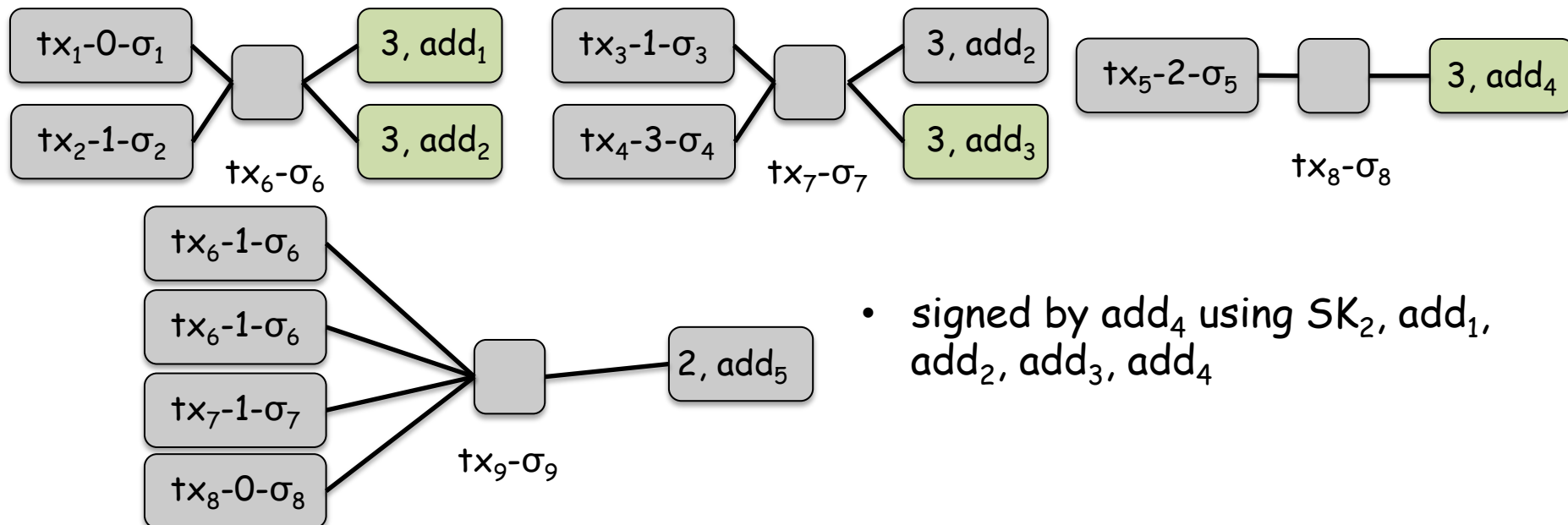


- signed by  $add_2$  using  $SK_2$

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- signed by  $add_4$  using  $SK_2, add_1, add_2, add_3, add_4$

## CryptoNote

- introduced by van Saberhagen [7] in 2013

SENDER

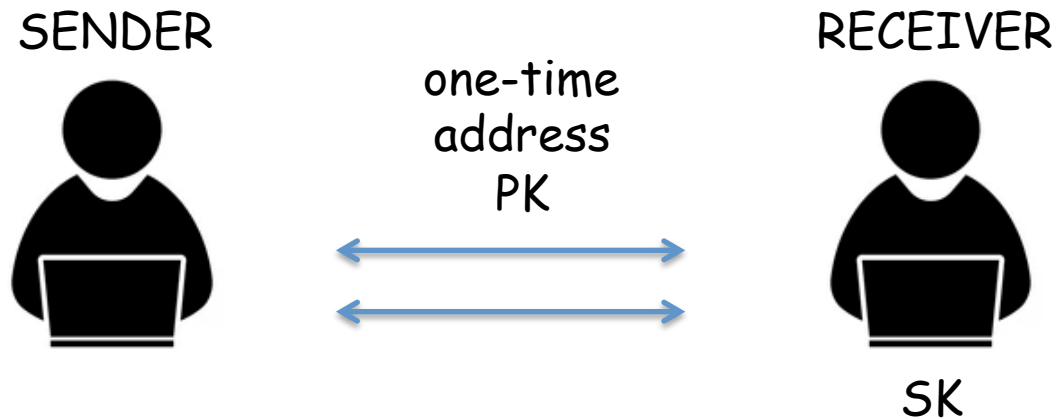


RECEIVER



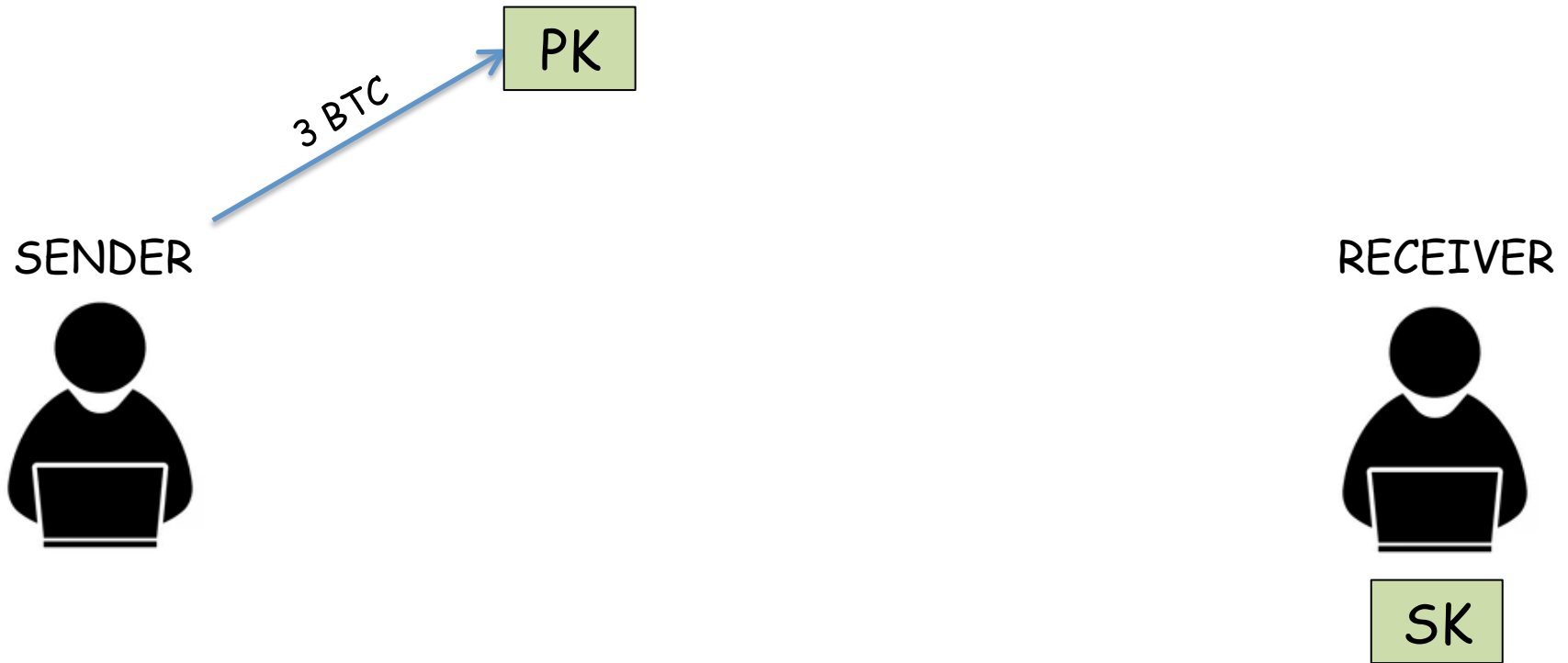
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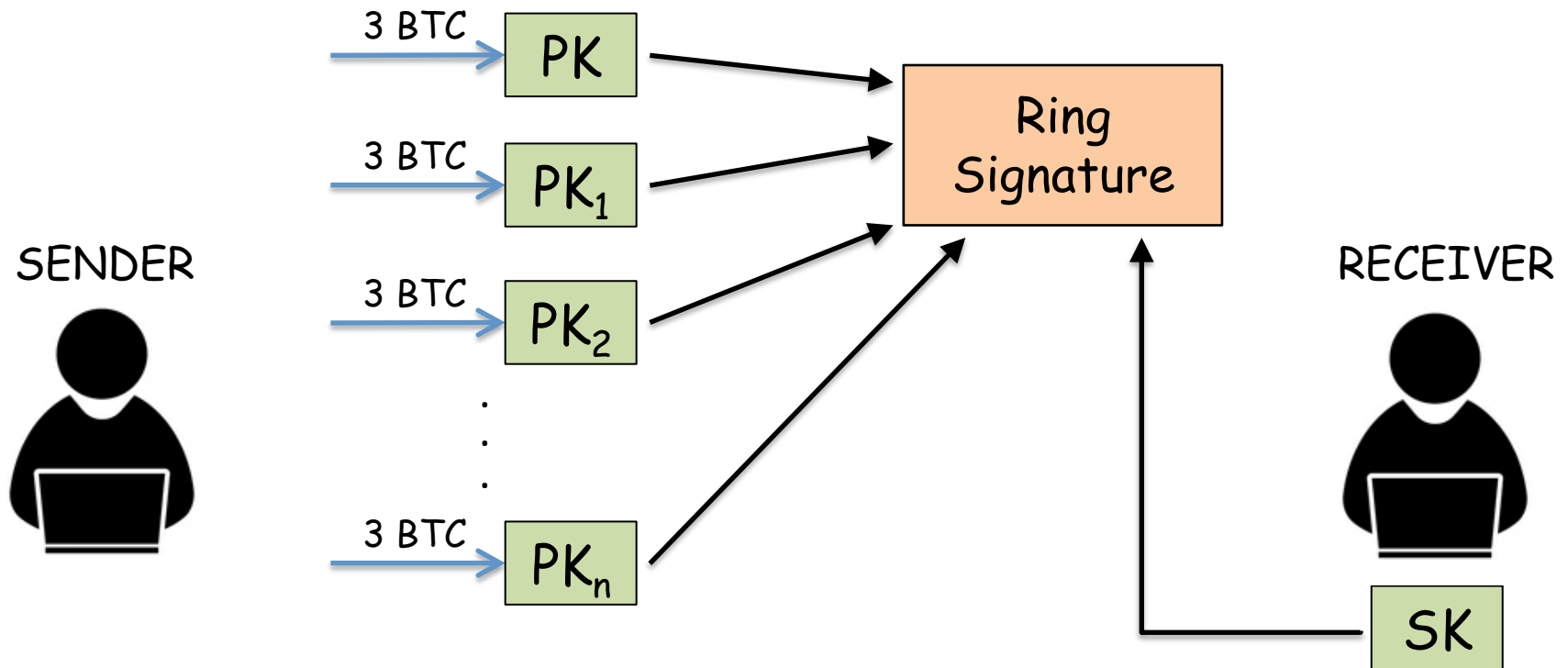
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- introduced by van Saberhagen [7] in 2013
- Kumar et al. [8] analyzed Monero network to examine the untreacibility characteristics of CryptoNote
  - 93% of all transaction output amounts appear only once in the network  
(cannot be combined with others to form ring signatures)
  - users mostly use small number of transaction outputs to avoid high fees

- introduced by Goldwasser et al. [9] in 1985

PROVER



VERIFIER



- allows one party (prover) to convince another party (verifier) that a statement is true without revealing any information other than this fact

# Privacy Enhancing Techniques

# - Zero Knowledge

- introduced by Goldwasser et al. [9] in 1985

AYLA



color-blind

BULENT



# Privacy Enhancing Techniques

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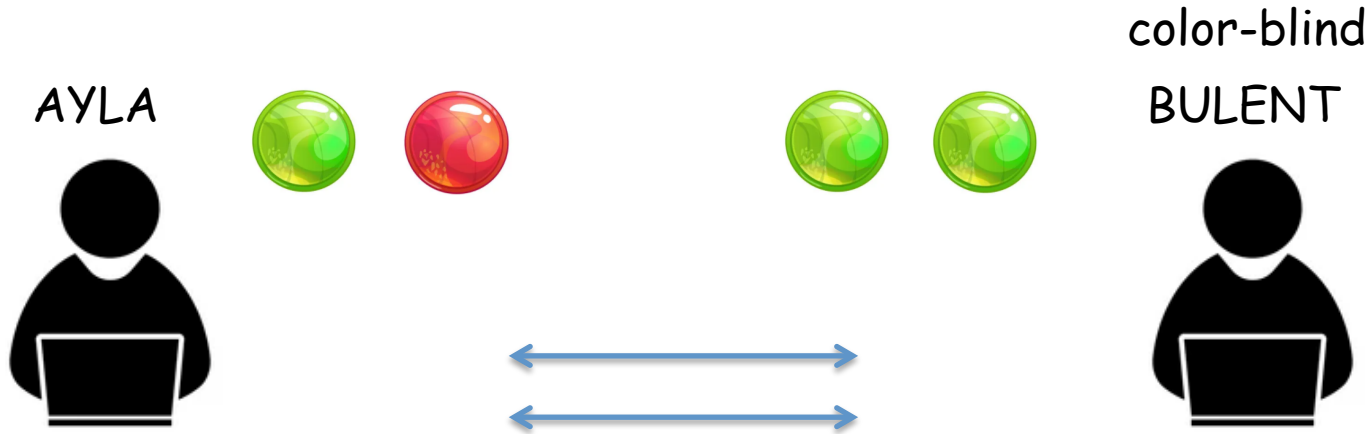


color-blind  
BULENT



they seem completely  
identical to Bulent

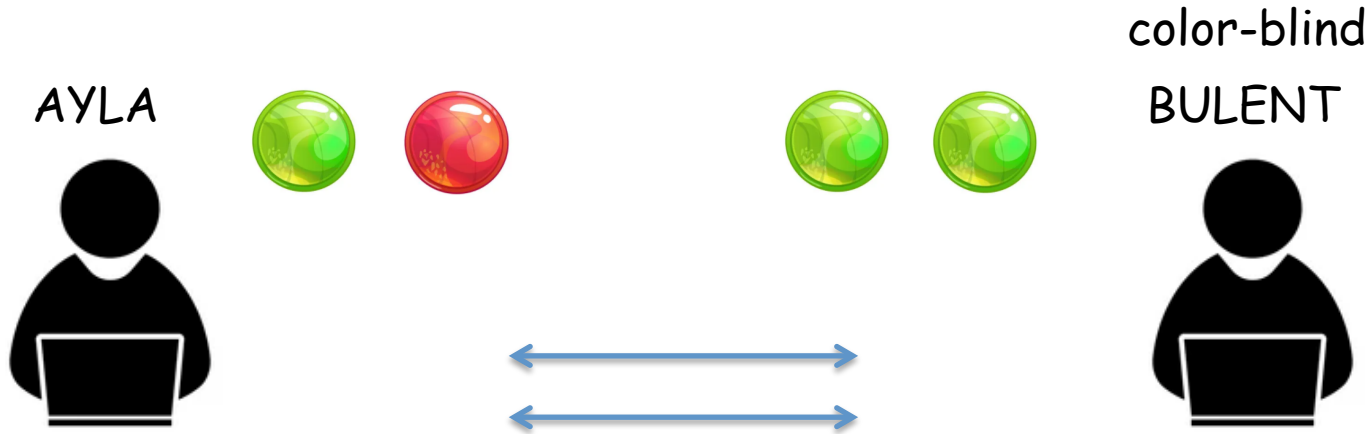
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Ayla wants to convince Bulent they are in different colors without revealing which one is red and which one is green

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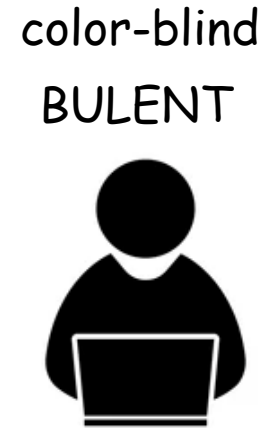
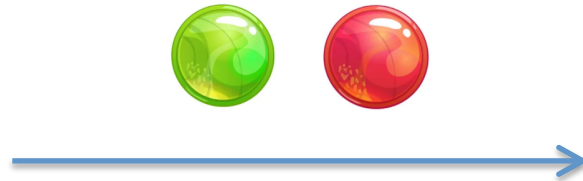


Ayla wants to convince Bulent they are in different colors without revealing which one is red and which one is green

they seem completely identical to Bulent

he thinks they are actually distinguishable

- introduced by Goldwasser et al. [9] in 1985



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he either switching the balls, or keeping them in same hands



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"Did I switch the balls?"

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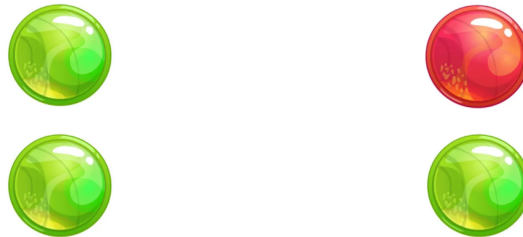


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- assume Ayla doesn't know which one green and which one is red
- what would be the probability that Ayla correctly guess whether he switched or not?

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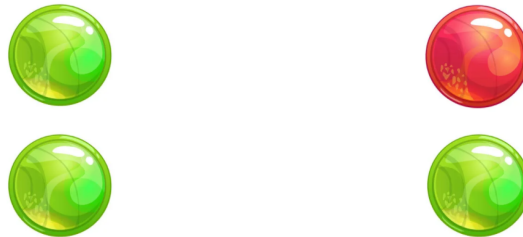
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$$1 / 2 = 0.5$$

$$1 / 2^2 = 0.25$$

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$$1 / 2 = 0.5$$

$$1 / 2^5 = 0.03125$$

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color-blind  
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$$1 / 2 = 0.5$$

$$1 / 2^{10} = 0.00097$$

- introduced by Goldwasser et al. [9] in 1985

PROVER



VERIFIER



- allows one party (prover) to convince another party (verifier) that a statement is true without revealing any information other than this fact
- Completeness : if the statement is true, the honest verifier will be convinced by the honest prover
- Soundness : if the statement is false, no cheating prover can convince the honest verifier that it is true
- Zero-Knowledge : the verifier learns anything other than the statement is true

## ZeroCoin

- introduced by Miers et al. [10] in 2013





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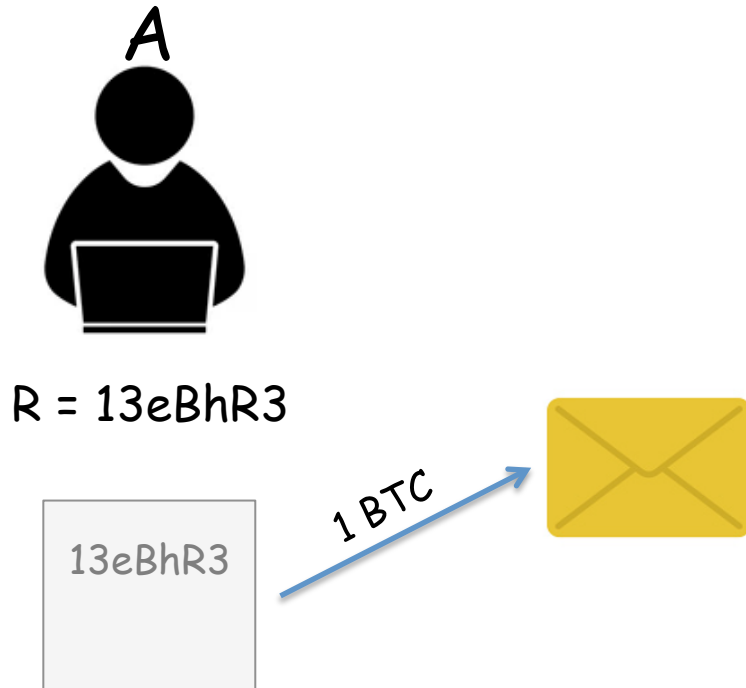


$R = 13eBhR3$

13eBhR3

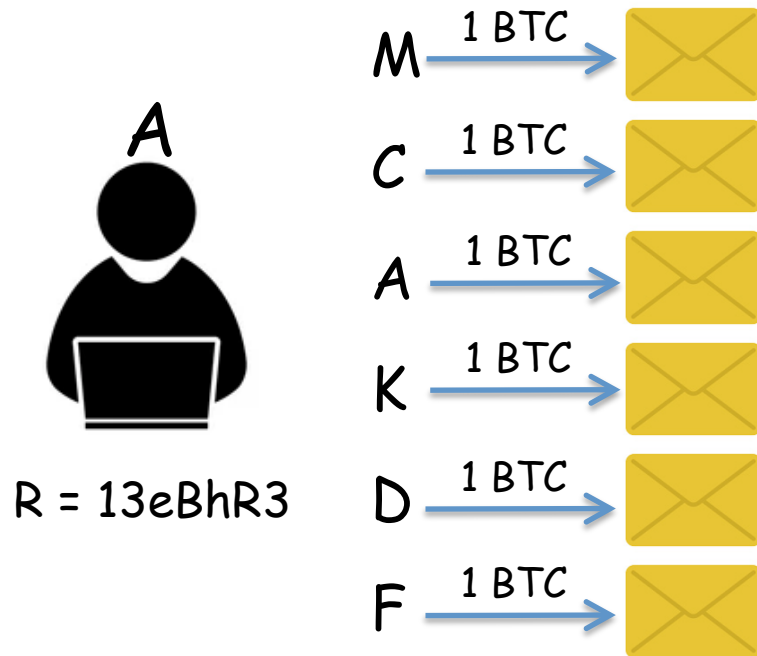
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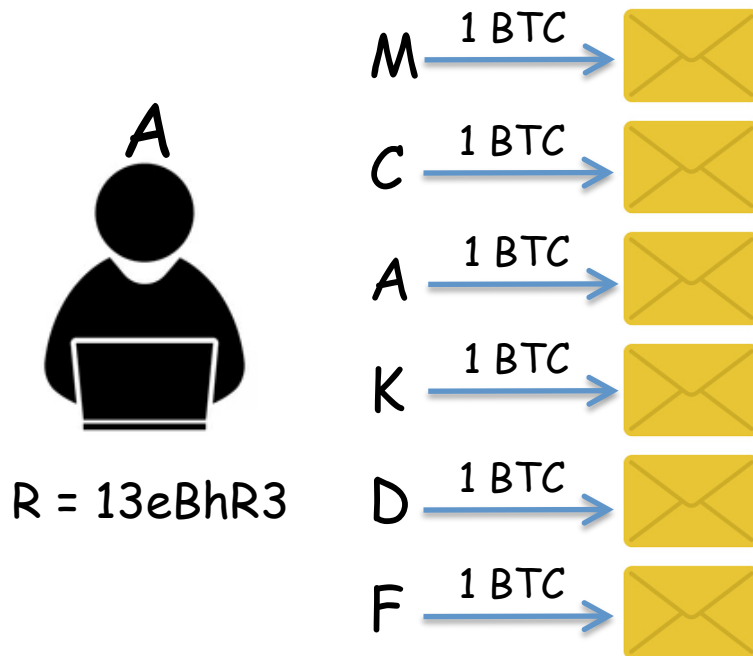
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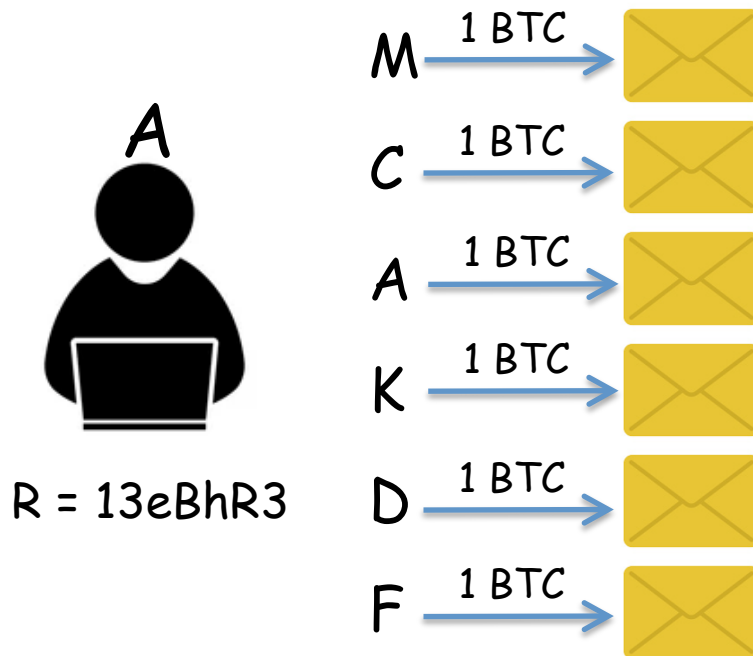


- $R$ , proof

proof shows that one of the unclaimed zerocoins contains the serial number  $R$

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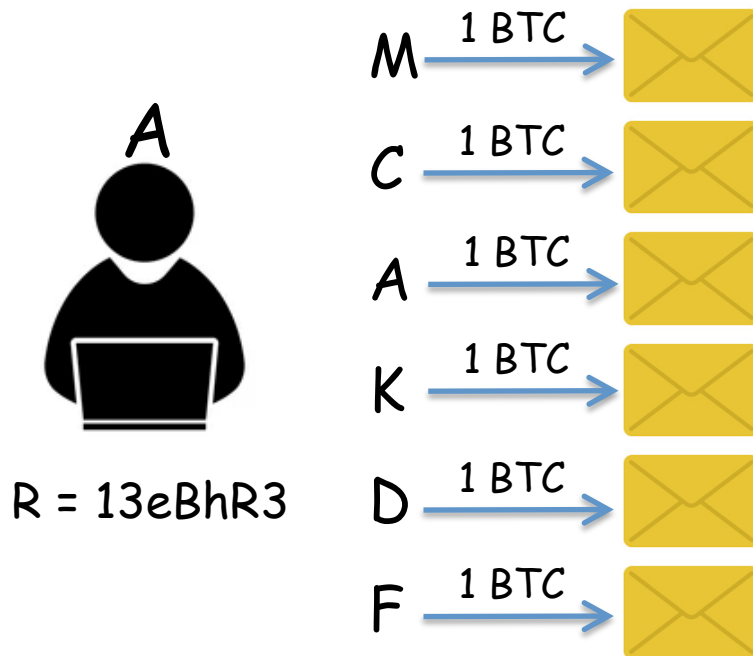
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- R, proof
- proof shows that one of the unclaimed zerocoins contains the serial number R
- prover A tries to convince verifier (whole network) that one of the commitments contains R without revealing which one exactly containing R
  - 'zero knowledge' prevents one to link this transaction to a specific address

# Privacy Enhancing Techniques

Privacy vs Accountability

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## Privacy vs Accountability

- attractive tools for criminals to perform illegal activities
- introducing serious concerns for regulatory authorities
- Singapore exchange Bittrue hacked in June 2019, over \$4 million stolen

"Bittrue working with Houbi, Bittrex to freeze stolen cryptocurrencies and accounts associated with the hack"



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## Privacy vs Accountability

- attractive tools for criminals to perform illegal activities
- introducing serious concerns for regulatory authorities
- Singapore exchange Bittrue hacked in June 2019, over \$4 million stolen
  - "Bittrue working with Houbi, Bittrex to freeze stolen cryptocurrencies and accounts associated with the hack"
- Japan exchange Liquid hacked in August 2021, over \$97 million stolen
  - "stolen funds converted to Ether using Uniswap and Sushiswap, then Ether laundered through Tornado Cash"

# References

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