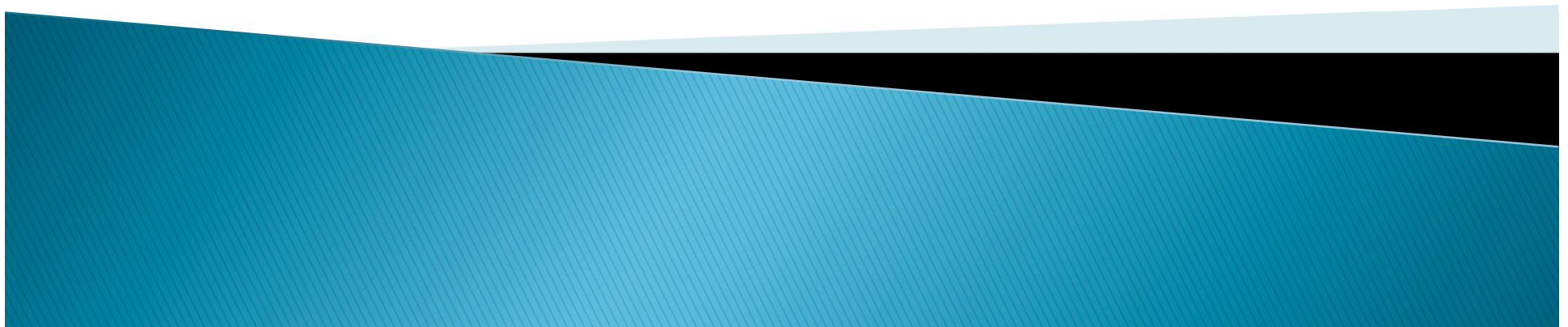


# FDE 205 FLUID MECHANICS



# OVERALL MOMENTUM BALANCE

- ▶ A momentum balance is similar to the overall mass balance.
- ▶ Momentum is a vector quantity.
- ▶ The total linear momentum vector (P) of the total mass (M) of a moving fluid having a velocity of  $v$  is

$$P = Mv$$

The unit of momentum is  $\text{kg}\cdot\text{m}/\text{s}$



# OVERALL MOMENTUM BALANCE

- ▶ Newton's second law:

The time rate of change of momentum of a system is equal to the summation of all forces acting on the system and takes place in the direction of the net force.

$$\underbrace{\sum F}_{\text{Force (N)}} = \frac{dP}{dt}$$

Force (N)



- ▶ The equation for the conservation of the momentum with respect to a control volume can be written as follows:

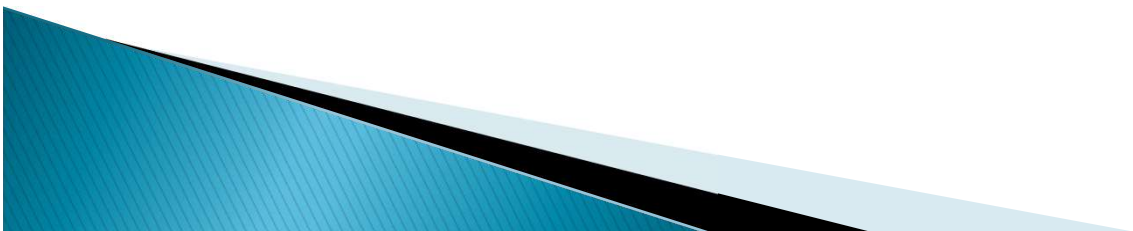
Sum of forces acting on control volume =  
Rate of momentum out of control volume -  
Rate of momentum into control volume +  
Rate of accumulation of momentum in control  
volume

We should note that  $\Sigma F$  in general may have a component in any direction (x, y, z), and that F is the force the surroundings exert on the control volume fluid.



# Overall Momentum Balance in Flow Systems in One Direction:

- ▶  $\Sigma F_x$  = sum of forces only in x direction
- ▶ 1. Body force: The body force ( $F_{xg}$ ) is the x-directed force caused by gravity acting on the total mass  $M$  in the control volume. It is zero if the x direction is horizontal.
- ▶ 2. Pressure force: The force ( $F_{xp}$ ) is the x-directed force caused by the pressure forces acting on the surface of the fluid system.

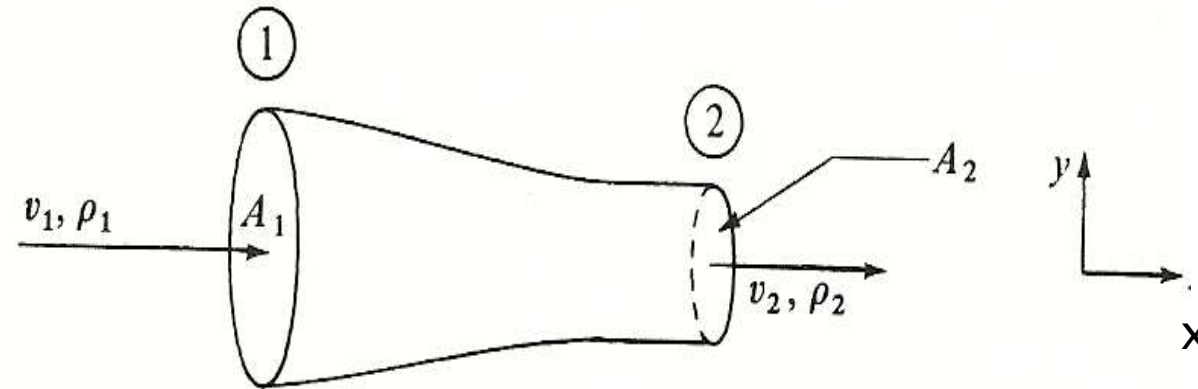


# Overall Momentum Balance in Flow Systems in One Direction:

- ▶ 3. Friction force: When the fluid is flowing, and  $x$ -directed friction force ( $F_{x_s}$ ) is present. In many cases, this frictional force may be negligible compared to the other forces.
- ▶ 4. Solid Surface force: ( $R_x$ ) This is the force exerted by the solid surface on the fluid. Typically occurs when the control volume includes a section of pipe and the fluid it contains.



# Overall Momentum Balance in Flow Systems in One Direction:



$$\sum F_x = \frac{\dot{m} v_2}{\beta} - \frac{\dot{m} v_1}{\beta}$$

# Overall Momentum Balance in Flow Systems in One Direction:

$$F_{xg} + F_{xp} + F_{xs} + R_x = \frac{\dot{m}v_2}{\beta} - \frac{\dot{m}v_1}{\beta}$$

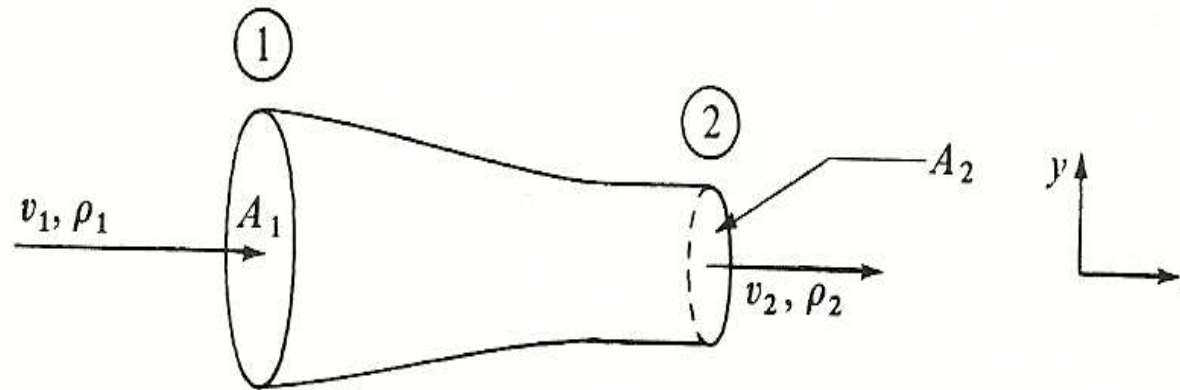
- ▶ If the flow is turbulent
- ▶ Frictional losses are negligible

$$R_x = \dot{m}v_2 - \dot{m}v_1 + P_2A_2 - P_1A_1$$



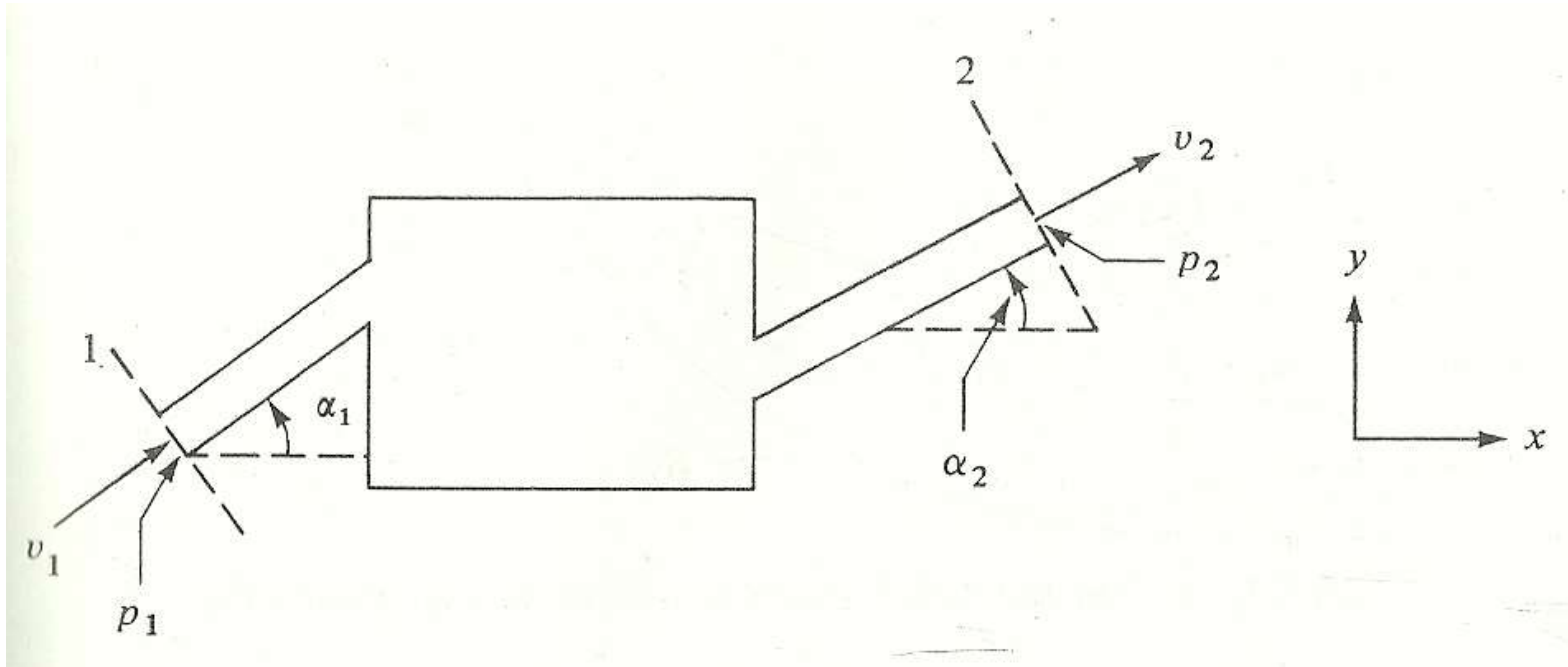


## Example 2.8-2



- ▶ Water is flowing at a rate of  $0.03154 \text{ m}^3/\text{s}$  through a horizontal nozzle shown in the figure above and discharges to the atmosphere at point 2. The nozzle is attached at the upstream end at point 1 and frictional forces are considered negligible. The upstream ID is  $0.0635 \text{ m}$  and the downstream  $0.0286 \text{ m}$ . Calculate the resultant force on the nozzle. The density of the water is  $1000 \text{ kg}/\text{m}^3$ .

# Overall Momentum Balance in Two Direction:

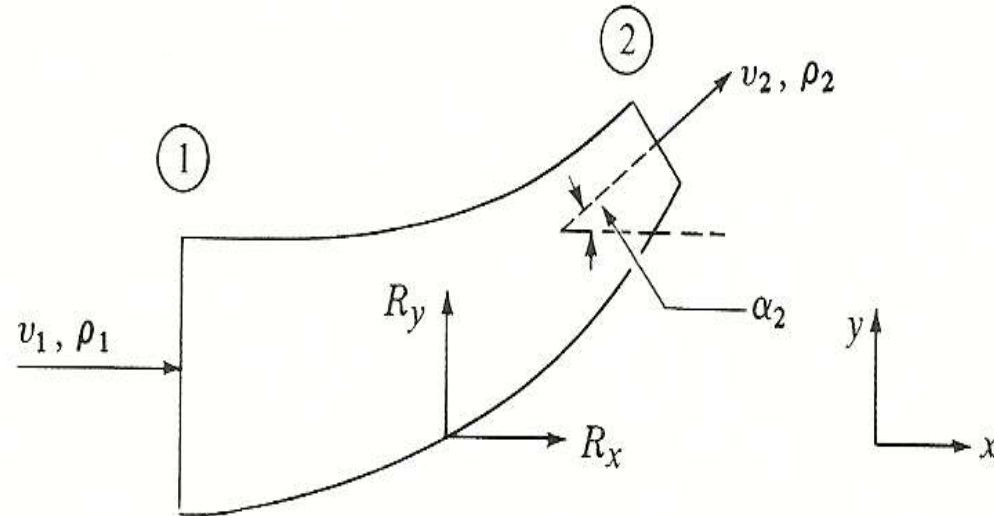


$$R_x = \dot{m} v_2 \cos \alpha_2 - \dot{m} v_1 \cos \alpha_1 + P_2 A_2 \cos \alpha_2 - P_1 A_1 \cos \alpha_1$$

$$R_y = \dot{m} v_2 \sin \alpha_2 - \dot{m} v_1 \sin \alpha_1 + P_2 A_2 \sin \alpha_2 - P_1 A_1 \sin \alpha_1 + M_t g$$

$$|R| = \sqrt{(R_x^2 + R_y^2)}$$

# Example 2.8.3



- ▶ Fluid is flowing at steady state through a reducing pipe bend. Turbulent flow will be assumed with frictional forces negligible. The volumetric flow rate of the liquid and the pressure  $p_2$  at point 2 are known, as are the pipe diameters at both ends. Derive the equations to calculate the forces on the bend. Assume that The density( $\rho$ ) is constant.