

PID Control Parameters

- If the PID control constants are not selected properly, the control system may even drive your system to instability.

$$\theta_o = K_c \left[\theta_e + \frac{1}{\tau_I} \int_0^t \theta_e dt + \tau_D \frac{d\theta_e}{dt} \right]$$

Integral time constant

Derivative time constant

The methods used for calculation of optimum values of PID parameters are;

- TRIAL AND ERROR
- COHEN-COON METHOD
- YUWANA- SEBORG METHOD
- ZIEGLER-NICHOLS METHOD

Cohen-coon method is the oldest and the most commonly applied one. So we will focus on its application;

COHEN-COON METHOD

- Valid only for first order processes.

$$G_1(s) = \frac{K}{\tau s + 1}$$

- If time delay or dead time is also taken into consideration with a transfer function of ;

$$G_2(s) = e^{-\tau_{dead} s}$$

- The transfer function of the process can be rewritten as;

$$G_{process}(s) = \frac{K \times e^{-\tau_{dead}s}}{\tau s + 1}$$

- I. The steady state values of the process are obtained.
- II. The control system is cutout.
- III. A step input with a known magnitude is applied to manipulated variable.
- IV. The controlled variable is waited to reach the new steady state value.
- V. The graph of the response of the process vs time is drawn.

- A tangent is drawn to the curve at its maximum ascent point. The point where the tangent crosses the x-axis is named as dead time (τ_{dead}).
- The slope of the tangent is given as $m = M_u / \tau$
- M_u is the final steady state value of the output variable
- τ is the time constant of the system.
- K (gain): can be calculated by using the following equation; $K = M_u / X_0$

where, M_u is the difference between second steady state value and the first steady state value of the controlled variable, X_0 is the magnitude of the step input.

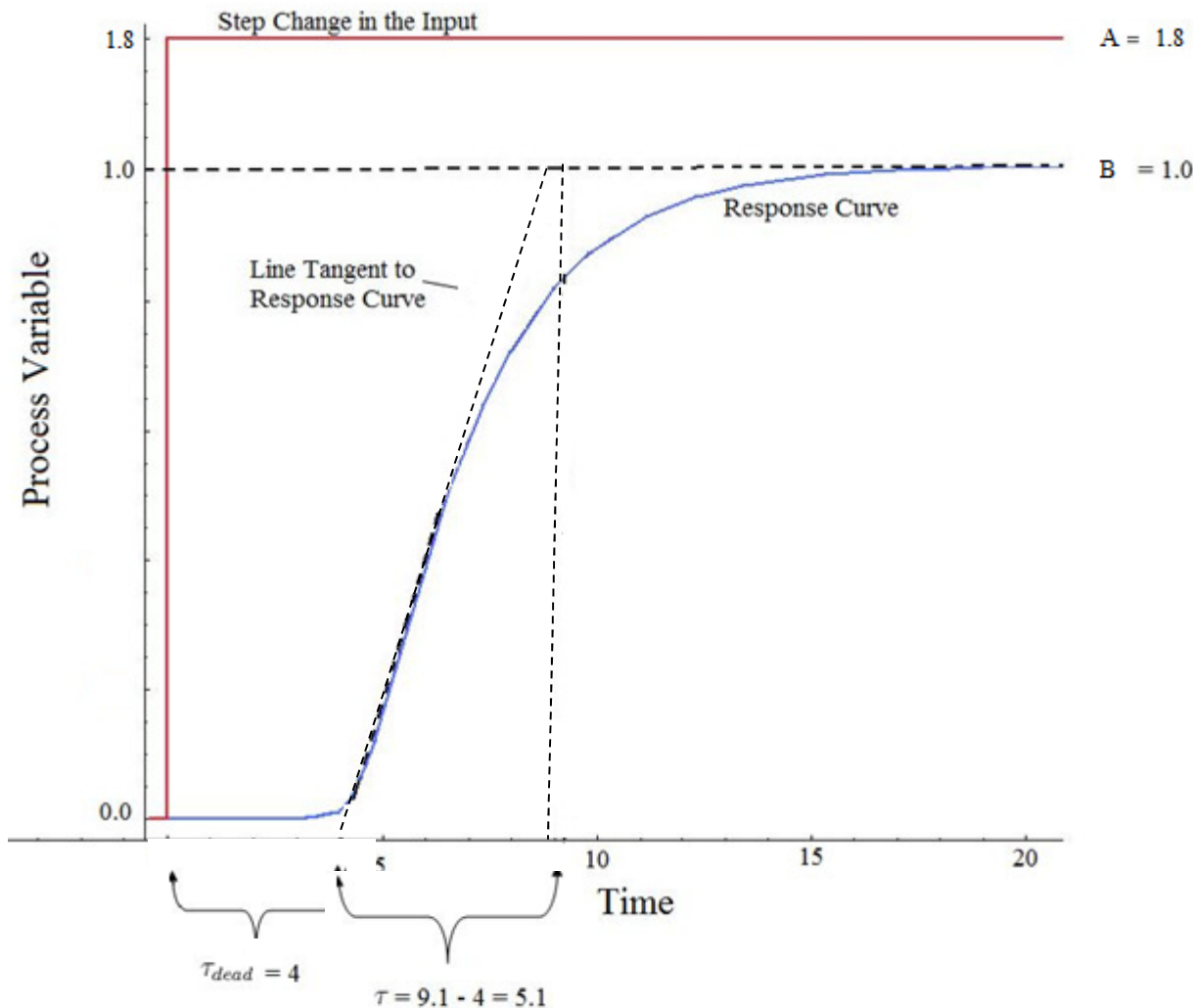
The equations used to calculate the optimum control parameters;

$$K_c = \frac{1}{K} - \frac{\tau}{\tau_{dead}} - \left[\frac{4}{3} \times \frac{\tau}{4\tau_{dead}} \right]$$

$$\tau_{Integral} = \left[\frac{32 + 6 \left(\frac{\tau_{dead}}{\tau} \right)}{13 + 8 \left(\frac{\tau_{dead}}{\tau} \right)} \right] \times \tau_{dead}$$

$$\tau_{Derivative} = \tau_{dead} \left[\frac{4}{11 + 2 \left(\frac{\tau_{dead}}{\tau} \right)} \right]$$

Example:



The graph of process variables versus time (t) is given in the figure;

- Calculate the dead time, K (gain), and τ (time constant) values and write the transfer function of the system.
- Write down the transfer function of a PID control system applied to this process.