7.WEEK

**CHE 212 FLUID MECHANICS** 

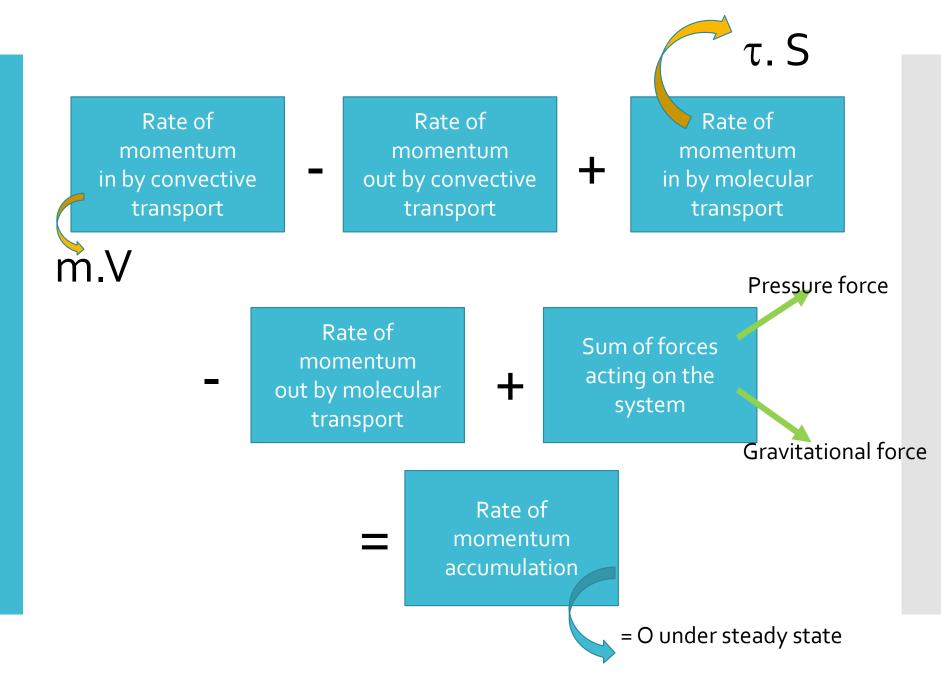
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 SHELL MOMENTUM BALANCES and VELOCITY DISTRIBUTIONS IN LAMINAR FLOW

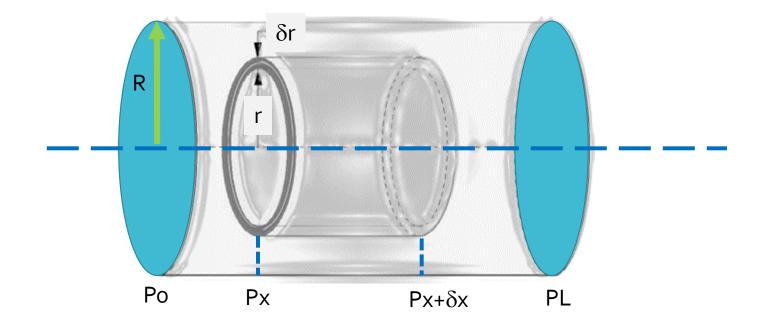
In order to obtain a velocity profile in flow systems, a momentum balance shall be made on a volume element, in which momentum enters and leaves the system by;

- a. Convection: from flow of the bulk fluid
- b. Molecular transport: as a result of velocity gradients (viscous action)



- In order to set up and solve viscous problems
- a. A momentum balance over a thin shell should be written.
- b. The differential equation for the momentum flux should be written.
- c. Newton's Law of Viscosity should be inserted to obtain a differential equation for the velocity
- d. This equation should be solved by using boundary conditions.

- Boundary conditions are statements about the velocity or stress at the boundaries of the system. The most commonly used boundary conditions are:
- a. At solid-liquid interface, te velocity of the fluid equals the velocity of the solid surface tangential to the fluid.
- At liquid-liquid interface, momentum transport nad velocity perpendicular to the interface is constant.
- c. At gas-liquid interface momentum transport is taken to be zero.



#### Assumptions:

- a. One-dimensional laminar flow
- b. Newtonian fluid
- c. End-effects are ignored
- d. Steady-state

Total momentum balance equation:

• 
$$\tau r x$$
.  $2\pi r \Delta x \Big|_{r} - \tau r x$ .  $2\pi r \Delta x \Big|_{r+\Delta r} + \rho V_{x}^{2}$ .  $2\pi r \Delta r \Big|_{x} \rho V_{x}^{2}$ .  $2\pi r \Delta r \Big|_{x+\Delta x} + \rho V_{x}^{2}$ 

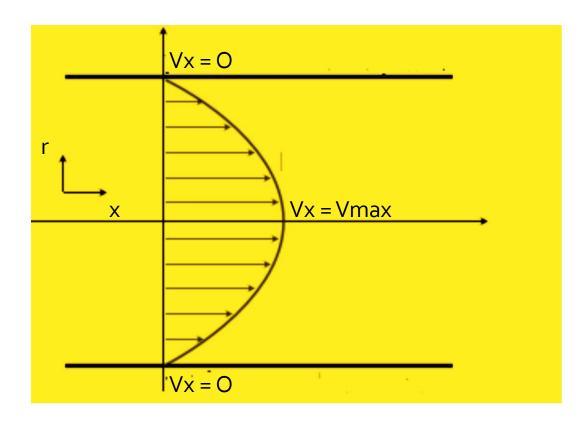
$$P2\pi r\Delta r | - P2\pi r\Delta r | = 0$$

$$\times \Delta r | \Delta r = 0$$

$$Vx = \frac{\Delta P}{\mu L} \frac{r^2}{4} + c1 \ln r + C2$$

Boundary conditions are:

• 
$$Vx = \frac{(Po - PL)}{4\mu L}$$
.  $R^2(1 - (\frac{r}{R})^2)$ 



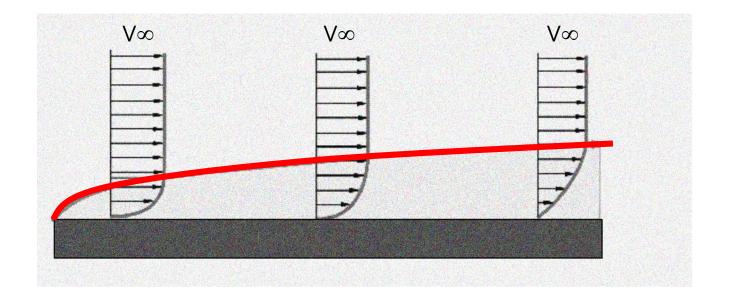
HAGEN-POISEUILLE EQUATION;

$$Vx = \frac{(Po - PL)D^2}{32 \,\mu L}$$

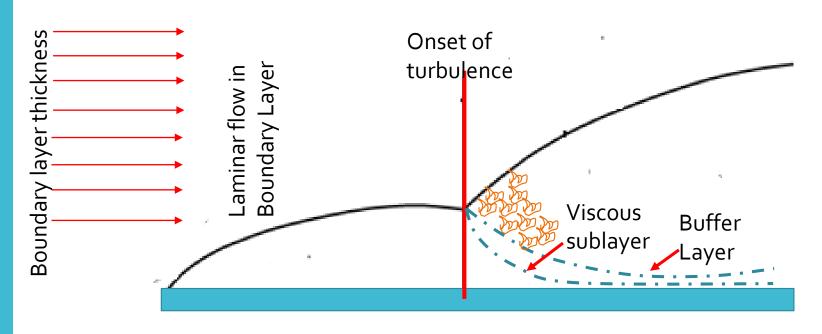
gives the pressure drop because of friction in laminar flow through a horizontal pipe. One of its uses is in the experimental measurement of viscosity

## BOUNDARY LAYERS

 A Boundary Layer is defined as that part of a moving fluid in which the fluid motion is influenced by the presence of a solid boundary.



# BOUNDARY LAYERS



Distance from the leading edge