

# ELE 321

# Linear System Analysis

Ankara University

Faculty of Engineering

Electrical and Electronics Engineering Department

# Transformations of the Independent Variable

ELE321 Linear System Analysis

Lecture 2

# Agenda

- Independent variable
- Transformation of independent variable
- Time shifting
- Time reversal
- Time scaling

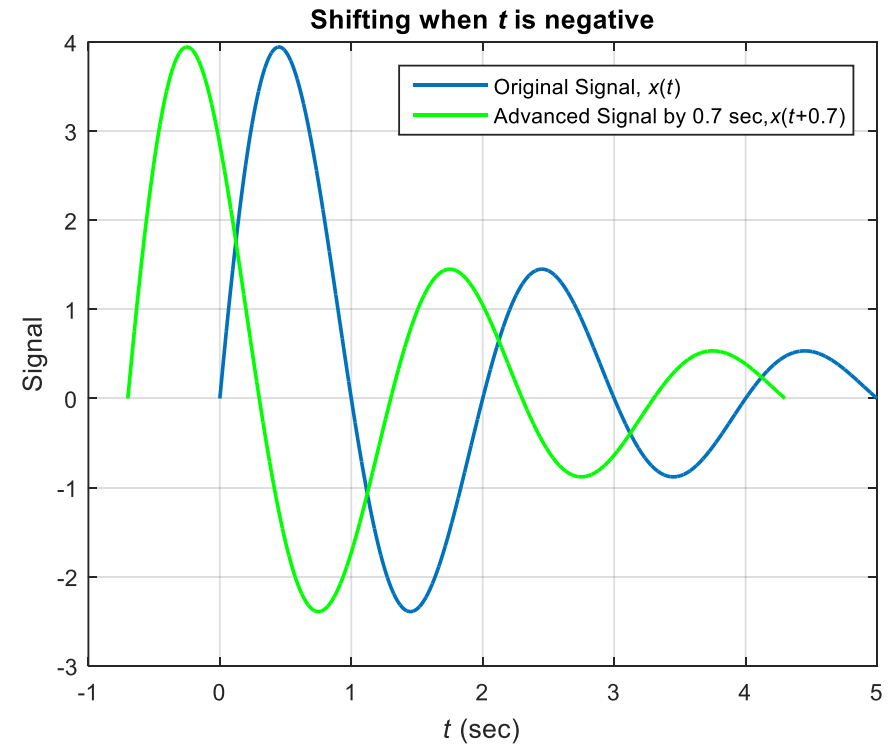
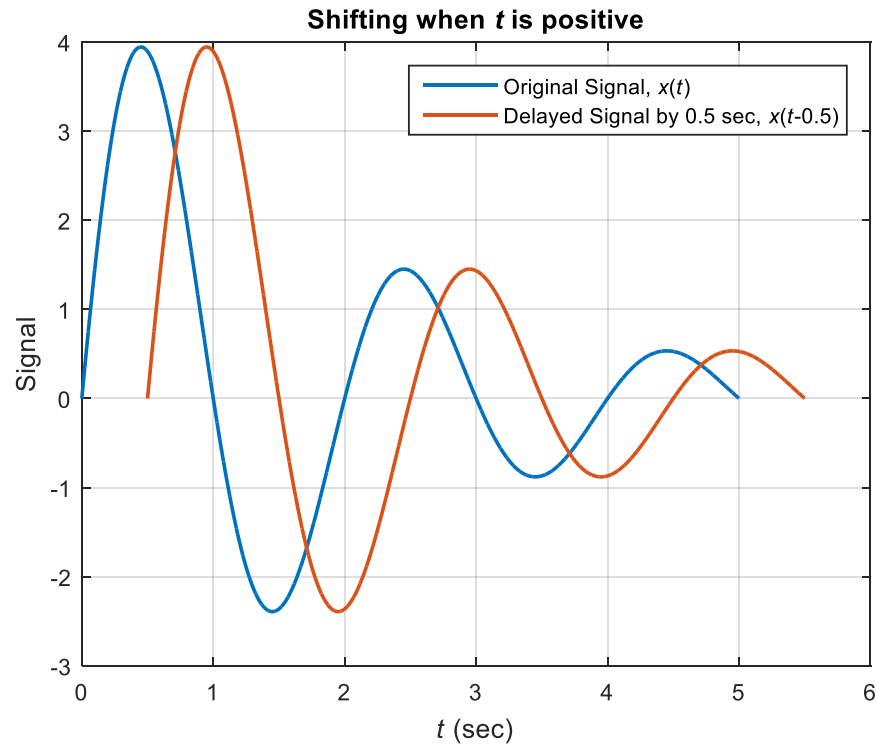
## Transformations of the Independent Variable

(Modifications of the independent variable, time)

- **Time shift:**  $x(t) \rightarrow x(t-t_0)$ ,  $t_0$  can be (+) or (-).  
 $x[n] \rightarrow x[n-n_0]$ ,  $n_0$  can be (+) or (-).
  - If  $t_0$  is positive,  $x(t-t_0)$  is delayed version of the original signal  $x(t)$ .
  - If  $t_0$  is negative,  $x(t-t_0)$  is advanced version of the original signal  $x(t)$ .
  - **Time reversal:**  $x(-t)$  (Reflection at  $t=0$ ).
  - **Time scaling:**  $x(at)$ ,  $a$ : constant
  - If  $a > 1$ ,  $x(at)$  is speeded up signal.
  - If  $a < 1$ ,  $x(at)$  is slowed down signal.
- \* All operations are applicable to discrete-time signals as well.

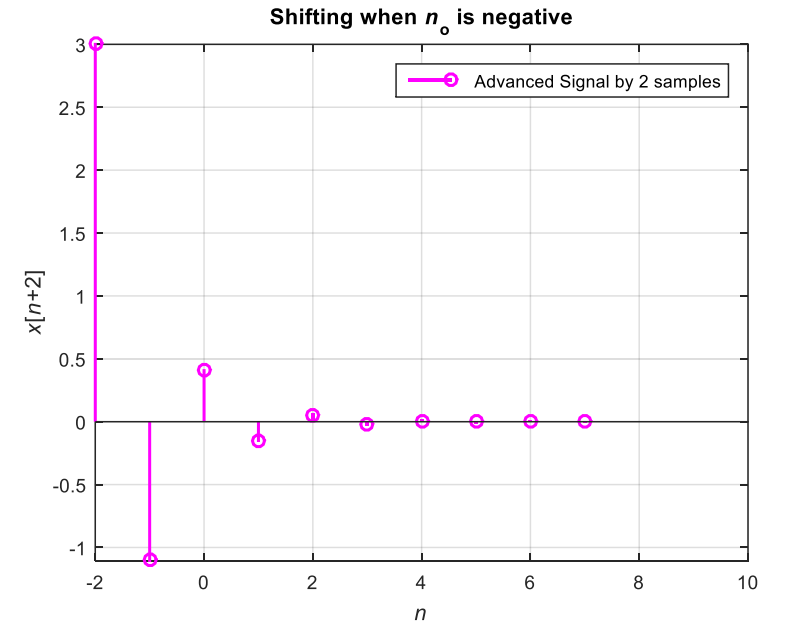
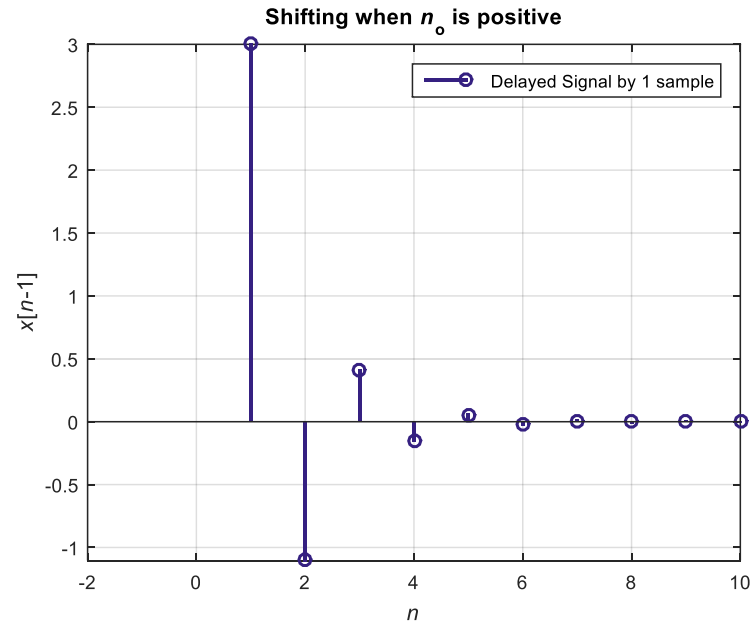
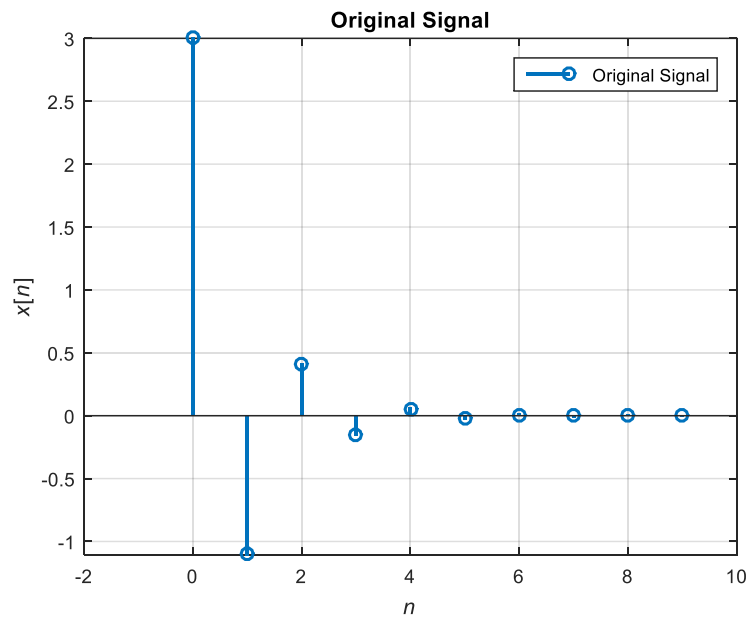
# Time Shifting

- Continuous time example



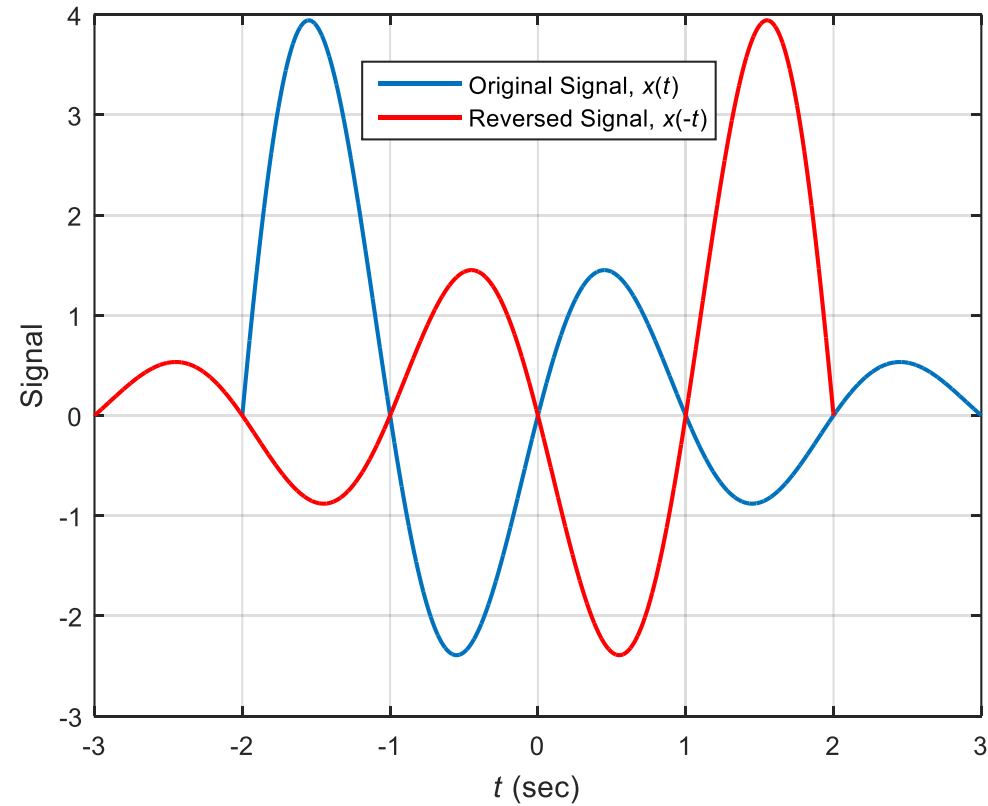
# Time Shifting

- Discrete time example



# Time Reversal

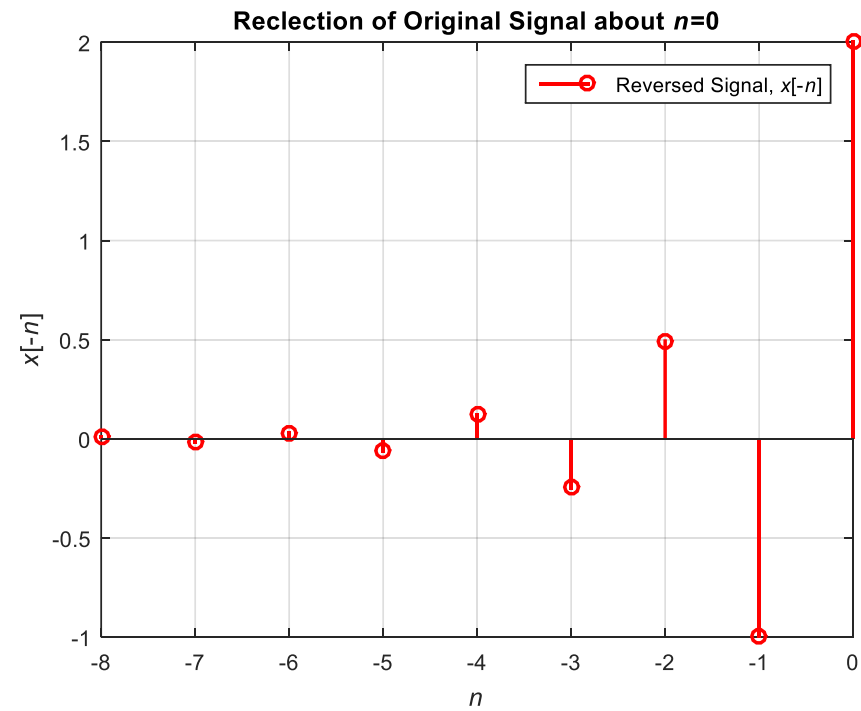
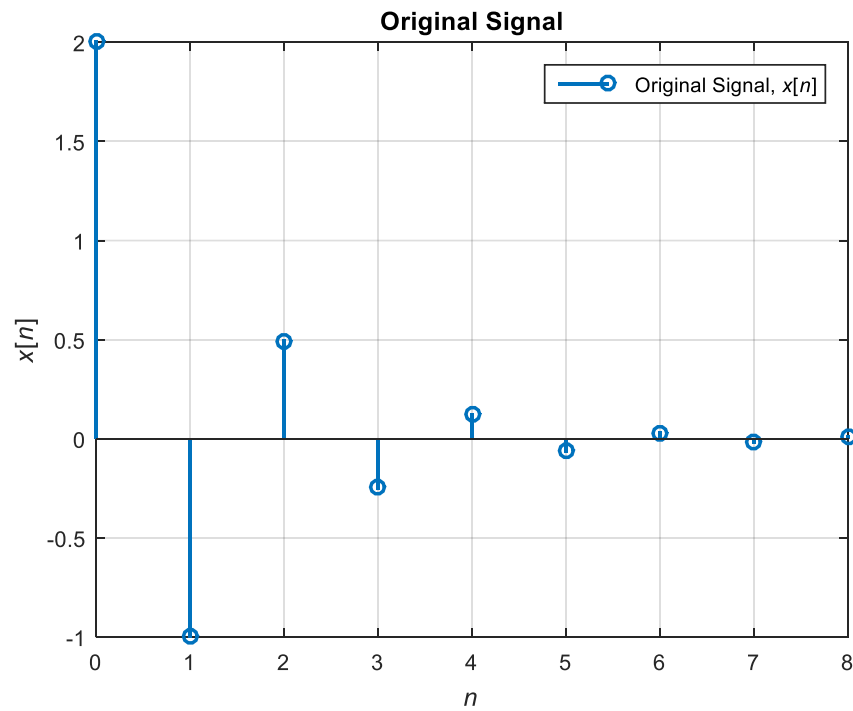
- Continuous time example



$x(-t)$  is obtained from the signal  $x(t)$  by a reflection about  $t=0$ .

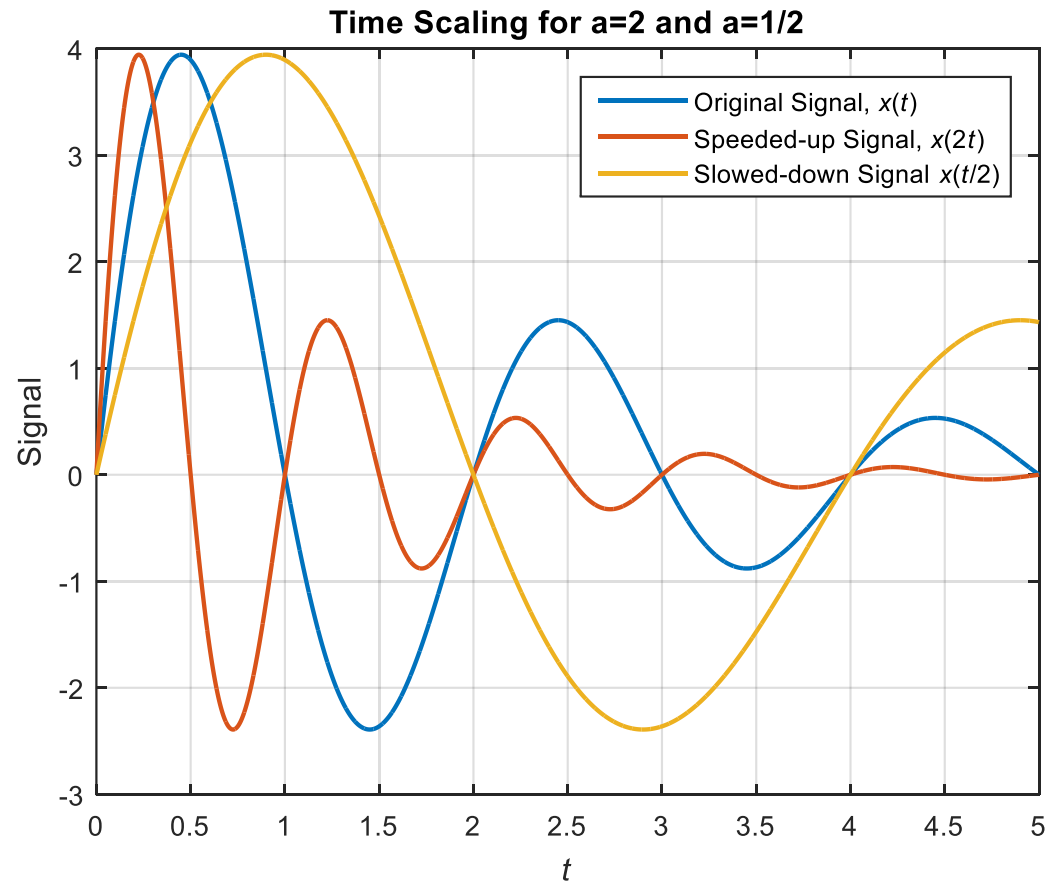
# Time Reversal

- Discrete time example

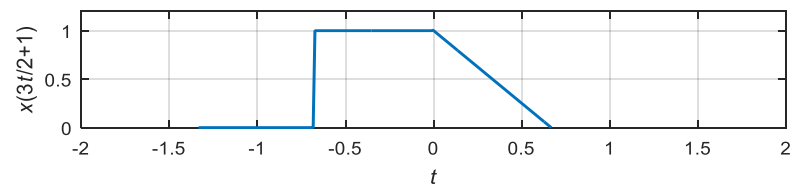
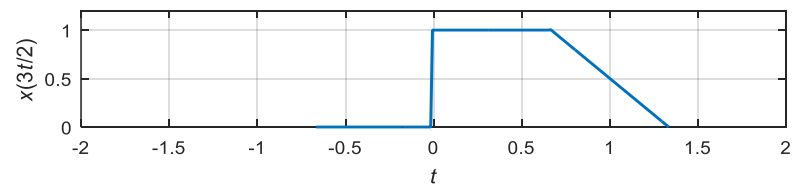
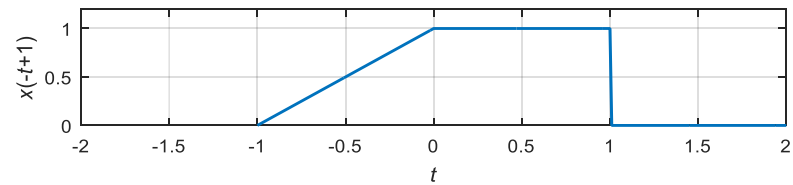
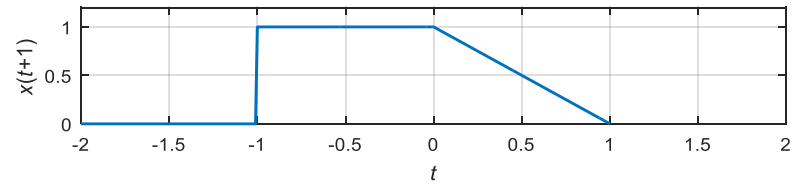
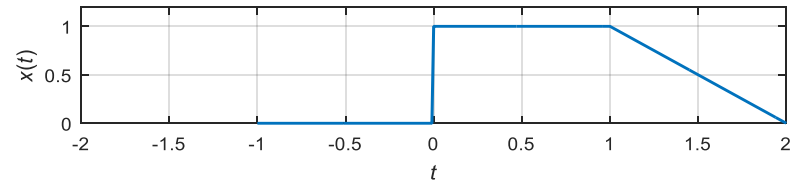




# Time Scaling



# Example \*



\* Example 1.1. Signals and Systems, A.V. Oppenheim, A. S. Willsky with S. H. Nawab

# References

- Signals and Systems, 2nd Edition, Oppenheim, Willsky, Nawab