$x \rightarrow \infty$ means that x gets larger and larger without a bound.

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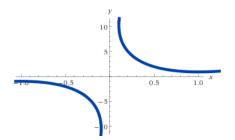
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 $x \to \infty$ means that x gets larger and larger without a bound. $x \to -\infty$ means that x gets smaller and smaller without a bound.

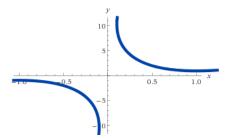
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 $\lim_{x \to \infty} \frac{1}{x} = 0 = \lim_{x \to -\infty} \frac{1}{x}.$ Note that for a positive number *k*,

$$\lim_{x\to\infty}\frac{1}{x^k}=0=\lim_{x\to-\infty}\frac{1}{x^k}.$$

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For f(x) a real function, the limit of f as x approaches infinity is L, denoted

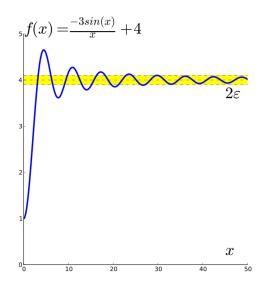
$$\lim_{x\to\infty}f(x)=L,$$

means that for all $\varepsilon > 0$, there exists c such that $|f(x) - L| < \varepsilon$ whenever x > c. Similarly, the limit of f as x approaches negative infinity is L, denoted

$$\lim_{x\to-\infty}f(x)=L,$$

means that for all $\varepsilon > 0$ there exists c such that $|f(x) - L| < \varepsilon$ whenever x < c. For example

$$\lim_{x\to -\infty} e^x = 0.$$



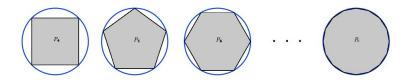
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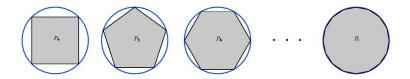
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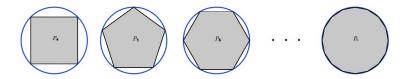
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Let f(n) be the area of the *n*-gon inscribed in a circle of radius *r*.



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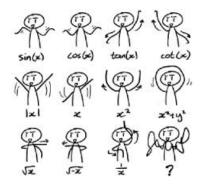
Math Dance Moves

Oktay Olmez and Serhan Varma

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Math Dance Moves



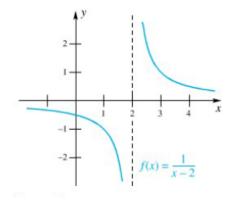
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Oktay Olmez and Serhan Varma

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 $\lim_{x\to c^+} f(x) = \infty$ means that f(x) can be made as large as we wish by taking x sufficiently close but to the right of c.

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 $\lim_{x\to c^-} f(x) = -\infty$ means that f(x) can be made as small as we wish by

taking x sufficiently close but to the left of c.

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Vertical and Horizontal Asymptotes

Definition

Line x = c is a vertical asymptote of the graph of y = f(x). If any of the following is satisfied:

- $\lim_{x\to c^+} f(x) = \infty$
- $\lim_{x\to c^+} f(x) = -\infty$
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Definition

Line y = b is a horizontal asymptote of the graph of y = f(x). If any of the following is satisfied:

•
$$\lim_{x\to\infty} f(x) = b$$

•
$$\lim_{x \to -\infty} f(x) = b$$

Oktay Olmez and Serhan Varma