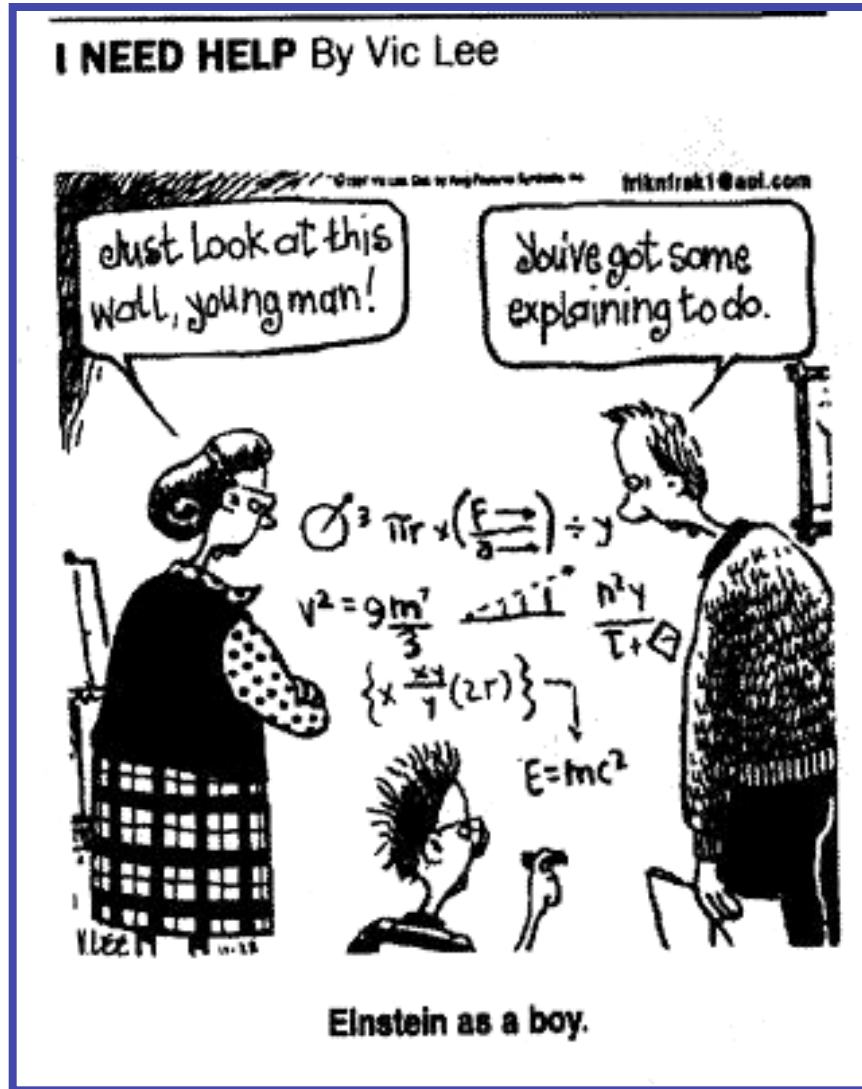


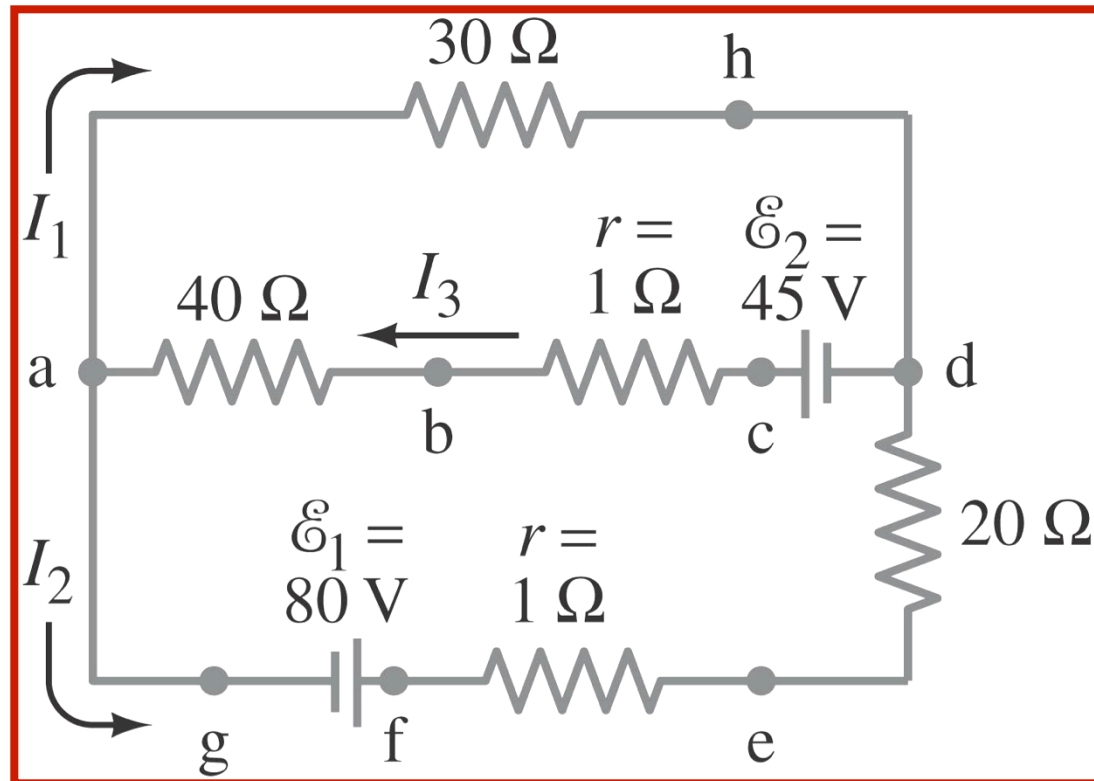
Kirchhoff's Rules



Kirchhoff's Rules

- Some circuits cannot be broken down into series & parallel connections. For these circuits we use

Kirchhoff's Rules.



Kirchhoff's Rules:

Their Underlying Physics

1. Kirchhoff's Junction Rule (First Rule):

At a junction point, the sum of all currents entering the junction equals the sum of all currents leaving it.

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The sum of the changes in Electric Potential : V around any closed loop in a circuit is zero.

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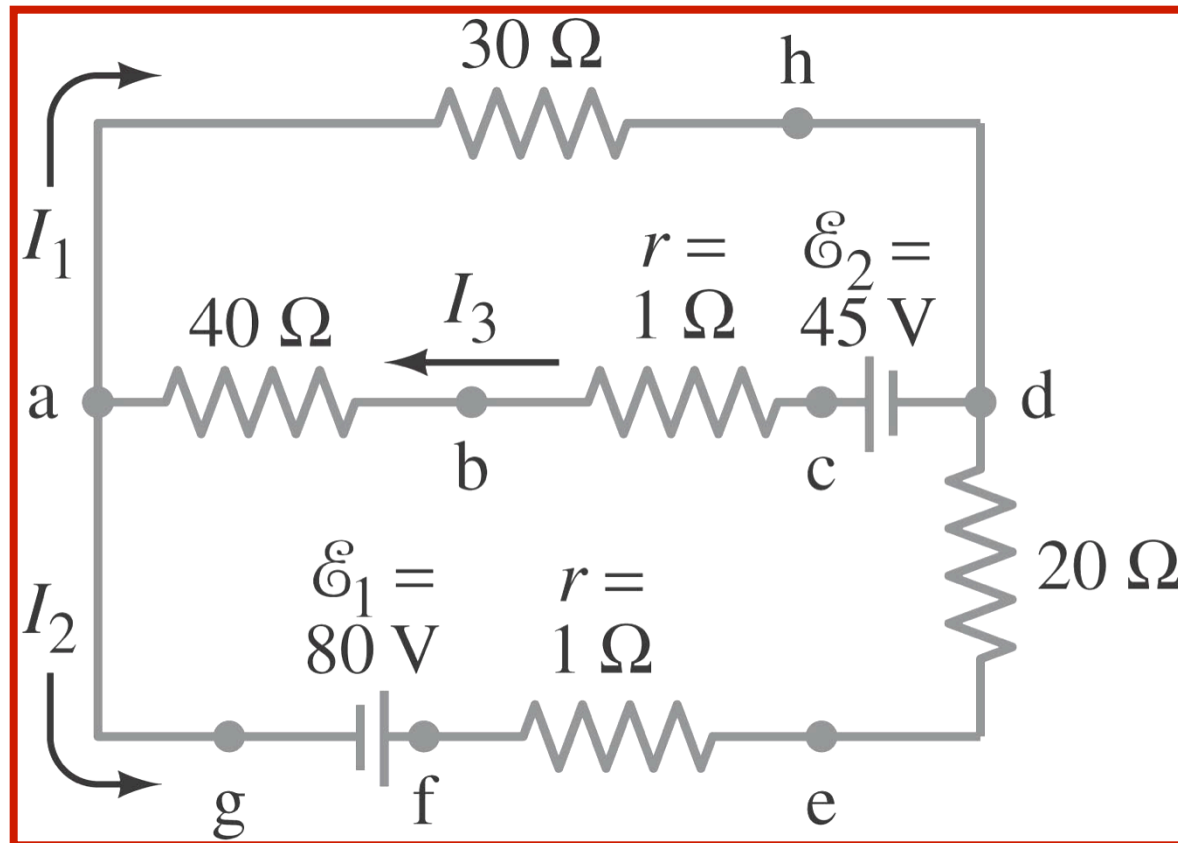
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The sum of the changes in Electric Potential : V around any closed loop in a circuit is zero.

Physics: Conservation of Energy in the Circuit.

Kirchhoff's Junction Rule

- The sum of the currents entering a junction equals the sum of the currents leaving it.



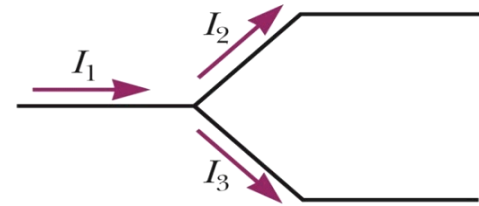
Kirchhoff's Junction Rule

The sum of currents entering a junction equals the sum of the currents leaving it.

- Currents directed into the junction are entered into the equation as **+I** and those leaving as **-I**.
- This is analogous to water flowing in pipes at a junction.

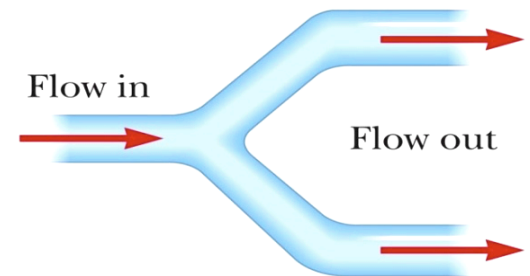
See figure.

The amount of charge flowing out of the branches on the right must equal the amount flowing into the single branch on the left.



a

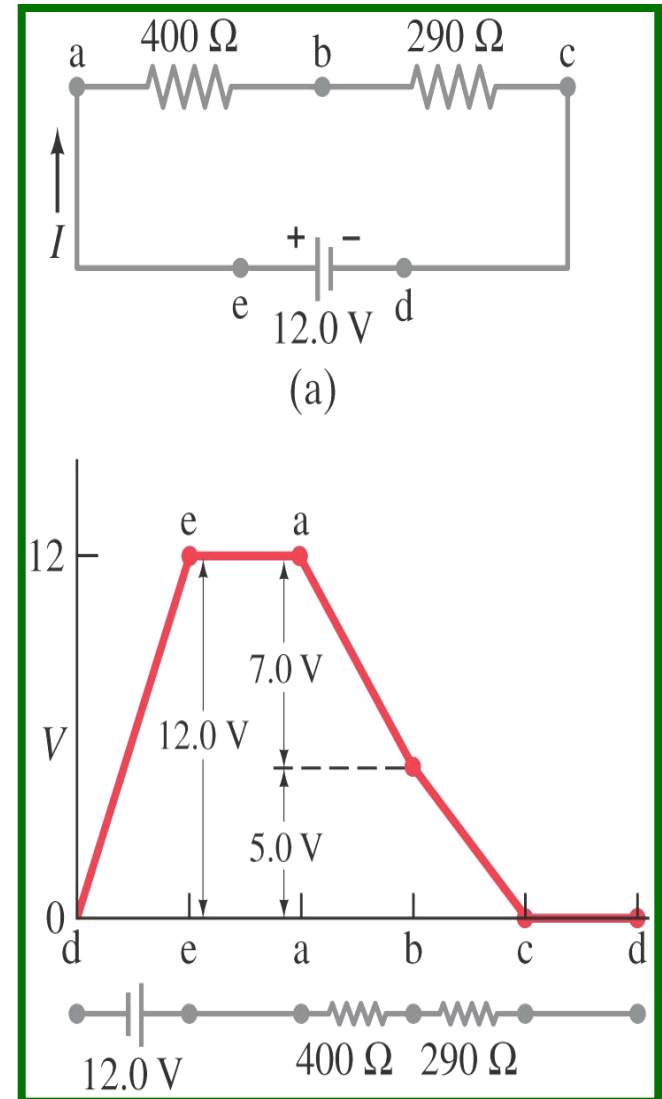
The amount of water flowing out of the branches on the right must equal the amount flowing into the single branch on the left.



b

Kirchhoff's Loop Rule

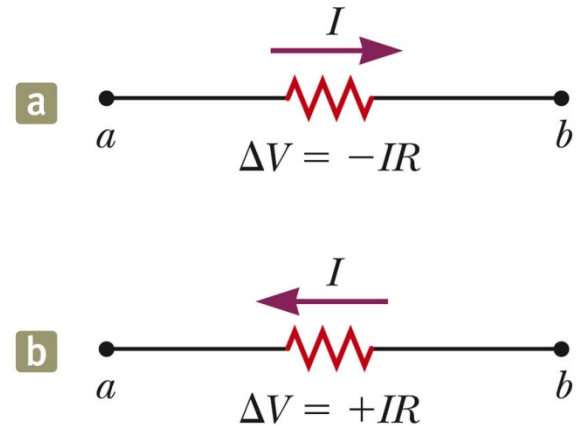
The sum of the
changes in Electric
Potential ΔV
around
any closed loop in a
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Kirchhoff's Loop Rule

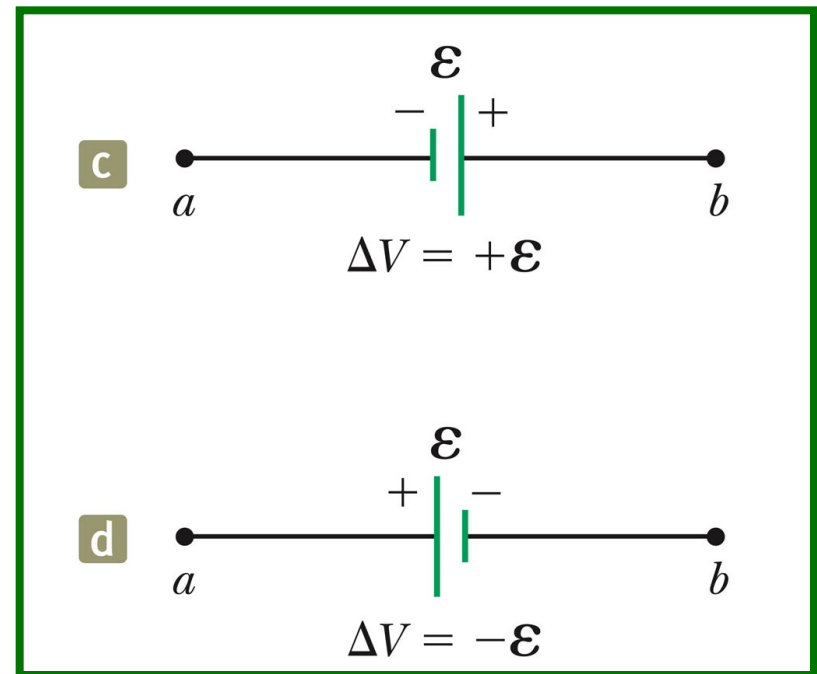
- Traveling around the loop from a to b:
- In **(a)**, the resistor is traversed in the direction of the current, the potential across the resistor is **$-IR$** .
- In **(b)**, the resistor is traversed in the direction opposite of the current, the potential across the resistor is **$+IR$** .

In each diagram, $\Delta V = V_b - V_a$ and the circuit element is traversed from a to b , left to right.



Kirchhoff's Loop Rule

- In **(c)**, the source of emf is traversed in the direction of the emf (from $-$ to $+$), and the change in the potential difference is $+\epsilon$.
- In **(d)**, the source of emf is traversed in the direction opposite of the emf (from $+$ to $-$), and the change in the potential difference is $-\epsilon$.



Problem Solving: Kirchhoff's Rules

1. Label each current, including its direction.
2. Identify unknowns.
3. Apply the Junction & Loop Rules:
 - The number of independent equations needed is equal to the number of unknowns in the problem.
4. Solve the Equations, with

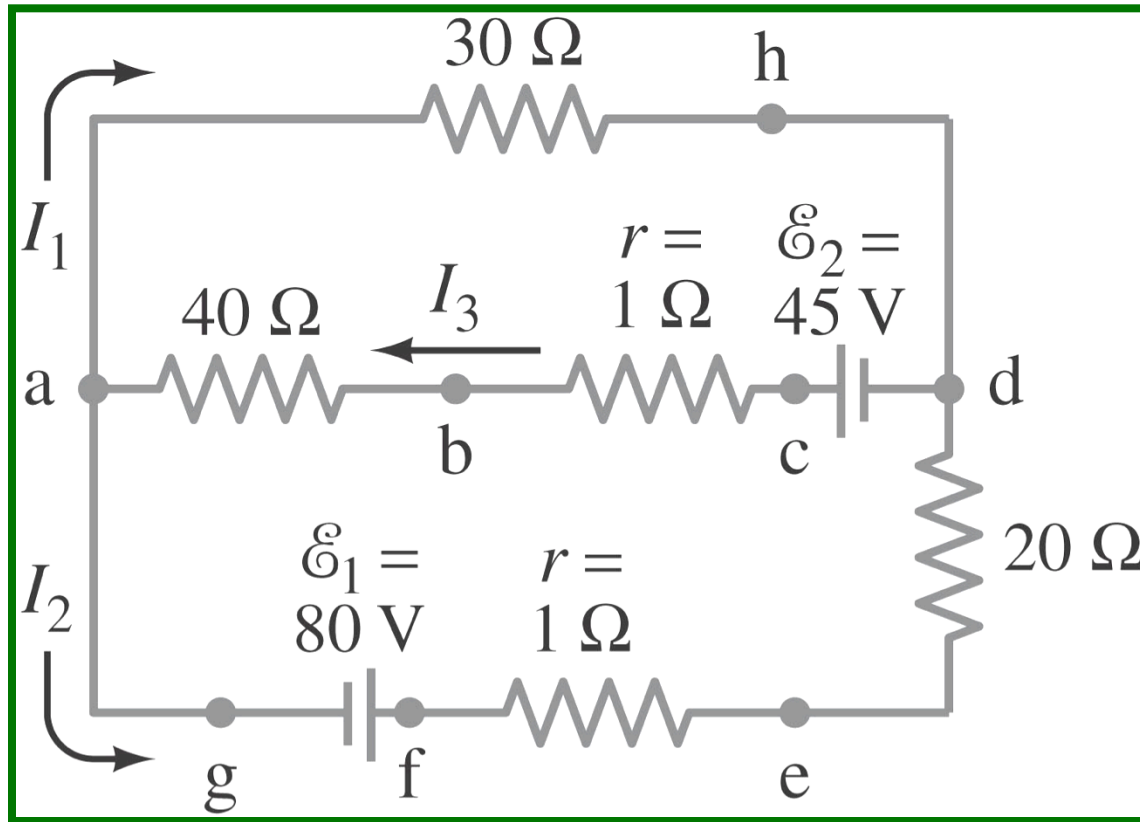
Careful Algebra!!!!

Be careful with signs!!!

- If the solution for a current is negative, that current is in the opposite direction from the one you have chosen.

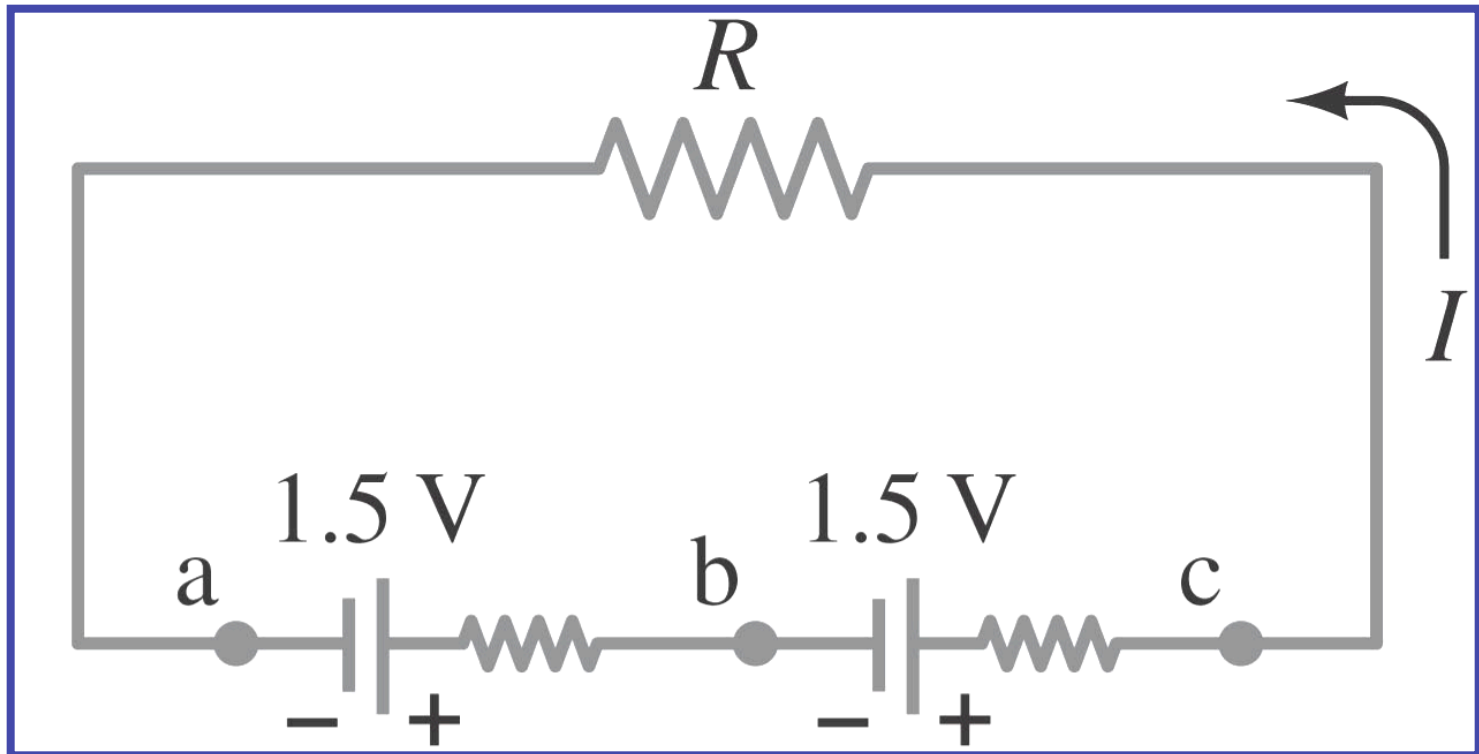
Example: Using Kirchhoff's rules.

Calculate the currents I_1 , I_2 , and I_3 in the three branches of the circuit in the figure.

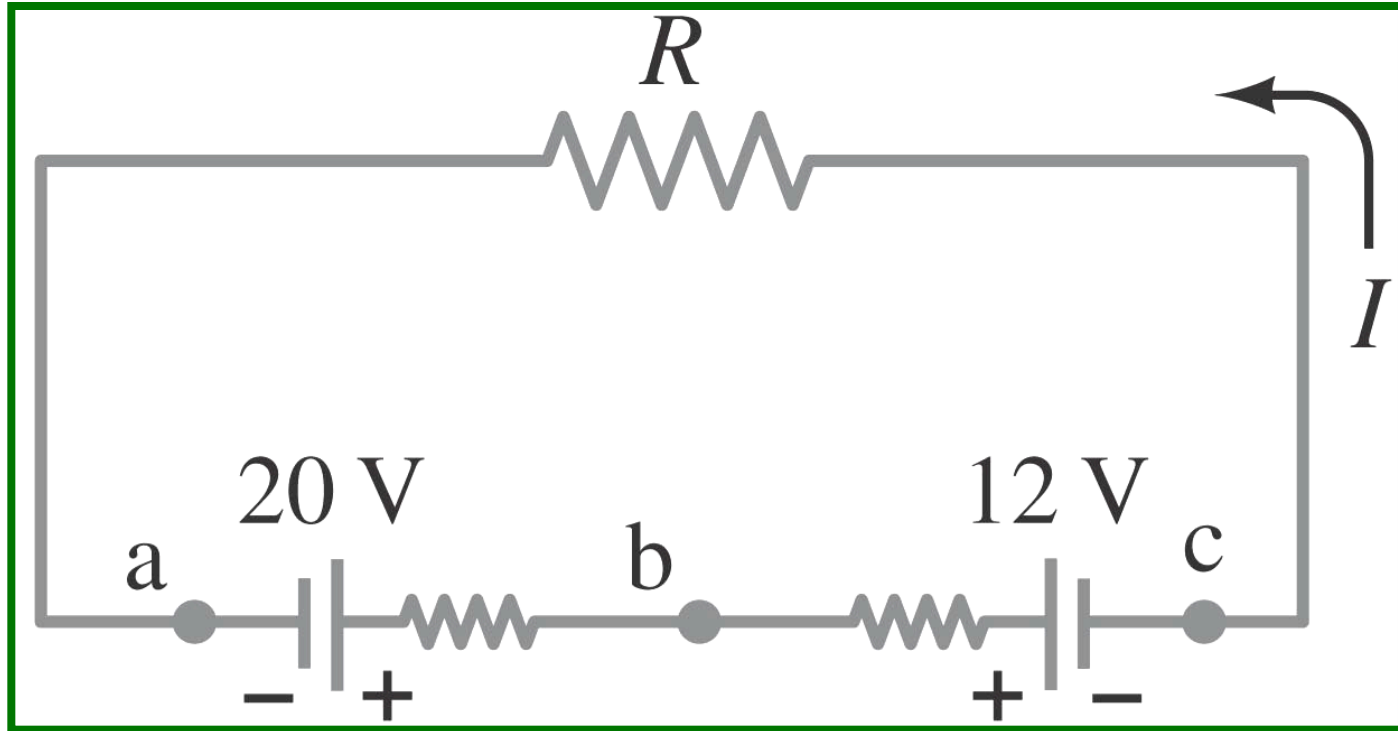


Series & Parallel EMFs; Battery Charging

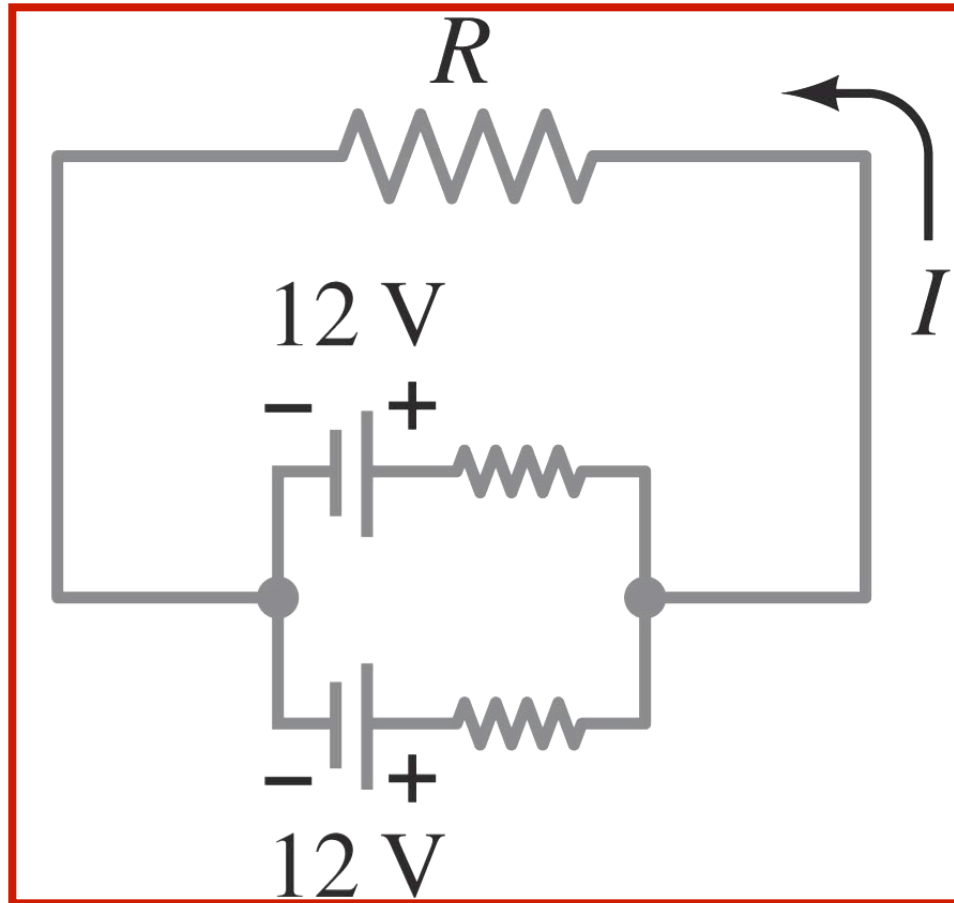
For **two or more EMFs in series** in the same direction, **the total voltage is the sum of the separate voltages.**



For **two EMFs in series** in the opposite direction, the total voltage is their difference. In addition, the lower-voltage battery will be charged by the higher voltage battery.



Two EMFs in Parallel only make sense if the voltages are the same. This arrangement can produce more current than a single emf.



Example: Jump starting a car.

A good car battery is being used to jump start a car with a weak battery. The good battery has an emf of $\mathcal{E}_1 = 12.5 \text{ V}$ & internal resistance $r_1 = 0.020 \ \Omega$. Suppose that the weak battery has an emf of $\mathcal{E}_2 = 10.1 \text{ V}$ and internal resistance $r_2 = 0.10 \ \Omega$. Each copper jumper cable is 3.0 m long and 0.50 cm in diameter, and can be attached as shown. Assume that the starter motor can be represented as a resistor $R_s = 0.15 \ \Omega$. Calculate the current through the starter motor:

- (a) if only the weak battery is connected to it,
- (b) if the good battery is also connected.

