

## Lecture 13 :

**Radiation reaction :** While an accelerated charged particle radiates, as a consequence of this emission it loses kinetic energy at the same time. Radiation thus exerts a recoil force on the particle.

### a) Abraham-Lorentz formula for the radiation reaction force.

Power =  $P = \mathbf{F} \cdot \mathbf{v}$  in general. Replacing the Larmor formula (with a minus sign in front because energy is being lost) and integrating over time one can obtain

$$\text{radiation reaction force } \mathbf{F}_{rad} = \frac{\mu_0 q^2}{6\pi c} \dot{\mathbf{a}}$$

### b) Runaway solutions

Writing Newton's second law as  $\mathbf{F}_{rad} = m\mathbf{a}$ , this immediately gives exponentially increasing solutions :

$$a(t) = a_0 e^{t/\tau} \text{ where } \tau = \frac{\mu_0 q^2}{6\pi mc} . \quad \text{For an electron } \tau \approx 10^{-24} \text{ s} !$$

### c) Physical basis of the radiation reaction

Radiation reaction is due to force exerted by the fields generated by different parts of the charge distribution; so it is a self force. See the textbook D.Griffiths Int. to Electrodynamics. See also "F. Rohrlich, The self-force and radiation reaction, American Journal of Physics 68, 1109 (2000); "Jacques D. Templin, An approximate method for the direct calculation of radiation reaction, American Journal of Physics 66, 403 (1998); Abraham-Lorentz versus Landau-Lifshitz, David J. Griffiths, Thomas C. Proctor, and Darrell F. Schroeter American Journal of Physics 78, 391 (2010)

Homework :

Solve the following problems from the textbook D.Griffiths' "Int. to Electrodynamics"

Solve Problem 11.22

Solve Problem 11.29

Solve Problem 11.31