

Principles of unit conversion


- **Dimensional equation**: Equation containing numerical value and its unit
- For example; $10 \text{ BTU}/(\text{h ft } ^\circ\text{F}) = 56.78 \text{ W/m } ^\circ\text{C}$ is an dimensional equation.
- Whatever the mathematical procedure is applied to the numerical value in dimensional equation, the same procedure is applied to the units in dimensional equation.


During unit conversion


- Prepare an equation
- In the equation, the followings should occur:
 - Conversion factor
 - the unit of final answer
 - the unit being converted
 - conversion units
- Calculate the **conversion factor** from the equation

Steps in conversion of units

- Place the units of the final answer on the left-hand side of the equation and the unit being converted on the right hand side of equation.
- Do **not** add the numerical value of the unit being converted to the equation.
- Then, put an **equal sign** between two expression.

- 
- **Conversion units** are found from **conversion tables** for the units to be converted in the right hand side of equation.
 - Set up the **conversion units** as a **ratio**, using Appendix Table 1.
 - Sequentially multiply the conversion factors such that the original units are systematically eliminated by cancellation replacement with the desired unit.

- 
- **After cancellation of units** in the right hand side of equation, appropriate **conversion factor** is calculated.
 - The numerical value in front of the unit converted is now taken into consideration. This **numerical value is put on both side of equation.**



Example 1: Covert thermal conductivity in English Engineering System (10 BTU/(h ft °F)) to **SI unit** system.

Result:

$$CF = 1.73$$

$$10 \text{ BTU}/(\text{h ft } ^\circ\text{F}) = 17.3 \text{ J}/(\text{m s K})$$

Example 2: Specific heat of orange juice concentrate with 45% water soluble solid content is $c_p = 0.64 \text{ BTU/lb}_m \text{ } ^\circ\text{F}$. Express this value in **SI unit** system.

Result:

$$CF = 4186.5$$

$$0.64 \text{ BTU/ lb}_m \text{ } ^\circ\text{F} = 2679.4 \text{ J/kg K}$$

Example 3: Heat transfer coefficient of salami at 21°C is $h_s = 210 \text{ BTU/ft}^2 \text{ h } ^\circ\text{F}$. Express this value in **SI unit** system.

Result:

$$CF = 5.6780$$


$$210 \text{ BTU/ h ft}^2 \text{ }^\circ\text{F} = 1192.4 \text{ J/m}^2 \text{ s K}$$

Example 4: The density of cow milk is 64.5 lb_m/ft^3 . Express this value in **SI unit** system.

Result:


$$CF = 16.02$$

$$64.5 \text{ lb}_m/\text{ft}^3 = 1033.3 \text{ kg/m}^3$$



Example 6: For a fluid passing through a pipe, type of flow (laminar, turbulent) depends on the pressure (ρV^2) and viscosity forces ($\mu V/D$) of fluid. And, the ratio of these values gives Reynold number (RN). RN is used to determine the type of flow. If RN is:

- below 2300, the flow is laminar,
- above 4000, the flow is turbulent,
- In between 2300-4000, the flow is transition (mixed).


$$\text{Re} = \frac{\rho V^2}{\mu V/D} = \frac{\rho V D}{\mu}$$

where;

D : diameter of the pipe in which the liquid flows, m,


V : velocity, m/s,

ρ : density, kg/m³,

μ : viscosity, kg/m s.

In a milk processing plant, the type of flow of milk is found to be turbulent ($Re=50000$). The velocity (V) of milk flowing in a diameter (D) of 1 in. of a pipe is 13.5 ft/s and the density (ρ) at 294 K is $64.3 \text{ lb}_m/\text{ft}^3$. **Wall thickness of the pipe is 0.1 in.** Determine the viscosity (μ) of milk at 294 K in:


- SI unit system,
- cgs unit system.

- 
- **Example 7 :** A tube is filled with a fruit juice with the height of h cm and density of ρ . The pressure exerted to the base of the tube by this fruit juice is P atmosphere. Calculate the density of fluid in the SI system.


Answer: $1 \times 10^6 \text{ kg/m}^3$

- **Example 8:** In a milk processing plant, once the milk is brought to the plant, first, the milk is placed in a pre-storage tank and then centrifuged to remove somatic cells, leucosits, blood coagulates and some microorganisms (clarification process). During this clarification process, the milk is pumped to the centrifuge which is 5 m higher than the storage tank at a velocity of 120 kg/min. During transportation, the friction loss in pipes is 45 J/kg and calculate the necessary power of pump is “SI” unit system.

Answer: 188.1 W

- 
- **Example 9:** The heat loss through the walls of an electrical oven is 6500 BTU/h. If the oven is operated for 2 h, how many kilowatt-hours of electricity will be used just to maintain the oven temperature (heat input = heat loss)?

Answer: 3.8 kW h


- 
- **Example 10:** The height of a pomegranate juice with a density of 1.068 g/cm^3 in a tube is 8.325 in. Calculate the pressure applied by pomegranate juice in the SI system.

Answer: $2215.1 \text{ kg}/(\text{m s}^2) \text{ (Pa)}$

Lenght units in English engineering sytem


- 1 in = 2.54 cm
- 1 foot = 12 in
- 3 feet = 1 yard
- 3.28 feet = 1 m






Volume units in English engineering sytem


- 1 gal = 3.79 L
- 1 gal = 4 quarts
- 1 quart = 2 pints
- 1 pint = 16 fluid ounce (fl oz)
- 1 quart = 32 fluid ounce


- 
- **Example 11:** Calculate your height in “feet” and “in.” (173 cm)

Answer: 5'8''

- 
- **Example:** Calculate the area of rectangular with the measurement of $2' 5''^{1/16}$ and $5' 9''^{3/32}$ in SI unit system.

Answer: 2.1 m^2

- 
- **Example 12:** Calculate the volume of a car tank with the capacity of 40 L in “gallons” and “pints.”

- 
- **Example 15:** Express the viscosity values given below as the unit asked.

Viscosity is the resistance of fluids to movement.

Viscosity = Pressure x time

Viscosity is expressed as:

$$\text{cgs} \rightarrow \frac{\text{g}}{\text{cm s}} = \text{poise}$$

$$\text{SI} \rightarrow \frac{\text{kg}}{\text{m s}}$$

$$\text{EES} \rightarrow \frac{\text{lb}_m}{\text{ft s}}$$



a) Express 20 cp in “Pa s.”

b) Express 15 cp in “EES.”

c) Express “30 lb_m/(ft h)” in “SI” unit system.

Answers

a) $20 \text{ cp} = 0.02 \text{ Pa s}$


b) $15 \text{ cp} = 0.01 \text{ lb}_m/(\text{ft s})$

c) $30 \text{ lb}_m/(\text{ft h}) = 0.0124 \text{ kg}/(\text{m s})$

- **Example 16:** Pressure is expressed in the SI system in Pascals. Calculate the English equivalent of 8 Pa.
($lbf = 4.44823 \text{ N}$)

Answer:

$$8 \text{ Pa} = 0.00116 \frac{\text{lb}_f}{\text{in}^2}$$

- 
- **Example 17:** Calculate the power in (SI system) required for peach nectar which flows down the raceway of a reservoir at a rate of $525 \text{ lb}_m/\text{min}$ from a height of 12.3 ft.



Answer: 146 W