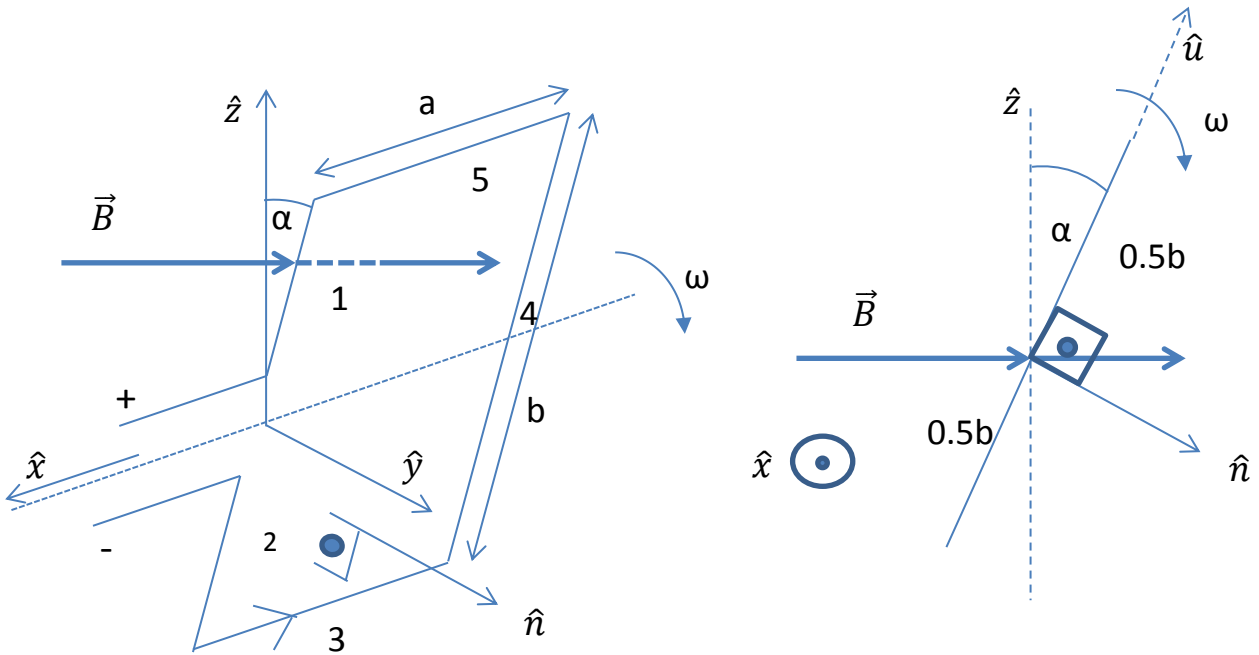


Total EMF	$\Phi = -\frac{d}{dt} \left(\int \vec{B} \cdot d\vec{S} \right)$	
	Assume $\vec{B} = B_0 \cos(\omega t) \hat{y}$	
	$\vec{B} \cdot d\vec{S} = \cos(\alpha) \cdot B_0 \cos(\omega t) \cdot dS$	
	$\Phi = -\frac{d}{dt} \left(\int \cos(\alpha) \cdot B_0 \cos(\omega t) \cdot dS \right)$	
	$\Phi = -\frac{d}{dt} \left(\cos(\alpha) \cdot B_0 \cos(\omega t) \int dS \right)$	
	$S = ab$	
	$\alpha = \omega t$	
	$\frac{d\alpha}{dt} = \omega$	
	$\Phi = -\frac{d}{dt} (\cos(\alpha) \cdot B_0 \cos(\omega t) S)$	
	$\Phi = - \left(-\sin(\alpha) \frac{d\alpha}{dt} B_0 \cos(\omega t) S + \cos(\alpha) \cdot B_0 (-\sin(\omega t) \omega) S \right)$	
	$\Phi = \sin(\alpha) \omega B_0 \cos(\omega t) S + \cos(\alpha) \cdot B_0 \sin(\omega t) \omega S$	
	$\Phi = 2\omega B S_0 \sin(\omega t) \cos(\omega t)$	
	$\Phi = \omega B S_0 \sin(2\omega t) \text{ (volts)}$	

Total EMF	$\Phi = -\frac{d}{dt} \left(\int \vec{B} \cdot d\vec{S} \right) = - \left(\int \frac{d\vec{B}}{dt} \cdot d\vec{S} \right) + \oint \vec{v} \times \vec{B} \cdot d\vec{l}$	
Transformer EMF	$\Phi_{Transformer} = - \left(\int \frac{d\vec{B}}{dt} \cdot d\vec{S} \right)$	
	$\Phi_{Transformer} = - \left(\int \frac{d(B_0 \cos(\omega t) \hat{y})}{dt} \cdot d\vec{S} \right)$	
	$\Phi_{Transformer} = - \left(\int -\omega B_0 \sin(\omega t) \hat{y} \cdot d\vec{S} \right)$	
	$\hat{y} \cdot d\vec{S} = \cos(\alpha) dS$	
	$\Phi_{Transformer} = - \left(\int -\omega B_0 \sin(\omega t) \cos(\alpha) dS \right)$	
	$\Phi_{Transformer} = \int \omega B_0 \sin(\omega t) \cos(\alpha) dS$	
	$\Phi_{Transformer} = \omega B_0 \sin(\omega t) \cos(\alpha) \int dS$	
	$S=ab$	
	$\Phi_{Transformer} = \omega B_0 \sin(\omega t) \cos(\alpha) S$	
Total EMF	$\Phi = -\frac{d}{dt} \left(\int \vec{B} \cdot d\vec{S} \right) = - \left(\int \frac{d\vec{B}}{dt} \cdot d\vec{S} \right) + \oint \vec{v} \times \vec{B} \cdot d\vec{l}$	
Motional EMF	$\Phi_{motional} = \oint \vec{v} \times \vec{B} \cdot d\vec{l}$	



1:	$u: 0.5b \rightarrow 0$	$\vec{dl} = du \hat{u}$
2:	$u: 0 \rightarrow -0.5b$	$\vec{dl} = du \hat{u}$
3:	$x: 0.5a \rightarrow -0.5a$	$\vec{dl} = dx \hat{x}$
4:	$u: -0.5b \rightarrow 0.5b$	$\vec{dl} = du \hat{u}$
5:	$x: -0.5a \rightarrow 0.5a$	$\vec{dl} = dx \hat{x}$
1:	$\vec{v} = \omega(u)(\hat{n})$	
2:	$\vec{v} = \omega(-u)(-\hat{n})$	
3:	$\vec{v} = \omega(-0.5b)(-\hat{n})$	
4:	$\vec{v} = \omega(u)(\hat{n})$	
5:	$\vec{v} = \omega(0.5b)(\hat{n})$	

1:	$\vec{v} \times \vec{B} = \omega(u)(\hat{n}) \times B_0 \cos(\omega t) \hat{y}$	
2:	$\vec{v} \times \vec{B} = \omega(-u)(-\hat{n}) \times B_0 \cos(\omega t) \hat{y}$	
3:	$\vec{v} \times \vec{B} = \omega(0.5b)(-\hat{n}) \times B_0 \cos(\omega t) \hat{y}$	
4:	$\vec{v} \times \vec{B} = \omega(u)(\hat{n}) \times B_0 \cos(\omega t) \hat{y}$	
5:	$\vec{v} \times \vec{B} = \omega(0.5b)(\hat{n}) \times B_0 \cos(\omega t) \hat{y}$	
1:	$\vec{v} \times \vec{B} = \omega(u) B_0 \cos(\omega t) \sin(\alpha) \hat{x}$	
2:	$\vec{v} \times \vec{B} = \omega(u) B_0 \cos(\omega t) \sin(\alpha) \hat{x}$	
3:	$\vec{v} \times \vec{B} = -\omega(0.5b) B_0 \cos(\omega t) \sin(\alpha) \hat{x}$	
4:	$\vec{v} \times \vec{B} = \omega(u) B_0 \cos(\omega t) \sin(\alpha) \hat{x}$	
5:	$\vec{v} \times \vec{B} = \omega(0.5b) B_0 \cos(\omega t) \sin(\alpha) \hat{x}$	

1:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$\omega(u)B_0 \cos(\omega t) \sin(\alpha) \hat{x} \cdot d\vec{l}$	
2:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$\omega(u)B_0 \cos(\omega t) \sin(\alpha) \hat{x} \cdot d\vec{l}$	
3:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$-\omega(0.5b)B_0 \cos(\omega t) \sin(\alpha) \hat{x} \cdot d\vec{l}$	
4:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$\omega(u)B_0 \cos(\omega t) \sin(\alpha) \hat{x} \cdot d\vec{l}$	
5:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$\omega(0.5b)B_0 \cos(\omega t) \sin(\alpha) \hat{x} \cdot d\vec{l}$	
1:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$\omega(u)B_0 \cos(\omega t) \sin(\alpha) \hat{x} \cdot du \hat{u}$	
2:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$\omega(u)B_0 \cos(\omega t) \sin(\alpha) \hat{x} \cdot du \hat{u}$	
3:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$-\omega(0.5b)B_0 \cos(\omega t) \sin(\alpha) \hat{x} \cdot dx \hat{x}$	
4:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$\omega(u)B_0 \cos(\omega t) \sin(\alpha) \hat{x} \cdot du \hat{u}$	
5:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$\omega(0.5b)B_0 \cos(\omega t) \sin(\alpha) \hat{x} \cdot dx \hat{x}$	
1:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	0	
2:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	0	
3:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$-\omega(0.5b)B_0 \cos(\omega t) \sin(\alpha) dx$	
4:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	0	
5:	$(\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$\omega(0.5b)B_0 \cos(\omega t) \sin(\alpha) dx$	
$\oint (\vec{v} \times \vec{B}) \cdot d\vec{l} = \int_1 (\vec{v} \times \vec{B}) \cdot d\vec{l} + \int_2 (\vec{v} \times \vec{B}) \cdot d\vec{l} + \int_3 (\vec{v} \times \vec{B}) \cdot d\vec{l}$ $+ \int_4 (\vec{v} \times \vec{B}) \cdot d\vec{l} + \int_5 (\vec{v} \times \vec{B}) \cdot d\vec{l}$			
1:	$\int_1 (\vec{v} \times \vec{B}) \cdot d\vec{l} =$	0	
2:	$\int_2 (\vec{v} \times \vec{B}) \cdot d\vec{l} =$	0	
3:	$\int_3 (\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$\int_{0.5a}^{-0.5a} -\omega(0.5b)B_0 \cos(\omega t) \sin(\alpha) dx$	
4:	$\int_4 (\vec{v} \times \vec{B}) \cdot d\vec{l} =$	0	
5:	$\int_5 (\vec{v} \times \vec{B}) \cdot d\vec{l} =$	$\int_{-0.5a}^{0.5a} \omega(0.5b)B_0 \cos(\omega t) \sin(\alpha) dx$	

3:	$\int_3 (\vec{v} \times \vec{B}) \cdot \vec{dl} =$	$\int_{-0.5a}^{0.5a} \omega(0.5b)B_0 \cos(\omega t) \sin(\alpha) dx$	
3:	$\int_3 (\vec{v} \times \vec{B}) \cdot \vec{dl} =$	$\omega(0.5b)aB_0 \cos(\omega t) \sin(\alpha)$	
5:	$\int_5 (\vec{v} \times \vec{B}) \cdot \vec{dl} =$	$\omega(0.5b)aB_0 \cos(\omega t) \sin(\alpha)$	
$\oint (\vec{v} \times \vec{B}) \cdot \vec{dl} = \int_1 (\vec{v} \times \vec{B}) \cdot \vec{dl} + \int_2 (\vec{v} \times \vec{B}) \cdot \vec{dl} + \int_3 (\vec{v} \times \vec{B}) \cdot \vec{dl}$ $+ \int_4 (\vec{v} \times \vec{B}) \cdot \vec{dl} + \int_5 (\vec{v} \times \vec{B}) \cdot \vec{dl}$			
$\oint (\vec{v} \times \vec{B}) \cdot \vec{dl} = 0 + 0 + \omega(0.5b)aB_0 \cos(\omega t) \sin(\alpha) + 0$ $+ \omega(0.5b)aB_0 \cos(\omega t) \sin(\alpha)$			
$\oint (\vec{v} \times \vec{B}) \cdot \vec{dl} = ab\omega B_0 \cos(\omega t) \sin(\alpha)$			
$\oint (\vec{v} \times \vec{B}) \cdot \vec{dl} = ab\omega B_0 \cos(\omega t) \sin(\omega t)$			
$\Phi_{\text{motional}} = \oint \vec{v} \times \vec{B} \cdot \vec{dl} = ab\omega B_0 \cos(\omega t) \sin(\omega t)$			
$\Phi_{\text{total}} = \omega S B_0 \sin(2\omega t)$			
$\Phi_{\text{total}} = \Phi_{\text{transformer}} + \Phi_{\text{motional}}$			
$\Phi_{\text{total}} = ab\omega B_0 \cos(\omega t) \sin(\omega t) + ab\omega B_0 \cos(\omega t) \sin(\omega t)$			
$\Phi_{\text{total}} = 2 ab\omega B_0 \cos(\omega t) \sin(\omega t)$			
$\Phi_{\text{total}} = S\omega B_0 2\cos(\omega t) \sin(\omega t)$			
$\Phi_{\text{total}} = \omega S B_0 \sin(2\omega t) \text{ (volts)}$			